



# Aircraft Design

## Annexes

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Dernière révision 7/11/19

**2017 - 2019**

Réservé uniquement aux enseignants et élèves de l'Ecole Centrale Paris

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## Annex 1. The Design Process Milestones

### 1.1 List of requirements

#### Non exhaustive list of requirements

Dominant design criteria

##### Mission profile

Takeoff: altitude

Climb: time, altitude

Cruise: altitude, maxi range condition, maxi endurance condition, ...

Loiter: time, altitude

Descent: time, altitude

Landing: altitude

##### Performance

Minimum flight speed

Takeoff: runway surface, altitude min & max

Climb: minimum rate of climb, minimum climb slope, ...

Cruise: altitude, flight speed

Landing: runway surface, altitude min & max

Ceiling

Performance in turn

Maximum level flight speed

##### Power plant

Type of engine

##### Useful load

Pax number

Mass min & max

Maximum volume: H x L x l

##### Description

Electronics (Maximum power, voltage, intensity)

Droppable load

Camera

Maximum density

...

Fuel system

Instruments, Avionics, Furnishing

Air conditioning

##### Costs

Market price

Operating costs

##### Miscellaneous

Airworthiness requirements

Ecological requirements

Material

Safety

## 1.2 Conceptual design

### Phases of the Aircraft Conceptual Design

Check and/or adjustment of Customer's specifications

Synthesis of Airworthiness Requirements

Iterative process in order to find the optimal design (according to the specifications)

General layout definition

#### Geometry definition

Wing

Tails (Horizontal Tail, Vertical Tail, Canard Surface, Butterfly Tail, ...)

Fuselage (according to the Payload, Useful weight and Useful Volume definition)

Landing gear (Type, Lateral, Vertical and Longitudinal position)

#### Propulsion definition

Engine selection (Type of engine & List of engines to be used)

Fuel system (mass & volume)

Electric system (type & mass & volume of the batteries)

Performance (Stall speed, Takeoff distance, Maximum Rate of Climb, Cruise speed, Landing distance)

Wing loading definition

Power loading definition

#### Weight analysis

Empty weight, Useful weight, Payload, Fuel weight, Maximum Takeoff weight

#### Aerodynamic analysis

Global lift & drag

#### 2D Model

3-View drawing

Cross Sections

#### 3D Model

Visual check

#### Marketing analysis

Estimated Market Price

#### Validation

Reverse Engineering

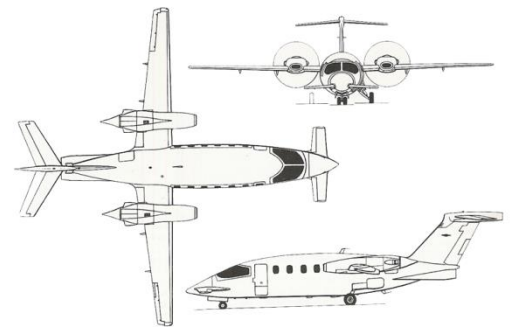
Statistical Analysis

#### Miscellaneous

Reports

Meetings

Final Report



## 1.3 Preliminary design

### Phases of the Aircraft Preliminary Design

#### Geometry

Lifting surfaces (Wing, Horizontal Tail, Vertical Tail, Canard Surface, Butterfly Tail, ...)

Planform optimization (span, twist, dihedral, sweep)

Position (incidence, vertical, longitudinal, ...)

Fuel volume

#### Fuselage

Shape optimization

Fuel Volume and/or Battery volume

Useful Volume

#### Landing Gear (Main & Auxiliary)

Tire size according to the runway surface

Shock absorber (type, dimension)

Length (propeller ground clearance, ...)

#### Nacelle

Shape optimization

#### Others

Hulls, Tailboom, Pylon, Ventral Fin, ...

#### 3D Model

Export to CAD

#### Propulsion

Uninstalled Engine power Vs Flight speed & Flight Altitude

Propeller characteristics (diameter, pitch angle (range), Tip speed, ...)

#### Aerodynamic analysis (for different flight conditions)

Drag (for each components & interference drag & trim drag & wave drag)

Airfoil optimization (airfoil performance)

Lift (for each components)

Airfoil optimization (airfoil performance)

Control surface definition (ailerons, leading edge, trailing edge devices, airbrakes, ...)

Type & position

Dimensions (chord & span & deflection)

#### Aerodynamic centre

Lifting surface

Wing & Fuselage

Airplane

- Neutral point stick fixed

- Neutral point stick free

- Maneuver point stick fixed

- Maneuver point stick free

#### Quality

Area rules

Streamline body check

**Cont.**

Graph report

Drag polar

- Flaps TO, gear down

- Flaps TO, gear up

- No flaps

- Flaps Ld, gear up

- Flaps Ld, gear down

- One Engine Inoperative (OEI)

- Normal flight condition @ different CG position

Drag report

Lift Vs Angle of Attack

Performance analysis (for different weight & CG position)

Mission specification

Stall

Deep stall

Takeoff

Climb

Cruise

Descent

Landing

Ground effect

Systems (Fuel, Electric, Hydraulic, ...)

Fuel system

Tank number & Volume & Position

Weight Analysis

Weight of each component

Weight breakdown

CG Position of each components

CG Position

CG Range

CG Enveloppe

Moment of Inertia

Load Analysis

V-n Diagram

Structural loads on the Fuselage

Structural loads on the Wing

Structural loads on the Horizontal Tail

Structural loads on the Canard Surface

Structural loads on the Vertical Tail

Structural loads on the Landing Gear

Structural loads on Control Surfaces

Structural loads on Control System



**Cont.**Stability & ControlLongitudinal stability derivatives

Steady state lift, drag, moment and thrust coefficients

Speed derivatives

Angle-of-attack derivatives

Rate of angle-of-attack derivatives

Pitch rate derivatives

Lateral-directional stability derivatives

Angle-of-sideslip derivatives

Rate of angle-of-sideslip derivatives

Roll rate derivatives

Yaw rate derivatives

Longitudinal control derivatives

Stabilizer control derivatives

Elevator control derivatives

Ruddervator control derivatives

Canard control derivatives

Canardvator control derivatives

Elevon control derivatives

Elevator tab control derivatives

Ruddervator tab control derivatives

Canardvator tab control derivatives

Elevon tab-control derivatives

Lateral-directional control derivatives

Aileron derivatives

Spoiler derivatives

Differential stabilizer derivatives

Rudder derivatives

Rudder tab derivatives

Aileron tab derivatives

Hinge moment derivatives

Aerodynamic balancing

Elevator stick force diagram

Aileron stick force diagram

Rudder stick force diagram

Trim diagram

**Cont.**Dynamic & Control

Longitudinal &amp; Lateral-directional dynamic characteristics

Airplane transfer functions

- Speed-to-Elevator
- Angle-of-Attack-to-Elevator
- Pitch-Angle-to-Elevator
- Speed-to-Ruddervator
- Angle-of-Attack-to-Ruddervator
- Pitch-Angle-to-Ruddervator
- Speed-to-Stabilizer
- Angle-of-Attack-to-Stabilizer
- Pitch-Angle-to-Stabilizer
- Speed-to-V-Tail
- Angle-of-Attack-to-V-Tail
- Pitch-Angle-to-V-Tail
- Speed-to-Elevon
- Angle-of-Attack-to-Elevon
- Pitch-Angle-to-Elevon
- Speed-to-Canardvator
- Angle-of-Attack-to-Canardvator
- Pitch-Angle-to-Canardvator
- Speed-to-Canard
- Angle-of-Attack-to-Canard
- Pitch-Angle-to-Canard
- Angle-of-Attack-to-Canardvator
- Human pilot
- Sideslip-Angle-to-Aileron
- Bank-Angle-to-Aileron
- Heading-Angle-to-Aileron
- Sideslip-Angle-to-Rudder
- Bank-Angle-to-Rudder
- Heading-Angle-to-Rudder

Cost Analysis

- Research, development, test and evaluation cost
- Prototype cost
- Manufacturing and acquisition costs
- Operating / Life cycle costs

Marketing Analysis

- Market price
- Comparative analysis

Optimization

Pollution / Quality analysis



**Cont.**

Validation

- Flight simulator
- Comparative analysis

Final checks

- Compliance with the specifications
- Compliance with the regulation
- Compliance with historical value
- Compliance with rules of thumbs (blanket of the horizontal tail - deep stall)

Miscellaneous

- Reports
  - Meetings
- Final Report
- Unusual concept (Wind tunnel test, ...)

## 1.4 Detail design

### Phases of the Aircraft Detail Design

#### New Techniques

- Validation of processes

#### Airplane

- 3D Model of each components (position, dimensions, ...) to check the interaction between components

#### Lifting surfaces (Wing, Horizontal tail, Vertical Tail, Canard surface, Winglets, ...)

- Stress analysis

- Spar sizing

- Ribs sizing

- Skin sizing

- 2D / 3D drawings

#### Control surfaces (Ailerons, Flaps, Elevator, Rudder, Canarvator)

- Stress analysis

- Spar sizing

- Ribs sizing

- Skin sizing

- 2D / 3D drawings

#### Engine Mount

- Stress analysis

- Sizing

- 2D / 3D drawings

#### Engine Cover

- Stress analysis

- Skin sizing

- 2D / 3D drawings

#### Engine Cooling

- Sizing

- 2D / 3D drawings

#### Bodies (Fuselage, Nacelle, Tailboom, ...)

- Stress analysis

- Frame sizing

- Stringer sizing

- Skin sizing

- Bulkhead sizing

- 2D / 3D drawings

#### Pylon

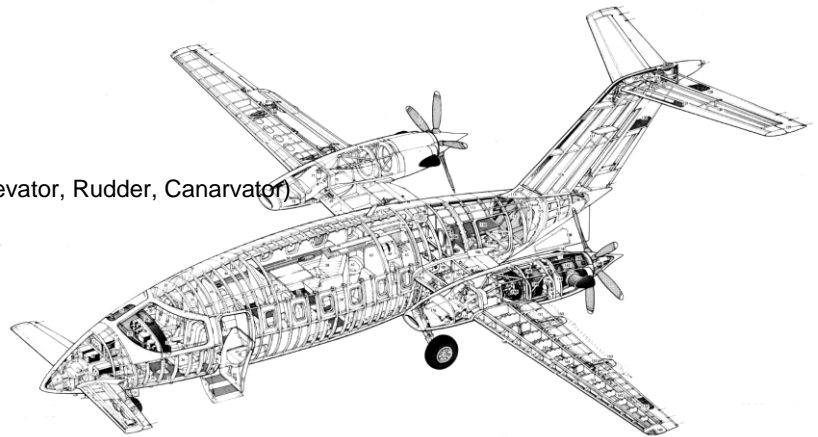
- Stress analysis

- Spar sizing

- Ribs sizing

- Skin sizing

- 2D / 3D drawings



**Cont.**

Landing gear (Main & Auxiliary)

- Stress analysis
- Sizing
- 3D drawings
- 2D drawings

Control System

- Stress analysis
- Sizing
- 3D drawings
- 2D drawings

Systems (Electric, Pneumatic, Hydraulic, Fuel, Water, Starter, APU, Anti-Ice, ...)

- Sizing
- 3D drawings
- 2D drawings

Instrument Panel

- Sizing
- 3D drawings
- 2D drawings

Furnishing

- Sizing
- 3D drawings
- 2D drawings

APU Mount

- Stress analysis
- Sizing
- 3D drawings
- 2D drawings

Canopy

- Sizing
- 3D drawings
- 2D drawings

Tools & jigs

Documents

- List of parts
- Manuals (Flight, Maintenance, ...)



## 1.5 Next phases

### Life cycle of the aircraft

- Testing
- Prototyping
- Handling
- Manufacturing
- Assembling
- Testing
- Storing
- (Distribution)
- (Installation)
- Operation
- Maintenance
- Upgrading
- Removing
- Disposal (recycling)

**Annex 2. Common values**

|                 |                             |                   | MCR01 | Diamond DA42 | A320-200               | A330-200               | A380-800                            |
|-----------------|-----------------------------|-------------------|-------|--------------|------------------------|------------------------|-------------------------------------|
| General         | Category                    | -                 | Light | Light        | Airliner               | Airliner               | Airliner                            |
|                 | Seat Capacity               | -                 | 2     | 4            | 150 - (2)<br>180 - (1) | 253 - (3)<br>380 - (1) | 525 - (3)<br>644 - (2)<br>853 - (1) |
| Weight          | Empty                       | kg                | 230   | 1268         | 41 300                 | 119 600                | 270 364                             |
|                 | Fuel                        | kg                | 58    | 157          | 23 700                 | 109 185                | 253 983                             |
|                 | Payload                     | kg                | 255   | 412          | 19 700                 | 49 000                 | 83 000                              |
|                 | Maximum                     | kg                | 490   | 1700         | 75 900                 | 238 000                | 569 000                             |
| Weight Ratio    | $W_{Empty}/W_{MxTO}$        | -                 | 0.469 | 0.746        | 0.544                  | 0.503                  | 0.475                               |
|                 | $W_{Fuel}/W_{MxTO}$         | -                 | 0.118 | 0.092        | 0.312                  | 0.459                  | 0.446                               |
|                 | $W_{Payload}/W_{MxTO}$      | -                 | 0.520 | 0.242        | 0.260                  | 0.206                  | 0.146                               |
| Dimensions      | Length                      | m                 | 5.48  | 8.56         | 37.57                  | 58.82                  | 72.72                               |
|                 | Span                        | m                 | 6.63  | 13.42        | 34.1                   | 60.3                   | 79.75                               |
|                 | Wing Area                   | m <sup>2</sup>    | 5.2   | 16.29        | 122.6                  | 361.6                  | 845                                 |
|                 | Tails Area                  | m <sup>2</sup>    | 1.602 | 4.668        | 52.5                   |                        |                                     |
|                 | Aspect Ratio                | -                 | 8.5   | 11.1         | 9.5                    | 10.1                   | 7.5                                 |
| Dimension Ratio | Length / Span               | -                 | 0.827 | 0.638        | 1.102                  | 0.975                  | 0.912                               |
|                 | Tails Ratio                 | -                 | 0.308 | 0.287        | 0.428                  |                        |                                     |
| Power Plant     | Engine number               | -                 | 1     | 2            | 2                      | 2                      | 4                                   |
|                 | Power (total)               | kW                | 69    | 198          | -                      | -                      | -                                   |
|                 | Thrust                      | daN               | -     | -            | 22 237                 | 60 000                 | 142 700                             |
|                 | SFC (propeller)             | kg/kW.h           | 0.238 | 0.212        | -                      | -                      | -                                   |
|                 | SFC (jet) <sub>Cruise</sub> | kg/N.h            | -     | -            | 0.061                  | 0.057                  | 0.059                               |
|                 | Fuel Flow                   | kg/h              | -     | -            | 3023                   | 7622                   | 18763                               |
|                 | Propeller efficiency        | -                 | 0.82  | 0.85         | -                      | -                      | -                                   |
| Aerodynamics    | Cl cruise                   | -                 | 0.25  | 0.34         | 0.63                   | 0.61                   | 0.58                                |
|                 | Cl <sub>Mx</sub>            | -                 | 2.36  | 2.00         |                        |                        |                                     |
|                 | e                           | -                 | 0.71  | 0.78         | 0.85                   | 0.85                   | 0.85                                |
|                 | Glide Ratio                 | -                 | 9     | 10.5         |                        |                        |                                     |
|                 | Wing loading <sub>Mx</sub>  | kg/m <sup>2</sup> | 94.2  | 104.4        | 619.1                  | 658.2                  | 673.4                               |
| Performance     | Cruise speed                | km/h              | 318   | 283          | 828                    | 870                    | 902                                 |
|                 | Cruise speed                | Mach              | -     | -            | 0.78                   | 0.82                   | 0.85                                |
|                 | Stall speed                 | km/h              | 91    | 104          |                        |                        |                                     |
|                 | Takeoff speed               | km/h              | 105   | 120          |                        |                        |                                     |
|                 | Takeoff run                 | m                 | 155   | 382          | 2 090                  | 2 220                  | 2 750                               |
|                 | Rate of Climb <sub>Mx</sub> | m/s               | 8.89  | 5.46         | 12.2                   |                        |                                     |
|                 | Maxi Range                  | km                |       |              | 7 000                  | 17 000                 | 18 000                              |
|                 | Power-to-Weight Ratio       | kW/kg             | 0.141 | 0.116        |                        |                        |                                     |
|                 | Weigh-to-Power Ratio        | kg/kW             | 7.101 | 8.586        |                        |                        |                                     |
|                 | Thrust-to-Weight Ratio      | daN/kg            | -     | -            | 0.293                  | 0.252                  | 0.251                               |
|                 | Weight-to-Thrust Ratio      | kg/daN            | -     | -            | 3.413                  | 3.967                  | 3.987                               |



|      |                   |       | MCR01 | Diamond<br>DA42 | A320-200 | A330-200 | A380-800 |
|------|-------------------|-------|-------|-----------------|----------|----------|----------|
| Cost | Unit Price (2012) | M\$   | 0.11  | 0.54            | 88       | 208      | 390      |
|      | M\$ / Seat        | M\$   | 0.055 | 0.135           | 0.489    | 0.547    | 0.457    |
|      | \$ / kg Empty     | \$/kg | 478   | 426             | 2131     | 1739     | 1442     |
|      | \$ / kg Payload   | \$/kg | 431   | 1311            | 4467     | 4245     | 4699     |
|      | \$ / kg Maximum   | \$/kg | 224   | 318             | 1159     | 874      | 685      |



### Annex 3. Forces and moments

An aircraft is nothing else than a car: a means to transport passengers or goods from one point to the other. With the only difference, that we would like not to travel on the ground but in the air.

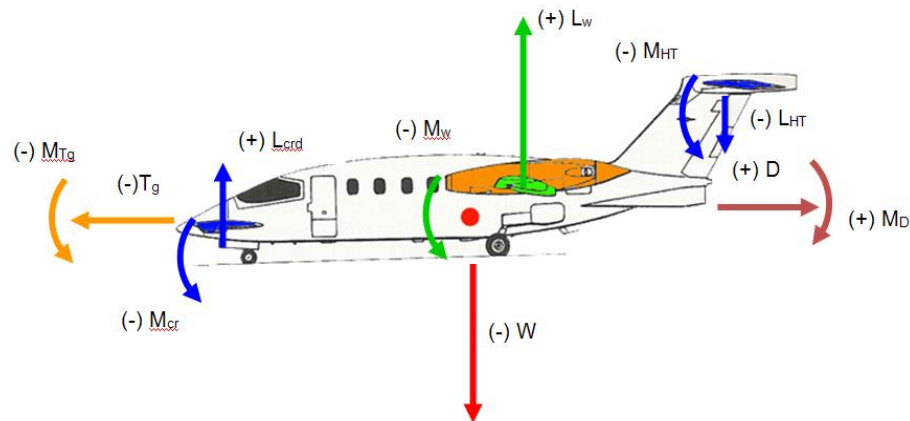
Due to the gravity, this mass (the aircraft) generates a force acting downwards: the weight ( $W$ ) of the aircraft.

To move the aircraft, we need to generate a force that will pull the aircraft forward. This force ( $T_g$ ) is generated by the engine (piston engine, turboprop, turbojet, rocket, ...).

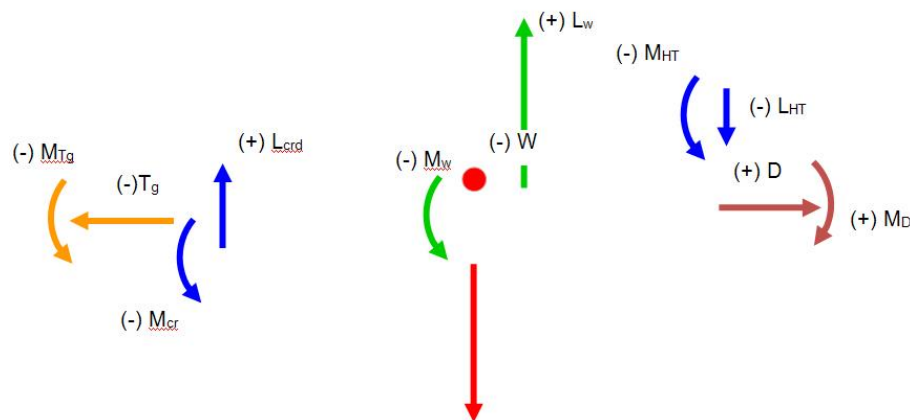
Unfortunately because of the physical properties of the air, every moving generates a drag ( $D$ ), a force acting in the opposite direction of the motion.

To lift the aircraft in the air, we need to add something to generate a vertical force ( $L_w$ ) acting upwards: the wing. The wing generates the lift but also a nose-down pitching moment.

To counteract this nose-down pitching moment, we need to generate forces ( $L_{cr}$ ,  $L_{HT}$ ) acting upwards and/or downwards depending on their location about the CG position.



An aircraft, in level flight in the air, is nothing else than forces in equilibrium around the CG. The designer will size the aircraft in order that this equilibrium remains for a given CG range.



## Annex 4. The standard atmosphere

### 4.1 Introduction

Since the real atmosphere never remains constant at any particular time or place, a hypothetical model must be used as an approximation to what may be expected. This model is known as the standard atmosphere.

### 4.2 Assumptions

Some assumptions are made in order to build the standard atmosphere:

1. The air in the model is assumed to be without dust, moisture and water vapour.
2. The air is supposed to be at rest with respect to the earth, this means that there is no wind, no turbulence.
3. The reference altitude is the mean sea level (MSL). At the MSL the conditions are:

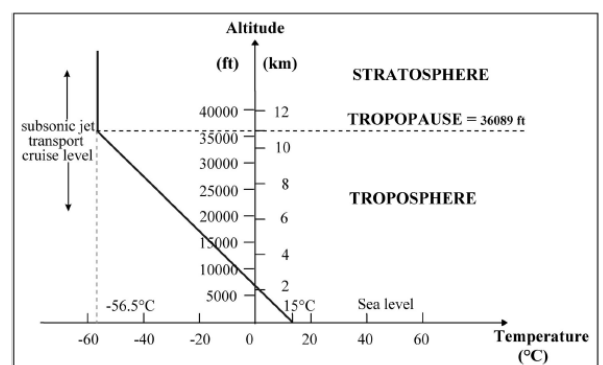
|                         |          |              |                   |
|-------------------------|----------|--------------|-------------------|
| Pressure                | $p_0$    | 101 325      | N/m <sup>2</sup>  |
| Density                 | $\rho_0$ | 1.225        | kg/m <sup>3</sup> |
| Temperature             | $T_0$    | 288.15<br>15 | °K<br>°C          |
| Speed of sound          | $a_0$    | 340.294      | m/s               |
| Acceleration of gravity | $g_0$    | 9.80665      | m/s <sup>2</sup>  |

4. The air is considered to be a perfect gas  $p = \rho \cdot R \cdot T$  with R is the real gas constant for the air (287 J/kg.K)
5. The temperature decreases with altitude at a constant rate of -6.5°C/1000m up to the tropopause
6. The standard tropopause altitude is 11 000m
7. The temperature remains constant at a value of -56.5°C from the tropopause up to 20 000 m

### 4.3 Standard temperature

The temperature decreases with altitude at a constant rate of -6.5°C/1000m up to the tropopause

$$T = T_0 - 6.5 \cdot \frac{h(m)}{1000}$$

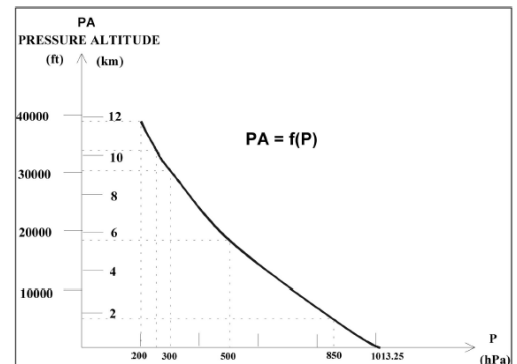


#### 4.4 Standard pressure

To compute the standard pressure ( $p$ ) at a given altitude, the temperature is assumed standard and the air is assumed to be a perfect gas.

$$p = p_0 \cdot \left( 1 - 0.0065 \cdot \frac{h}{T_0} \right)^{5.2561}$$

with the unit of  $T_0$  is °K and  $h$  is meters



#### 4.5 Standard density

To compute the standard density ( $\rho$ ), since the pressure and temperature are known for a given altitude, the perfect gas equation is used

$$\rho = \frac{P}{R \cdot T}$$

#### 4.6 Speed of sound

The speed of sound is proportional to the square root of the absolute temperature (K) but is independent of pressure or density for a given ideal gas. The sound travels faster in fluid than it does in air (4.3 times faster in water, 15 times faster in iron than in air at 20°C)

$$a = \sqrt{\gamma \cdot R \cdot T}, \text{ with } \gamma, \text{ the isentropic coefficient (1.4 for the air).}$$

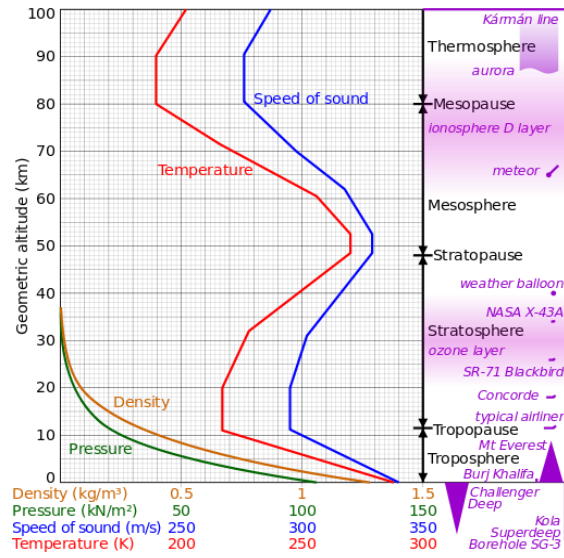
#### 4.7 Notes

The altitude obtained from the measurement of pressure is called the **pressure altitude**.

The altitude obtained from the measurement of density is called the **density altitude**. In other words, the density altitude is the altitude in the ISA model at which the air density would be equal to the actual air density at the place of observation.

The ISA model is used as a reference. If the real atmospheric conditions are different, they will be expressed as ISA +/-ΔISA (ISA+10°C)

### 4.8 The standard atmosphere up to 100.000 m



4.9 Table of the standard atmosphere

| ALTITUDE<br>(Feet) | TEMP.<br>(°C) | PRESSURE |       |       | PRESSURE<br>RATIO<br>$\delta = P/P_0$ | DENSITY<br>$\sigma = \rho/\rho_0$ | Speed of<br>sound<br>(kt) | ALTITUDE<br>(meters) |
|--------------------|---------------|----------|-------|-------|---------------------------------------|-----------------------------------|---------------------------|----------------------|
|                    |               | hPa      | PSI   | In.Hg |                                       |                                   |                           |                      |
| 40 000             | - 56.5        | 188      | 2.72  | 5.54  | 0.1851                                | 0.2462                            | 573                       | 12 192               |
| 39 000             | - 56.5        | 197      | 2.58  | 5.81  | 0.1942                                | 0.2583                            | 573                       | 11 887               |
| 38 000             | - 56.5        | 206      | 2.99  | 6.10  | 0.2038                                | 0.2710                            | 573                       | 11 582               |
| 37 000             | - 56.5        | 217      | 3.14  | 6.40  | 0.2138                                | 0.2844                            | 573                       | 11 278               |
| 36 000             | - 56.3        | 227      | 3.30  | 6.71  | 0.2243                                | 0.2981                            | 573                       | 10 973               |
| 35 000             | - 54.3        | 238      | 3.46  | 7.04  | 0.2353                                | 0.3099                            | 576                       | 10 668               |
| 34 000             | - 52.4        | 250      | 3.63  | 7.38  | 0.2467                                | 0.3220                            | 579                       | 10 363               |
| 33 000             | - 50.4        | 262      | 3.80  | 7.74  | 0.2586                                | 0.3345                            | 581                       | 10 058               |
| 32 000             | - 48.4        | 274      | 3.98  | 8.11  | 0.2709                                | 0.3473                            | 584                       | 9 754                |
| 31 000             | - 46.4        | 287      | 4.17  | 8.49  | 0.2837                                | 0.3605                            | 586                       | 9 449                |
| 30 000             | - 44.4        | 301      | 4.36  | 8.89  | 0.2970                                | 0.3741                            | 589                       | 9 144                |
| 29 000             | - 42.5        | 315      | 4.57  | 9.30  | 0.3107                                | 0.3881                            | 591                       | 8 839                |
| 28 000             | - 40.5        | 329      | 4.78  | 9.73  | 0.3250                                | 0.4025                            | 594                       | 8 534                |
| 27 000             | - 38.5        | 344      | 4.99  | 10.17 | 0.3398                                | 0.4173                            | 597                       | 8 230                |
| 26 000             | - 36.5        | 360      | 5.22  | 10.63 | 0.3552                                | 0.4325                            | 599                       | 7 925                |
| 25 000             | - 34.5        | 376      | 5.45  | 11.10 | 0.3711                                | 0.4481                            | 602                       | 7 620                |
| 24 000             | - 32.5        | 393      | 5.70  | 11.60 | 0.3876                                | 0.4642                            | 604                       | 7 315                |
| 23 000             | - 30.6        | 410      | 5.95  | 12.11 | 0.4046                                | 0.4806                            | 607                       | 7 010                |
| 22 000             | - 28.6        | 428      | 6.21  | 12.64 | 0.4223                                | 0.4976                            | 609                       | 6 706                |
| 21 000             | - 26.6        | 446      | 6.47  | 13.18 | 0.4406                                | 0.5150                            | 611                       | 6 401                |
| 20 000             | - 24.6        | 466      | 6.75  | 13.75 | 0.4595                                | 0.5328                            | 614                       | 6 096                |
| 19 000             | - 22.6        | 485      | 7.04  | 14.34 | 0.4791                                | 0.5511                            | 616                       | 5 791                |
| 18 000             | - 20.7        | 506      | 7.34  | 14.94 | 0.4994                                | 0.5699                            | 619                       | 5 406                |
| 17 000             | - 18.7        | 527      | 7.65  | 15.57 | 0.5203                                | 0.5892                            | 621                       | 5 182                |
| 16 000             | - 16.7        | 549      | 7.97  | 16.22 | 0.5420                                | 0.6090                            | 624                       | 4 877                |
| 15 000             | - 14.7        | 572      | 8.29  | 16.89 | 0.5643                                | 0.6292                            | 626                       | 4 572                |
| 14 000             | - 12.7        | 595      | 8.63  | 17.58 | 0.5875                                | 0.6500                            | 628                       | 4 267                |
| 13 000             | - 10.8        | 619      | 8.99  | 18.29 | 0.6113                                | 0.6713                            | 631                       | 3 962                |
| 12 000             | - 8.8         | 644      | 9.35  | 19.03 | 0.6360                                | 0.6932                            | 633                       | 3 658                |
| 11 000             | - 6.8         | 670      | 9.72  | 19.79 | 0.6614                                | 0.7156                            | 636                       | 3 353                |
| 10 000             | - 4.8         | 697      | 10.10 | 20.58 | 0.6877                                | 0.7385                            | 638                       | 3 048                |
| 9 000              | - 2.8         | 724      | 10.51 | 21.39 | 0.7148                                | 0.7620                            | 640                       | 2 743                |
| 8 000              | - 0.8         | 753      | 10.92 | 22.22 | 0.7428                                | 0.7860                            | 643                       | 2 438                |
| 7 000              | + 1.1         | 782      | 11.34 | 23.09 | 0.7716                                | 0.8106                            | 645                       | 2 134                |
| 6 000              | + 3.1         | 812      | 11.78 | 23.98 | 0.8014                                | 0.8359                            | 647                       | 1 829                |
| 5 000              | + 5.1         | 843      | 12.23 | 24.90 | 0.8320                                | 0.8617                            | 650                       | 1 524                |
| 4 000              | + 7.1         | 875      | 12.69 | 25.84 | 0.8637                                | 0.8881                            | 652                       | 1 219                |
| 3 000              | + 9.1         | 908      | 13.17 | 26.82 | 0.8962                                | 0.9151                            | 654                       | 914                  |
| 2 000              | + 11.0        | 942      | 13.67 | 27.82 | 0.9298                                | 0.9428                            | 656                       | 610                  |
| 1 000              | + 13.0        | 977      | 14.17 | 28.86 | 0.9644                                | 0.9711                            | 659                       | 305                  |
| 0                  | + 15.0        | 1013     | 14.70 | 29.92 | 1.0000                                | 1.0000                            | 661                       | 0                    |
| - 1 000            | + 17.0        | 1050     | 15.23 | 31.02 | 1.0366                                | 1.0295                            | 664                       | - 305                |

## Annex 5. Airspeed

### 5.1 Introduction

Airspeed is the speed of the aircraft relative to the air. The measurement is made by a pitot-static system. The indication is made on board by an airspeed indicator.

### 5.2 Pitot-static system

The airspeed is measured by a pressure-sensitive instrument called the pitot-static system

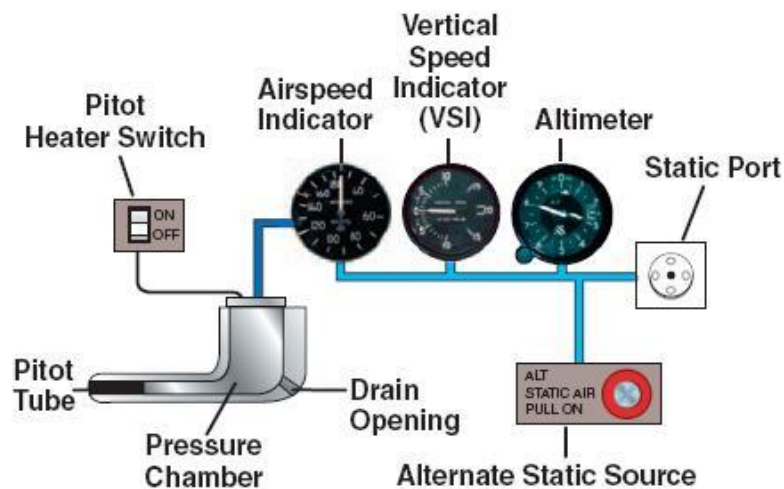


Image 1 : Pitot-static system

Using the Bernoulli's law, which states that the total pressure is the sum of the static pressure and the dynamic pressure.

$$p_t = p_s + \left( \frac{\rho \cdot V^2}{2} \right)$$

Solving that for velocity we get:

$$V = \sqrt{\frac{2 \cdot (p_t - p_s)}{\rho}}$$

### 5.3 Airspeed indicator

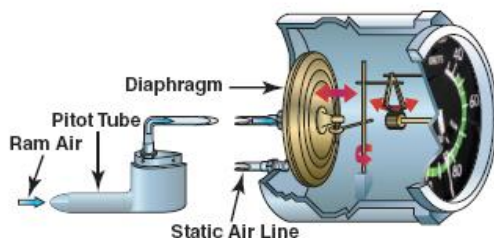


Image 2 : Airspeed indicator

### 5.4 Altimeter and Vertical airspeed indicator

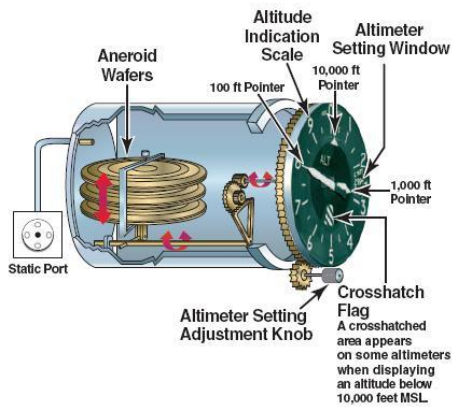


Image 3 : Altimeter

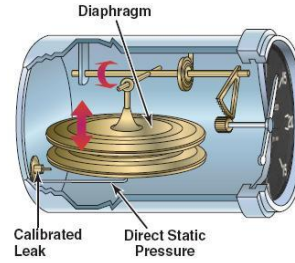


Image 4 : Vertical airspeed indicator

### 5.5 Pitot-static system on the Airbus A330-200

Location of the pitot probe and static port on the airbus A330-200

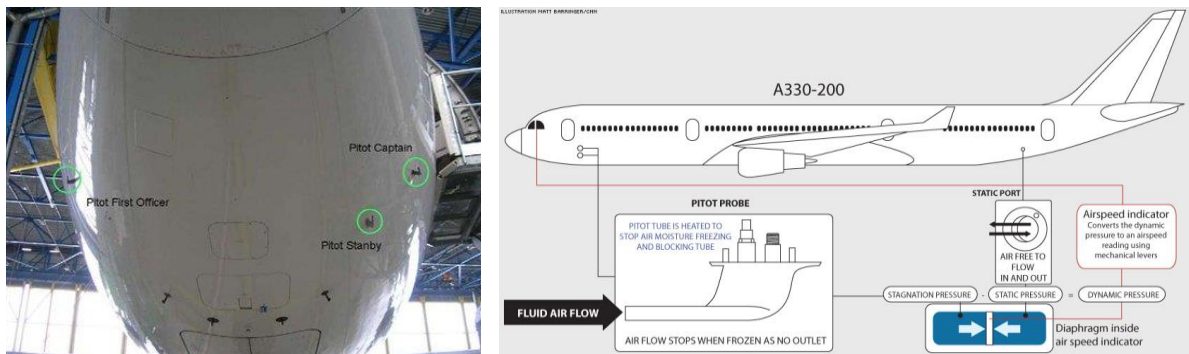


Image 5 : Pitot-static system on the Airbus A330-200

Three pitot probes are located in the front of the fuselage. From right to left:

- Pitot Captain
- Pitot Standby
- Pitot First Officer

## 5.6 Airspeed relationships

### 5.6.1 IAS – Indicated airspeed

Indicated airspeed is that shown on the airspeed indicator.

### 5.6.2 CAS – Calibrated airspeed

Calibrated airspeed is the indicated airspeed (IAS) corrected for position and instrument error.

### 5.6.3 EAS – Equivalent airspeed

Equivalent airspeed is calibrated airspeed (CAS) corrected for compressibility effect.

$$EAS = CAS \cdot \sqrt{\frac{p}{p_0} \cdot \left[ \frac{(q_c/p + 1)^{0.286} - 1}{(q_c/p_0 + 1)^{0.286} - 1} \right]^{0.5}}$$

With

|       |   |
|-------|---|
| $p$   | Pressure at the given altitude            |
| $p_0$ | Pressure at sea level                     |
| $q_c$ | $p \cdot ([1 + 0.2 \cdot M^2]^{3.5} - 1)$ |
| $M$   | $TAS/a$                                   |
| $a$   | Speed of sound                            |

### 5.6.4 TAS – True airspeed

True airspeed is the equivalent airspeed (EAS) corrected for change in atmospheric density.

$$TAS = EAS \cdot \sqrt{\frac{\rho_0}{\rho}}$$

With

|          |                               |
|----------|-------------------------------|
| $\rho$   | Density at the given altitude |
| $\rho_0$ | Density at sea level          |

### 5.6.5 GS – Ground speed

Ground speed is the speed relative to the ground.



## 5.7 Example

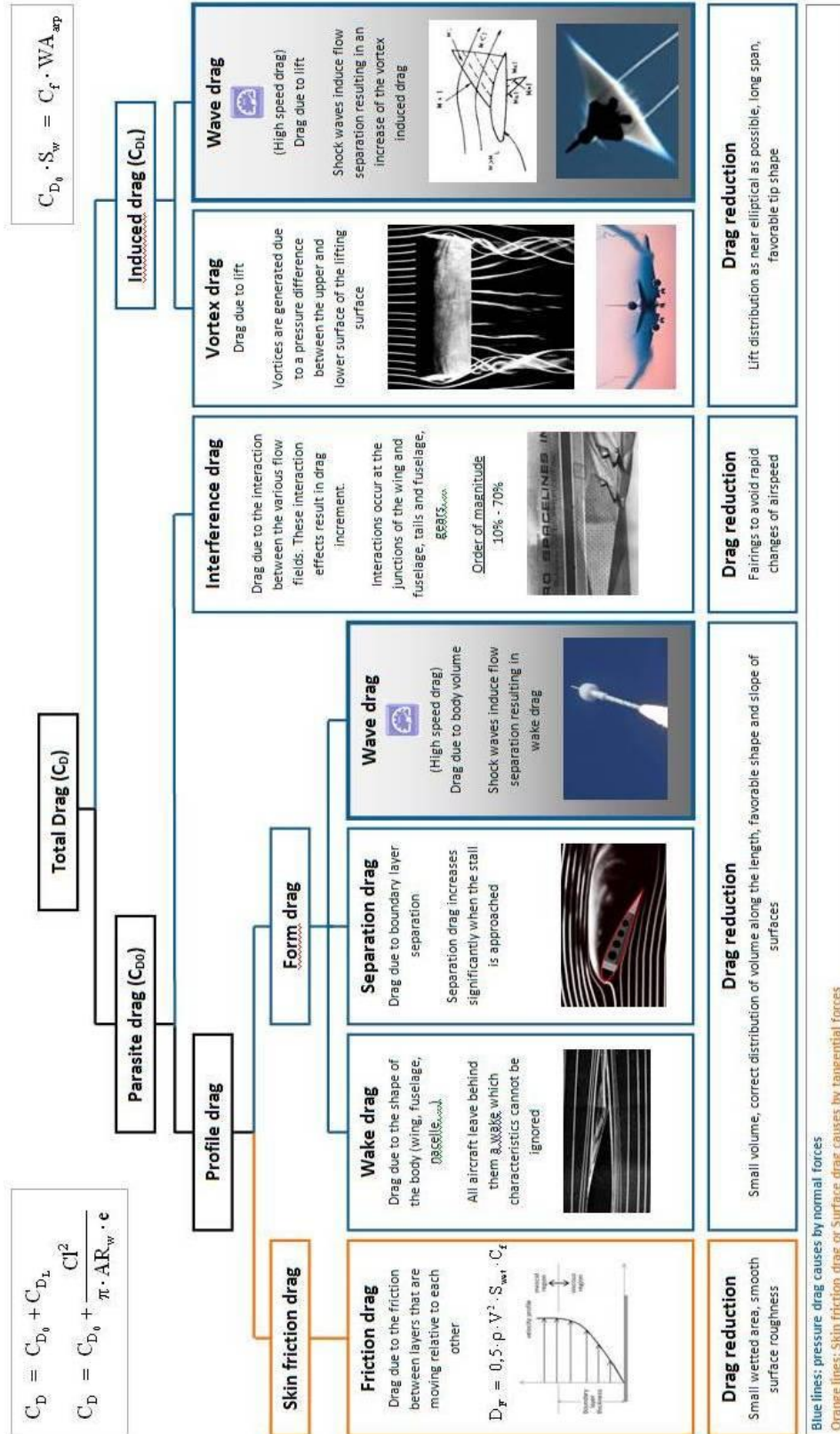
### Given

|                 |                          |
|-----------------|--------------------------|
| M               | 0.411                    |
| Flight altitude | 4000 m                   |
| $\rho$          | 0.819 kg/m <sup>3</sup>  |
| p               | 61 660 N/m <sup>2</sup>  |
| a               | 324.6 m/s                |
| $\rho_0$        | 1.225 kg/m <sup>3</sup>  |
| $p_0$           | 101.330 N/m <sup>2</sup> |
| $q_c$           | 7 995 N/m <sup>2</sup>   |

### Computed

| IAS     | CAS     | EAS     | TAS     |
|---------|---------|---------|---------|
| 110 m/s | 110 m/s | 109 m/s | 133 m/s |

## Annex 6. Drag breakdown



## Annex 7. Optimisation process

### 7.1 Cruising speed (propeller driven aircraft)

The relationship between wing loading and power loading for a propeller driven aircraft at cruise is given by

$$\frac{W}{P_{\text{eng}}} = R_P \cdot \frac{c_2 \cdot W/S_w}{c_3 + c_1 \cdot (W/S_w)^2}$$

with

$$R_P = \frac{\left(\frac{\rho}{1.225}\right)^{-0.15}}{0.85}$$

$$c_1 = \frac{1}{V} \cdot \frac{1}{\pi \cdot AR_w \cdot e} \cdot \frac{4 \cdot g^2}{\rho^2}$$

$$c_2 = \frac{2 \cdot \eta_p}{\rho}$$

$$c_3 = V^3 \cdot C_{D_0}$$

Development of the relationship between wing loading and power loading at cruise

$$\begin{aligned} P_{\text{avai}} \cdot \eta_p &= 0.5 \cdot \rho \cdot V^3 \cdot C_D \cdot S_w \\ V^3 &= \frac{2 \cdot P_{\text{avai}} \cdot \eta_p}{\rho \cdot C_D \cdot S_w} \\ V^3 &= \frac{2 \cdot \eta_p}{\rho \cdot C_D} \cdot \frac{W/S_w}{W/P_{\text{avai}}} \\ V^3 &= \frac{2 \cdot \eta_p}{\rho \cdot C_D} \cdot \frac{W/S_w}{W/P_{\text{avai}}} \text{ and } C_D = C_{D_0} + \frac{C_L^2}{\pi \cdot AR_w \cdot e} \text{ and } C_L = \frac{2 \cdot g}{\rho \cdot V^2} \cdot \frac{W}{S_w} \\ V^3 &= \frac{2 \cdot \eta_p}{\rho} \cdot \frac{W/S_w}{W/P_{\text{avai}}} \cdot \frac{1}{C_{D_0} + \frac{1}{\pi \cdot AR_w \cdot e} \cdot \left(\frac{2 \cdot g}{\rho \cdot V^2}\right)^2 \cdot \left(\frac{W}{S_w}\right)^2} \\ V^3 \cdot C_{D_0} + \frac{V^3}{\pi \cdot AR_w \cdot e} \cdot \frac{4 \cdot g^2}{\rho^2 \cdot V^4} \cdot \left(\frac{W}{S_w}\right)^2 &= \frac{2 \cdot \eta_p}{\rho} \cdot \frac{W/S_w}{W/P_{\text{avai}}} \\ \frac{1}{V} \cdot \frac{1}{\pi \cdot AR_w \cdot e} \cdot \frac{4 \cdot g^2}{\rho^2} \cdot \left(\frac{W}{S_w}\right)^2 - \frac{2 \cdot \eta_p}{\rho} \cdot \frac{W/S_w}{W/P_{\text{avai}}} + V^3 \cdot C_{D_0} &= 0 \end{aligned}$$

$$\begin{aligned}
 c_1 \cdot \left( \frac{W}{S_w} \right)^2 - c_2 \cdot \frac{W/S_w}{W/P_{\text{avai}}} + c_3 &= 0 \\
 c_2 \cdot \frac{W/S_w}{W/P_{\text{avai}}} - c_1 \cdot \left( \frac{W}{S_w} \right)^2 &= c_3 \\
 \frac{W}{P_{\text{avai}}} &= \frac{c_2 \cdot W/S_w}{c_3 + c_1 \cdot (W/S_w)^2} \\
 \frac{W}{P_{\text{eng}}} &= R_P \cdot \frac{W}{\text{BHP}_{\text{avai}}} \\
 \frac{W}{P_{\text{eng}}} &= R_P \cdot \frac{c_2 \cdot W/S_w}{c_3 + c_1 \cdot (W/S_w)^2}
 \end{aligned}$$

## 7.2 Stall speed

The relationship between wing loading and power loading at stall is given by

$$\boxed{\frac{W}{S_w} = \frac{\rho}{2 \cdot g} \cdot V_s^2 \cdot C_{L_2}}$$

Development of the relationship between wing loading and power loading at stall

$$\begin{aligned}
 L &= W \cdot g \\
 W \cdot g &= 0.5 \cdot \rho \cdot V_s^2 \cdot S_w \cdot C_{L_2} \\
 \frac{W}{S_w} &= \frac{\rho}{2 \cdot g} \cdot V_s^2 \cdot C_{L_2}
 \end{aligned}$$

The stall performance is independent of the power loading and is only function of the wing loading.

## 7.3 Landing field length

The relationship between wing loading and power loading at landing is given by

$$\boxed{\frac{W}{S_w} = \frac{\rho}{2 \cdot g} \cdot V_{\text{approach}}^2 \cdot C_L}$$

Development of the relationship between wing loading and power loading at landing

$$\begin{aligned}
 L &= W \cdot g \\
 W \cdot g &= 0.5 \cdot \rho \cdot V_{\text{approach}}^2 \cdot S_w \cdot C_L \quad \text{and} \quad V_{\text{approach}} = 1.3 \cdot V_s \\
 \frac{W}{S_w} &= \frac{\rho}{2 \cdot g} \cdot V_{\text{approach}}^2 \cdot C_L
 \end{aligned}$$

The landing performance is independent of the power loading and is only function of the wing loading

#### 7.4 Takeoff field length (propeller driven aircraft)

The relationship between wing loading and power loading for a propeller driven aircraft at takeoff is given by

$$\frac{W}{P_{\text{eng}}} = R_p \cdot \frac{C_1 \cdot C_5 \cdot \left(\frac{1}{W/S_w}\right)^{0.5}}{(W/S_w) + C_5 \cdot C_6}$$

With

$$R_p = \frac{\left(\frac{\rho}{1.225}\right)^{-0.15}}{0.85}$$

$$C_1 = \eta_p \cdot \left(\frac{\rho \cdot C_L}{2 \cdot g}\right)^{0.5}$$

$$C_2 = \frac{\rho \cdot C_{D_0}}{2} \cdot \left(\frac{2 \cdot g}{\rho \cdot C_L}\right)$$

$$C_3 = g \cdot c_{f_{gr}}$$

$$C_4 = g \cdot \sin \gamma$$

$$C_5 = \frac{d \cdot \rho \cdot C_L}{g}$$

$$C_6 = C_2 + C_3 + C_4$$

Development of the relationship between wing loading and power loading at takeoff

$$d = \frac{a \cdot t^2}{2} = \frac{V^2}{2 \cdot a}$$

$$a = \frac{F}{W} = \frac{T_g - D_0 - F_{\text{friction}} - F_{\text{slope}}}{W}$$

with

$$T_g = \frac{P_{\text{avail}} \cdot \eta_p}{V} \quad \text{and} \quad D_0 = \frac{\rho}{2} \cdot V^2 \cdot C_{D_0} \cdot S_w \quad \text{and} \quad F_{\text{friction}} = W \cdot g \cdot c_{f_{gr}} \quad \text{and} \quad F_{\text{slope}} = W \cdot g \cdot \sin \gamma$$

$$a = \frac{1}{W/P_{\text{avail}}} \cdot \frac{\eta_p}{V} - \frac{\rho}{2} \cdot V^2 \cdot C_{D_0} \cdot \frac{1}{W/S_w} - g \cdot c_{f_{gr}} - g \cdot \sin \gamma$$

with

$$V^2 = \frac{2 \cdot g}{\rho \cdot C_L} \cdot \frac{W}{S_w}$$

$$a = \frac{\eta_p}{W/P_{\text{avail}}} \cdot \left(\frac{\rho \cdot C_L}{2 \cdot g}\right)^{0.5} \cdot \left(\frac{1}{W/S_w}\right)^{0.5} - \frac{\rho \cdot C_{D_0}}{2} \cdot \left(\frac{2 \cdot g}{\rho \cdot C_L} \cdot \frac{W}{S_w}\right) \cdot \frac{1}{W/S_w} - g \cdot c_{f_{gr}} - g \cdot \sin \gamma$$

$$C_1 = \eta_p \cdot \left( \frac{\rho \cdot C_L}{2 \cdot g} \right)^{0.5}, \quad C_2 = \frac{\rho \cdot C_{D0}}{2} \cdot \left( \frac{2 \cdot g}{\rho \cdot C_L} \right), \quad C_3 = g \cdot c_{f_{gr}}, \quad C_4 = g \cdot \sin \gamma$$

$$a = C_1 \cdot \frac{1}{W/P_{avail}} \cdot \left( \frac{1}{W/S_w} \right)^{0.5} - C_2 - C_3 - C_4$$

$$d = \frac{g}{\rho \cdot C_L} \cdot (W/S_w) \cdot \frac{1}{C_1 \cdot \left( \frac{1}{W/P_{avail}} \right) \cdot \left( \frac{1}{W/S_w} \right)^{0.5} - C_2 - C_3 - C_4}$$

$$C_6 = C_2 + C_3 + C_4$$

$$C_5 = \frac{d \cdot \rho \cdot C_L}{g}$$

$$C_5 = (W/S_w) \cdot \frac{1}{C_1 \cdot \left( \frac{1}{W/P_{avail}} \right) \cdot \left( \frac{1}{W/S_w} \right)^{0.5} - C_6}$$

$$C_5 \cdot C_1 \cdot \left( \frac{1}{W/P_{avail}} \right) \cdot \left( \frac{1}{W/S_w} \right)^{0.5} - C_5 \cdot C_6 = (W/S_w)$$

$$C_5 \cdot C_1 \cdot \left( \frac{1}{W/P_{avail}} \right) \cdot \left( \frac{1}{W/S_w} \right)^{0.5} = (W/S_w) + C_5 \cdot C_6$$

$$\frac{W}{P_{avail}} = \frac{C_1 \cdot C_5 \cdot \left( \frac{1}{W/S_w} \right)^{0.5}}{(W/S_w) + C_5 \cdot C_6}$$

$$\frac{W}{P_{eng}} = R_p \cdot \frac{C_1 \cdot C_5 \cdot \left( \frac{1}{W/S_w} \right)^{0.5}}{(W/S_w) + C_5 \cdot C_6}$$

## 7.5 Climb performances (propeller driven aircraft)

The relationship between wing loading and power loading for a propeller driven aircraft in climb is given by

$$\frac{W}{P_{\text{eng}}} = R_p \cdot \frac{\eta_p}{0.5 \cdot (2 \cdot g)^{3/2} \cdot (\rho)^{-1/2} \cdot \left(\frac{W}{S_w}\right)^{1/2} \left(\frac{C_D}{C_L^{3/2}}\right) + g \cdot RC}$$

Development of the relationship between wing loading and power loading in climb

$$\begin{aligned} P_{\text{avail}} \cdot \eta_p &= P_{\text{req}} + W \cdot g \cdot RC \\ P_{\text{req}} &= 0.5 \cdot \rho \cdot V^3 \cdot S_w \cdot C_D \\ P_{\text{req}} &= 0.5 \cdot \rho \cdot \left(\frac{2 \cdot g \cdot W}{\rho \cdot C_L} \cdot \frac{W}{S_w}\right)^{3/2} \cdot S_w \cdot C_D \\ P_{\text{req}} &= 0.5 \cdot \rho \cdot S_w \cdot \frac{C_D}{C_L^{3/2}} \cdot \left(\frac{2 \cdot g \cdot W}{\rho} \cdot \frac{W}{S_w}\right)^{3/2} \\ P_{\text{avail}} \cdot \eta_p &= 0.5 \cdot \rho \cdot S_w \cdot \frac{C_D}{C_L^{3/2}} \cdot \left(\frac{2 \cdot g \cdot W}{\rho} \cdot \frac{W}{S_w}\right)^{3/2} + W \cdot g \cdot RC \\ \frac{P_{\text{avail}}}{W} &= \frac{1}{\eta_p} \cdot 0.5 \cdot (2 \cdot g)^{3/2} \cdot \left(\frac{1}{\rho}\right)^{1/2} \cdot \left(\frac{W}{S}\right)^{1/2} \cdot \frac{C_D}{C_L^{3/2}} + g \cdot RC \\ \frac{W}{P_{\text{eng}}} &= R_p \cdot \frac{\eta_p}{0.5 \cdot (2 \cdot g)^{3/2} \cdot (\rho)^{-1/2} \cdot \left(\frac{W}{S_w}\right)^{1/2} \left(\frac{C_D}{C_L^{3/2}}\right) + g \cdot RC} \end{aligned}$$

## Annex 8. Optimisation process (example)

### 8.1 Requirements (input data)

#### General

|   |                       |
|---|-----------------------|
| Aspect ratio  | 8.5                   |
| Oswald factor ( $e$ )                                       | 0.80                  |
| $g$   | 9.81 m/s <sup>2</sup> |
| Propeller efficiency ( $\eta_p$ )                           | 0.84                  |
| Engine specific fuel consumption (csf)                      | 0.274 kg/kW.h         |
| Payload ( $W_{\text{payload}}$ )                            | 200 kg                |
| Useful weight ratio ( $W_{\text{useful}}/W_{\text{MxTO}}$ ) | 0.475                 |

#### [1] Cruise

|   |                         |
|---|-------------------------|
| Flight speed ( $V_{\text{cr}}$ )        | 300 km/h                |
| Zero lift drag coefficient ( $C_{D0}$ ) | 0.0207                  |
| Air density ( $\rho_0$ )                | 0.996 kg/m <sup>3</sup> |
| Power ratio ( $R_p$ )                   | 0.78                    |
| Range                                   | 800 km                  |

#### [2] Stall speed - [3] Landing

|           |         |
|-----------|---------|
| $V_s$     | 80 km/h |
| $C_{LMx}$ | 2.80    |

#### [4] Takeoff

|   |                         |
|---|-------------------------|
| Takeoff run ( $d$ )                               | 150 m                   |
| Lift coefficient ( $C_{LTO}$ )                    | 1.52                    |
| Rolling friction coefficient ( $C_{\text{fgr}}$ ) | 0.02                    |
| Runway angle ( $\gamma$ )                         | 0°                      |
| Air density ( $\rho_0$ )                          | 1.225 kg/m <sup>3</sup> |
| Power ratio ( $R_p$ )                             | 1                       |

#### [5] Climb

|   |                         |
|---|-------------------------|
| Rate of climb (RC)                      | 8.05 m/s                |
| Propeller efficiency ( $\eta_p$ )       | 0.78                    |
| Zero lift drag coefficient ( $C_{D0}$ ) | 0.0219                  |
| Air density ( $\rho_0$ )                | 1.225 kg/m <sup>3</sup> |
| Power ratio ( $R_p$ )                   | 1                       |



## 8.2 Equations

|             |  |
|-------------|--|
| [1] Cruise  | $\frac{W}{P_{\text{eng}}} = R_p \cdot \frac{c_2 \cdot W/S_w}{c_3 + c_1 \cdot (W/S_w)^2}$   |
| [2] Stall   | $\frac{W}{S_w} = \frac{\rho}{2 \cdot g} \cdot V_s^2 \cdot C_{L_2}$   |
| [3] Takeoff | $\frac{W}{P_{\text{eng}}} = R_p \cdot \frac{C_1 \cdot C_5 \cdot \left(\frac{1}{W/S_w}\right)^{0.5}}{(W/S_w) + C_5 \cdot C_6}$  |
| [4] Climb   | $\frac{W}{P_{\text{eng}}} = R_p \cdot \frac{\eta_p}{0.5 \cdot (2 \cdot g)^{3/2} \cdot (\rho)^{-1/2} \cdot \left(\frac{W}{S_w}\right)^{1/2} \left(\frac{C_D}{C_L^{3/2}}\right) + g \cdot RC}$ |

## 8.3 Table

|     | [1]   | [2]   | [3]   | [4]   |
|-----|-------|-------|-------|-------|
| W/S | W/BHP | W/BHP | W/BHP | W/BHP |
| 40  | 4.3   |       | 23.6  | 7.6   |
| 50  | 5.3   |       | 17.5  | 7.4   |
| 60  | 6.2   |       | 13.7  | 7.3   |
| 70  | 7.1   |       | 11.1  | 7.1   |
| 80  | 7.9   |       | 9.2   | 7.0   |
| 90  | 8.6   |       | 7.8   | 6.9   |
| 100 | 9.3   |       | 6.7   | 6.8   |
| 110 | 9.9   |       | 5.9   | 6.6   |
| 120 | 10.4  |       | 5.2   | 6.6   |
| 130 | 10.9  |       | 4.6   | 6.5   |
| 140 | 11.3  |       | 4.2   | 6.4   |

From the selected wing loading ( $W/S$ ) and power loading ( $W/P$ ), the following values may be computed:

Fuel weight

$$W_{\text{fuel}}/W_0 = 1 - \frac{1}{e^{R/B}}$$

With

$$B = \frac{1000 \cdot 3600}{9.81} \cdot \frac{\eta_p}{S_{fc}} \cdot GR$$

From the Breguet range equation

$$\left| \begin{aligned} R &= \frac{1000 \cdot 3600}{9.81} \cdot \frac{\eta_p}{S_{fc}} \cdot GR \cdot \ln\left(\frac{W_0}{W_1}\right) \\ R &= \frac{1000 \cdot 3600}{9.81} \cdot \frac{\eta_p}{S_{fc}} \cdot GR \cdot \ln\left(\frac{W_0}{W_0 - W_{\text{fuel}}}\right) \\ R &= \frac{1000 \cdot 3600}{9.81} \cdot \frac{\eta_p}{S_{fc}} \cdot GR \cdot \ln\left(\frac{1}{1 - W_{\text{fuel}}/W_0}\right) \\ W_{\text{fuel}}/W_0 &= 1 - \frac{1}{e^{R/B}} \end{aligned} \right.$$

Maximum takeoff weight

$$W_{\text{TO}} = \frac{W_{\text{payload}}}{\frac{W_{\text{useful}}}{W_{\text{TO}}} - \frac{W_{\text{fuel}}}{W_{\text{TO}}}}$$

And

$$\frac{W_{\text{payload}}}{W_{\text{TO}}} = \frac{W_{\text{useful}} - W_{\text{fuel}}}{W_{\text{TO}}}$$

Empty weight

$$W_{\text{empty}} = W_{\text{TO}} - W_{\text{payload}} - W_{\text{fuel}}$$

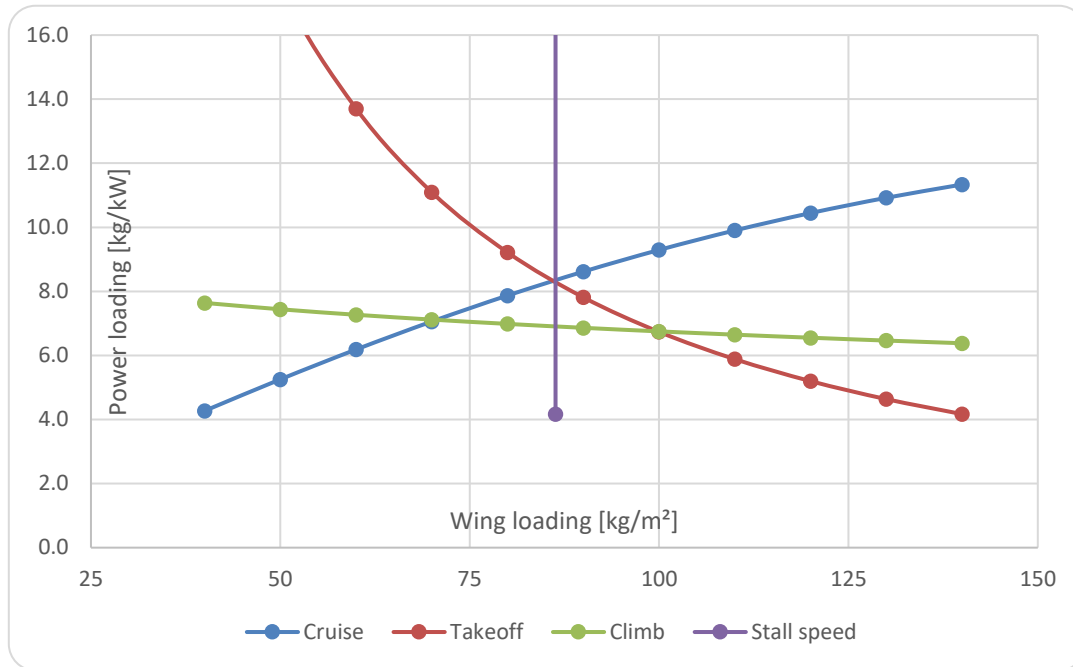
Wing area

$$S_w = \frac{W}{W/S_w}$$

Maximum engine power

$$P_{\text{eng}} = \frac{W}{W/P_{\text{eng}}}$$

### 8.4 Chart



The selection of a given match point defined by a given value of wing loading and the corresponding value of power loading will allow the designer to compute the wing area and maximum engine power of the aircraft that fulfills the requirements.

|        |                      |
|--------|----------------------|
| →W/S   | 86 kg/m <sup>2</sup> |
| →W/BHP | 7.6 kg/kW            |

|                      |          |
|----------------------|----------|
| <b>Cruise</b>        |          |
| C <sub>L</sub>       | 0.24     |
| C <sub>D0</sub>      | 0.02070  |
| C <sub>DL</sub>      | 0.00279  |
| GR                   | 10.39    |
| B                    | 11685796 |
| W <sub>fuel</sub> /W | 0.07     |
| W                    | 489 kg   |
| W <sub>fuel</sub>    | 32 kg    |
| W <sub>empty</sub>   | 257 kg   |

|                    |                     |
|--------------------|---------------------|
| S <sub>w</sub>     | 5.69 m <sup>2</sup> |
| BHP <sub>eng</sub> | 64.4 kW             |



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## Annex 9. Airworthiness requirements

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### 9.1 Introduction

**Airworthiness** is a term used to describe whether an aircraft has been certified as suitable for safe flight.

The **Federal Aviation Regulations**, or **FARs**, are rules prescribed by the Federal Aviation Administration (FAA) governing all aviation activities in the United States. The FARs are part of Title 14 of the Code of Federal Regulations (CFR). A wide variety of activities are regulated, such as airplane design, typical airline flights, pilot training activities, hot-air ballooning, lighter-than-air aircraft, man-made structure heights, obstruction lighting and marking, and even model rocket launches and model aircraft operation. The rules are designed to promote safe aviation, protecting pilots, passengers and the general public from unnecessary risk.

The FARs are organized into sections, called *parts* due to their organization within the CFR. Each part deals with a specific type of activity. For example, *14 CFR Part 141* contains rules for pilot training schools.

- Part 1 – Definitions and Abbreviations
- Part 13 – Investigation and Enforcement Procedures
- Part 21 – Certification Procedures for Products and Parts
- Part 23 – Airworthiness Standards: Normal, Utility, Acrobatic and Commuter Airplanes
- Part 25 – Airworthiness Standards: Transport Category Airplanes
- Part 27 – Airworthiness Standards: Normal Category Rotorcraft
- Part 29 – Airworthiness Standards: Transport Category Rotorcraft
- Part 33 – Airworthiness Standards: Aircraft Engines
- Part 34 – Fuel Venting and Exhaust Emission Requirements for Turbine Engine Powered Airplanes
- Part 35 – Airworthiness Standards: Propellers
- Part 39 – Airworthiness Directives
- Part 43 – Maintenance, Preventive Maintenance, Rebuilding, and Alteration
- Part 45 – Identification and Registration Marking
- Part 47 – Aircraft Registration
- Part 61 – Certification: Pilots, Flight Instructors, and Ground Instructors
- Part 65 – Certification: Airmen Other Than Flight Crewmembers
- Part 67 – Medical Standards and Certification
- Part 71 – Designation of Class A, Class B, Class C, Class D, and Class E Airspace Areas; Airways; Routes; and Reporting Points
- Part 73 – Special Use Airspace
- Part 91 – General Operating and Flight Rules
- Part 97 – Standard Instrument Approach Procedures
- Part 101 – Moored Balloons, Kites, Unmanned Rockets and Unmanned Free Balloons
- Part 103 – Ultralight Vehicles
- Part 105 – Parachute Operations
- Part 119 – Certification: Air Carriers and Commercial Operators
- Part 121 – Operating Requirements: Domestic, Flag, and Supplemental Operations
- Part 125 – Certification and Operations: Airplanes Having a Seating Capacity of 20 or More Passengers or a Payload Capacity of 6,000 Pounds or More
- Part 133 – Rotorcraft External-Load Operations
- Part 135 – Operating Requirements: Commuter and On Demand Operations and Rules Governing Persons on Board Such Aircraft
- Part 136 – Commercial Air Tours and National Parks Air Tour Management
- Part 137 – Agricultural Aircraft Operations
- Part 139 – Certification of Airports
- Part 141 – Flight Schools
- Part 142 – Training Centres
- Part 145 – Repair Stations



- Part 147 – Aviation Maintenance Technicians Schools
- Part 183 – Representatives of The Administrator

**Part 23** contains airworthiness standards for airplanes in the normal, utility, aerobatic, and commuter categories. It dictates the standards required for issuance and change of type certificates for airplanes in these categories.

This Part has a large number of regulations to ensure airworthiness in areas such as structural loads, airframe, performance, stability, controllability, and safety mechanisms, how the seats must be constructed, oxygen and air pressurization systems, fire prevention, escape hatches, flight management procedures, flight control communications, emergency landing procedures, and other limitations, as well as testing of all the systems of the aircraft. It also determines special aspects of aircraft performance such as stall speed (for single engine airplanes - not more than 61 knots), rate of climb (not less than 300 ft/min), take off speed (not less than  $1.2 \times V_{s1}$ ), weight of each pilot and passenger (170 lb for airplanes in the normal and commuter categories, and 190 lb for airplanes in the acrobatic and utility categories). The Cessna 177, Cirrus SR20 and Piper PA-34 Seneca are well-known airplane types that were certificated to FAR Part 23.

Most of the Federal Aviation Regulations, including Part 23, commenced on February 1, 1965. Prior to that date, airworthiness standards for airplanes in the normal, utility and acrobatic categories were promulgated in Part 3 of the US Civil Air Regulations. Many well-known types of light airplane are type certificated to CAR Part 3, even though they remained in production after 1965. For example, the Cessna 150 and Piper Cherokee are type certificated to CAR Part 3.

**Part 25** contains airworthiness standards for airplanes in the transport category. Transport category airplanes are either:

- Jets with 10 or more seats or a maximum takeoff weight (MTOW) greater than 12,500 pounds (5,670 kg); or
- Propeller-driven airplanes with greater than 19 seats or a MTOW greater than 19,000 pounds (8,618 kg).

The Boeing 737 and later types, and Airbus A300 series, are well-known airplane types that were certificated to FAR Part 25.

Most of the Federal Aviation Regulations, including Part 25, commenced on February 1, 1965. Prior to that date, airworthiness standards for airplanes in the transport category were promulgated in Part 4b of the US Civil Air Regulations. The Boeing 707 and 727 are two well-known airplane types that were certificated to CAR Part 4b.

## 9.2 Miscellaneous

|  | FAR 23<br>CS 23  |  |  |  | FAR 25<br>CS 25   |
|--|--|--|--|--|---|
|  | N <sup>a</sup>   | U <sup>a</sup>   | A <sup>a</sup>   | C <sup>a</sup>   |   |
| Maximum takeoff weight <sup>b</sup>      | $\leq 12500 \text{ lb}$<br>$\geq 170.s + \Delta_1$<br>$\geq MC + \Delta_2$ | $\leq 12500 \text{ lb}$<br>$\geq 190.s + \Delta_1$<br>$\geq MC + \Delta_2$ | $\leq 12500 \text{ lb}$<br>$\geq 190.s + \Delta_1$<br>$\geq MC + \Delta_2$ | $\leq 19000 \text{ lb}$<br>$\geq 170.s + \Delta_1$<br>$\geq MC + \Delta_2$ | Not restricted  |
| Minimum weight <sup>b</sup>              | EW + MC + WFC  |  |  |  | Not restricted  |
| Number of engines                        | $\geq 1$   | $\geq 1$   | $\geq 1$   | $\geq 2_{(FAR 23)}$<br>$2_{(CS 23)}$                                       | $\geq 2$  |
| Maximum number of Occupants <sup>a</sup> | $\leq 9+\text{pilot(s)}$   | $\leq 9+\text{pilot(s)}$   | $\leq 9+\text{pilot(s)}$   | $\leq 19+\text{pilot(s)}$  | Not restricted  |
| Type of engine                           | All  | All  | All  | Propeller-driven   | All <sub>(FAR 25)</sub><br>TP <sub>(CS 25)</sub> <sup>c</sup> |
| Maximum operating altitude, ft           | 35000 ft   | 35000 ft   | 35000 ft   | 35000 ft   | Not restricted  |

<sup>a</sup> Cf. FAR 23.3 : Airplane categories for the definition of each category - CS 23.1 : Applicability

<sup>b</sup> Cf. FAR 23.25 - CS 23.25 : Weight limits

<sup>c</sup> Turbine-powered, including Turbopropeller

N : Normal

U : Utility

A : Acrobatic

C : Commuter

s : Number of seats

$\Delta_1$  : Oil at full capacity + Weight of fuel for 30' of operation at maximum continuous power (if VFR<sub>day</sub>)

$\Delta_1$  : Oil at full capacity + Weight of fuel for 45' of operation at maximum continuous power (if VFR<sub>night</sub> or IFR)

$\Delta_2$  : Oil at full capacity + Fuel at full capacity

EW : Empty weight

MC : required minimum crew (assume 170 lb for each crew member)

WFC : minimum fuel weight

|                             |   |
|-----------------------------|---|
| Turbojet powered air-planes | WFC : weight of 5% of the total fuel capacity |
|-----------------------------|---|

|                 |   |
|-----------------|---|
| Other airplanes | WFC : weight of the fuel necessary for 30' of operation at maximum continuous power |
|-----------------|---|

### 9.3 Structure – Manoeuvring load factors

|                                   | $n_1^a$   | $n_2^a$  | $n_g^b$  | $n_{flap}^c$ |
|-----------------------------------|---|--|--|--------------|
| <b>FAR 23 - CS 23 - Normal</b>    | $\leq 3.8$  | $-0.4 \cdot n_1$                               | $1 \pm \frac{K_g \cdot \rho_0 \cdot U_{de} \cdot V \cdot a}{2 \cdot \frac{W}{S}}$  | 2            |
| <b>FAR 23 - CS 23 - Commuter</b>  | $2.1 + (10884 / (W + 4535))$                            |  |  |              |
| <b>FAR 23 - CS 23 - Utility</b>   | 4.4   | $-0.4 \cdot n_1$                               |  |              |
| <b>FAR 23 - CS 23 - Acrobatic</b> | 6   | $-0.5 \cdot n_1$                               |  |              |
| <b>FAR 25 - CS 25</b>             | $2.5 \leq n_1 \leq 3.8$<br>$2.1 + (10884 / (W + 4535))$ | $-1 \rightarrow V_C$<br>$-1 \leq n_2 \leq 0^d$ | $1 \pm \frac{K_g \cdot \rho_0 \cdot U_{ref} \cdot V \cdot a}{2 \cdot \frac{W}{S}}$ | 2            |

<sup>a</sup> Cf. FAR 23.337 - CS23.337 - FAR 25.337 - CS 25.337 : Limit manoeuvring load factors

<sup>b</sup> Cf. FAR 23.341 - CS23.341 - FAR 25.341 - CS 25.341 : Gust load factors

<sup>c</sup> Cf. FAR 23.345 - CS23.345 - FAR 25.345 - CS 25.345 : High lift devices

<sup>d</sup> Varies linearly from the value at  $V_C$  to zero at  $V_D$

$n_1$  : positive maneuvering load factor

$n_2$  : negative maneuvering load factor

$n_g$  : gust load factor

$W$  : design maximum takeoff weight (kg)

$K_g$  : gust alleviation factor

$\mu_g$  : airplane mass ratio

$S$  : aerodynamic reference wing area ( $m^2$ )

$\rho_0$  : air density at sea level ( $kg/m^3$ )

$\rho$  : air density at the altitude considered ( $kg/m^3$ )

$c$  : mean geometric chord (m)

$g$  : acceleration due to gravity ( $m/s^2$ )

$V$  : aircraft equivalent speed (m/s)

$a$  : slope of the airplane normal force curve (/rad)

$U_{de}$  : derived gust velocity (m/s)

$U_{ref}$  : The reference gust velocity in equivalent airspeed (m/s)

$W/S$  : wing loading ( $N/m^2$ )

|                                       |  |
|---------------------------------------|--|
| $K_g = \frac{0.88\mu_g}{5.3 + \mu_g}$ | $\mu_g = \frac{2\left(\frac{W}{S}\right)}{\rho \cdot c \cdot a \cdot g}$   |
| $U_{de} @ V_C$                        | 15.24 m/s (SL $\rightarrow$ 6096 m)  |
| $U_{de} @ V_D$                        | 0.5 $U_{de} @ V_C$   |
| $U_{ref} @ V_C$                       | 17.07 m/s (SL)   |
|                                       | 17.07 m/s $\rightarrow$ 13.41 m/s (SL $\rightarrow$ 4572 m)                |
|                                       | 13.41 m/s $\rightarrow$ 7.92 m/s (4572 m $\rightarrow$ 15240 m) for FAR 25 |
|                                       | 13.41 m/s $\rightarrow$ 6.36 m/s (4572 m $\rightarrow$ 18288 m) for CS 25  |
| $U_{ref} @ V_D$                       | 0.5 $U_{ref} @ V_C$  |



### 9.4 Performances- Stall speed

|                              | FAR 23<br>CS 23  |                |                |                | FAR 25<br>CS 25                       |
|------------------------------|--|----------------|----------------|----------------|---------------------------------------|
|                              | N <sup>a</sup>   | U <sup>a</sup> | A <sup>a</sup> | C <sup>a</sup> |                                       |
| V <sub>S</sub> <sup>b</sup>  | ≤ 61 kts if n ≤ 1<br>≤ 61 kts if ( n > 1 and W < 6000 lb and RC OEI < RC <sub>Min</sub> OEI ) <sup>c</sup> |                |                |                |                                       |
| V <sub>SR</sub> <sup>b</sup> |  |                |                |                | $\geq \frac{V_{CLMx}}{\sqrt{n_{zw}}}$ |

<sup>a</sup> Cf. FAR 23.3 Airplane categories for the definition of each category

<sup>b</sup> Cf. FAR 23.49 - CS 23.49 : Stalling speed - FAR 25.103 - CS 25.103 : Stall speed

<sup>c</sup> Cf. FAR 23.67 - CS 23.67 : Climb: One engine inoperative

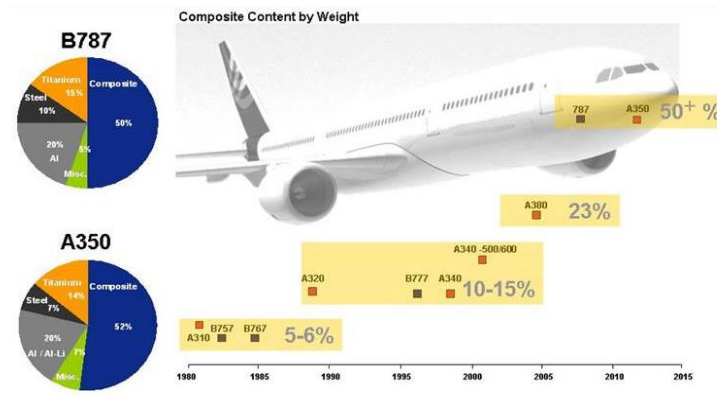
n : Number of engines

n<sub>zw</sub> : Load factor normal to the flight path at V<sub>CLMx</sub>

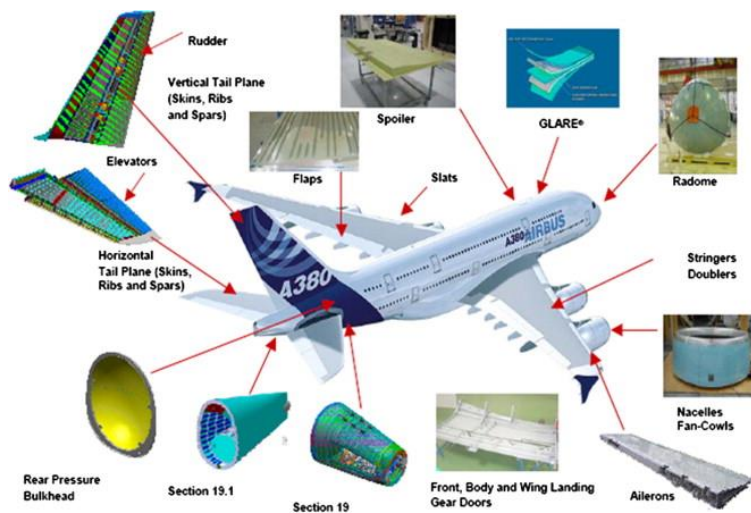


## Annex 10. Materials in aviation

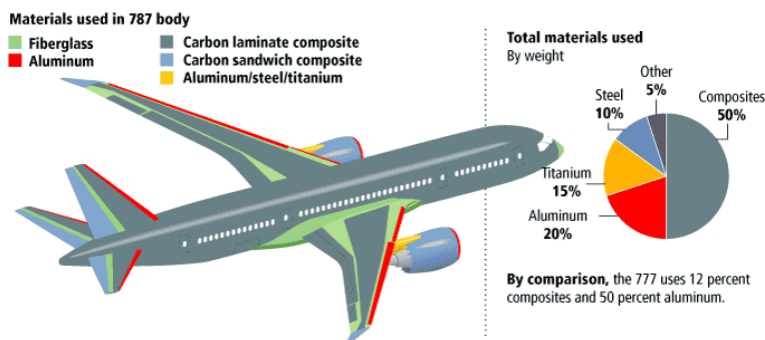
### 10.1 Percentage of composite



### 10.2 Current aircraft



#### 10.2.1 Next generation aircraft



## Annex 11. The power-plant

### 11.1 Introduction

The engine is one component of the propulsion system of the aircraft that is used to generate the thrust.

In aviation, most of the engine are internal combustion engine. They could be classified in 2 categories: shaft engines which drive a propeller, and reaction engines which generate thrust. Electric motors are used on very small aircraft (radio controlled aircraft or unmanned aerial vehicles)

The selection of engine type is function of different parameters: the maximum power required, the flight speed and the flight altitude.

A single engine aircraft has the engine in the fuselage in a tractor or pusher configuration. A multi engine aircraft, most of the time, has the engines on both sides of the fuselage, on or below the wing.

Sometimes a twin engine propeller driven aircraft may have the engines located in the fuselage in a push-pull configuration, one engine in the front and one engine in the rear of the fuselage.

### 11.2 Summary

|             |  |
|-------------|--|
| Definition  | Mechanical device used to generate power   |
| Category    | <p>Internal combustion engine</p> <ul style="list-style-type: none"> <li>- Shaft engine <ul style="list-style-type: none"> <li>o Piston</li> <li>o Turboprop</li> <li>o Turboshaft</li> </ul> </li> <li>- Reaction engine <ul style="list-style-type: none"> <li>o Turbojet</li> <li>o Turbofan</li> </ul> </li> </ul> <p>Electric</p> |
| Application | <p>Piston : Light aviation, UAV</p> <p>Turboprop : low speed and high power aircraft (transport aircraft)</p> <p>Turboshaft : Helicopter</p> <p>Turbojet : High speed (military aircraft)</p> <p>Turbofan : Long range, high speed aircraft</p> <p>Electric : UAV</p>  |
| Position    | <p>Single engine : on the fuselage, in a tractor or pusher configuration</p> <p>Multi engine:</p> <ul style="list-style-type: none"> <li>- Under the wing for transport aircraft,</li> <li>- In the fuselage for military fighters</li> </ul>  |

### 11.3 Thrust

The equation of the thrust provided by the propulsion system is:

$$T = m \cdot a = \dot{m} \cdot (V - V_0)$$

With:

|           |  |
|-----------|--|
| T         | Thrust [N]                             |
| $\dot{m}$ | Mass flow rate [kg/s]                  |
| a         | Fluid acceleration [m/s <sup>2</sup> ] |
| $V_0$     | Free stream fluid velocity [m/s]       |
| V         | Exhaust fluid velocity [m/s]           |

The thrust will be maximized if

1. The mass flow rate is maximized (↗)
2. The fluid acceleration is maximized (↗), high fluid velocity.

### 11.4 Propulsion efficiency

The propulsion efficiency is defined as the ratio between the thrust (or power) obtained to the thrust (or power) expended

$$\eta_p = \frac{P}{P_{\text{expended}}} = \frac{2}{V/V_0 + 1}$$

With:

|       |                                  |
|-------|----------------------------------|
| $V_0$ | Free stream fluid velocity [m/s] |
| V     | Exhaust fluid velocity [m/s]     |

There is an unavoidable tradeoff between thrust and efficiency. For maximum thrust, the ratio between exhaust and free stream velocity must be very high. But for maximum efficiency, this ratio must be close to unity...

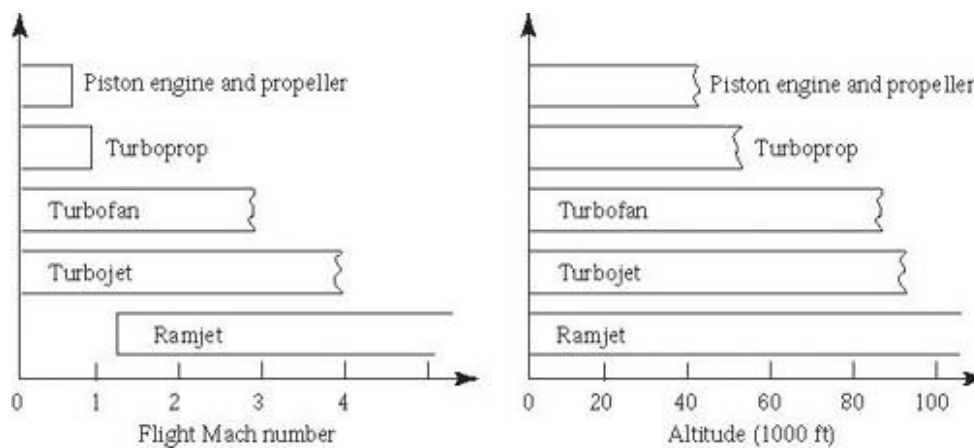
## 11.5 Engine technology

### 11.5.1 Introduction

There exist different types (technology) of propulsion systems:

- Electric engine & propeller
- Piston engine & propeller
- Turbopropulsor
- Turbofan
- Turbojet

According to the flight speed and flight altitude, one propulsion system will be preferably used from another.



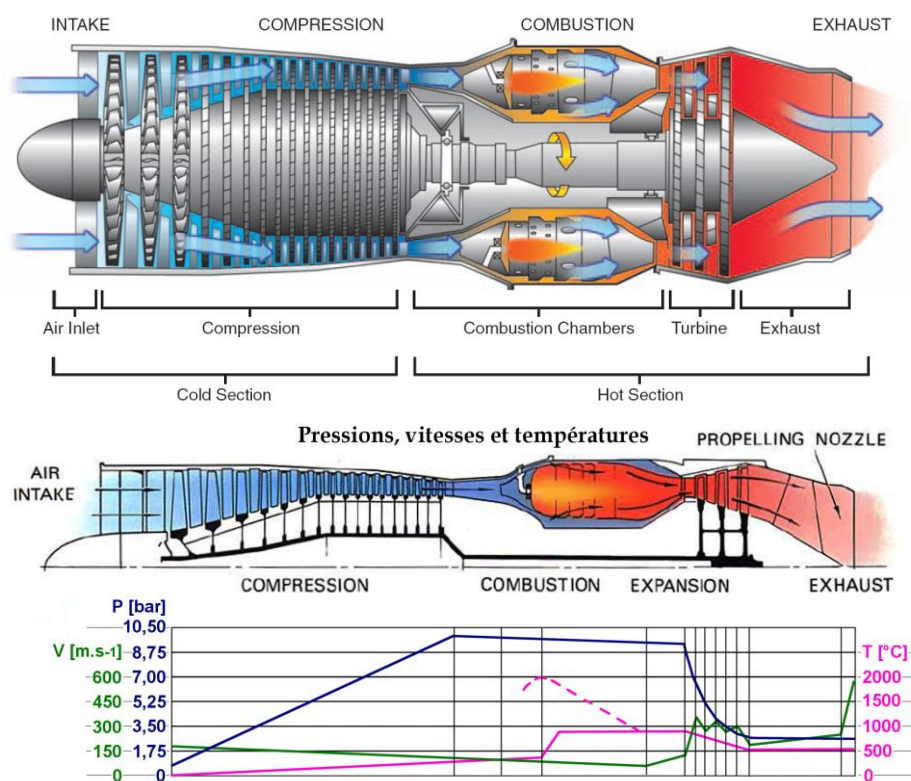
### 11.5.2 Turbojet

#### Advantages

- Low friction
- Little wear
- Long service life (20.000 – 30.000 h)
- Simplicity
- Low cost
- Low drag

#### Drawbacks

- High exhaust gas velocity (500 – 600 m/s) in order to reach a high thrust
- Low efficiency (30%) at subsonic flight speed



Turbojet engines are used on high speed (supersonic) aircraft.

### 11.5.3 Turbofan

In order to improve the propulsion efficiency, the exhaust fluid velocity is reduced. In order to increase the thrust, the mass flow is increased using a fan, which works like a compressor with a low compression ratio.

The bypass ratio is the ratio between the mass flow passing through the fan and the mass passing through the turbine (used for combustion).

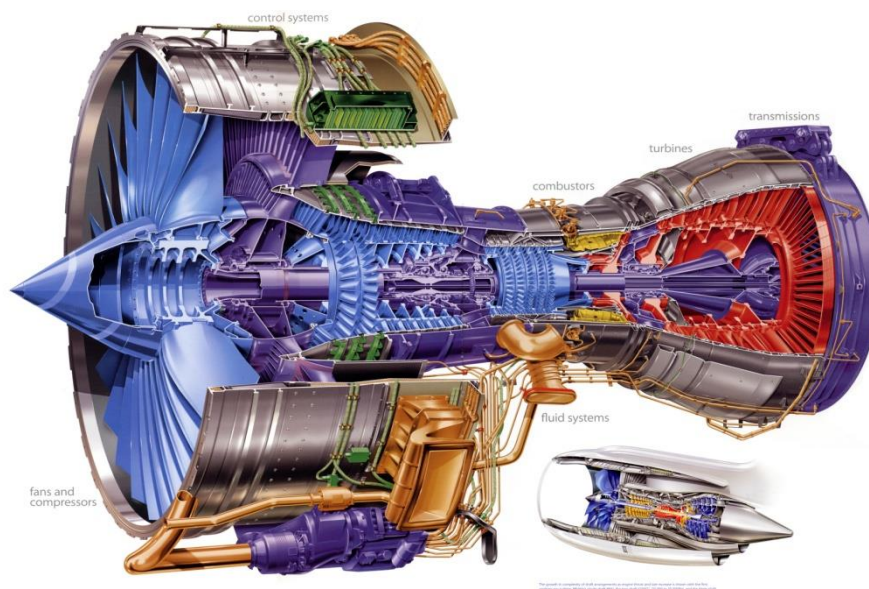
$$T = \dot{m} \cdot a = \dot{m}_{\text{jet}} \cdot (V_{\text{jet}} - V_0) + \dot{m}_{\text{fan}} \cdot (V_{\text{fan}} - V_0)$$

#### Advantages

- High global efficiency (50%)
- Low fuel consumption (0.03 kg/N.h @ TO, SL, ISA conditions)
- Low CO<sub>2</sub> emissions

#### Drawbacks

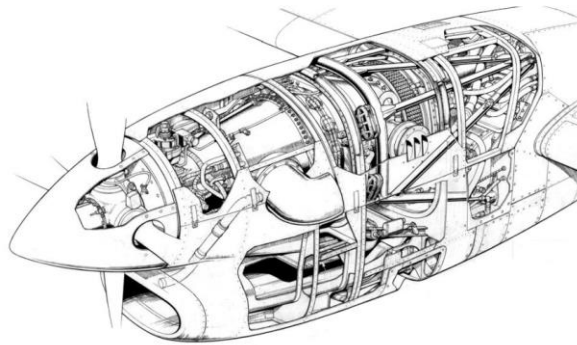
- Higher weight
- Higher drag



High bypass turbofan engines are used on subsonic transport aircraft.

### 11.5.4 Turbopropulsor

A turbopropulsor is a low-power turbofan with a very high bypass ratio. The fan is replaced by a propeller. In order to have a good propeller efficiency ( $> 80\%$ ), a gearbox is used between the turbine (@ 8.000 – 15.000 t/min) and the propeller (800 – 2000 t/min).

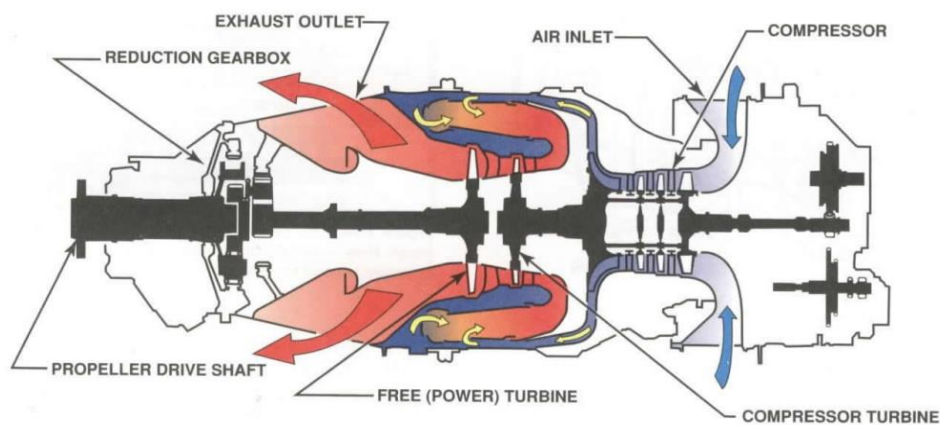


#### Advantages

- High power-to-weight ratio
- Very low fuel consumption
- STOL capability

#### Drawbacks

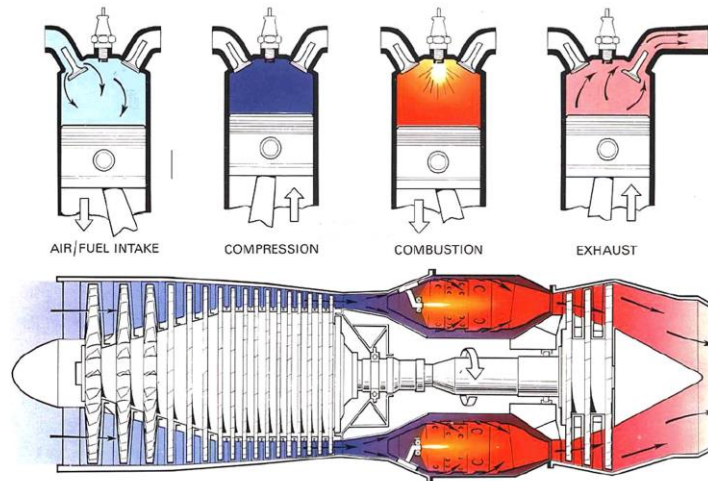
- Limited flight speed
- High noise level
- High weight due to the gearbox
- Lubrication
- Vibrations



Turbopropulsor engines are used on low speed transport aircraft.

### 11.5.5 Piston & propeller

Most commonly used propulsion system when the need of power is lower than 230 kW (300 hp).



A comparison between the working cycle of a turbo-jet engine and a piston engine.

#### Advantages

- Low cost

#### Drawbacks

- Heavy
- High level of vibrations due to the oscillating motion of the pistons
- High friction
- Low efficiency (30%)
- Short service life (2.000 – 3.000 h)

### 11.5.6 Electric & propeller

More and more used for low-powered systems like micro-UAS.



#### Advantages

- Low cost
- No limit in altitude (except for the propeller)
- No vibration
- No gearbox
- Light (if the engine is taken alone)
- High efficiency (95%)

#### Drawbacks

- Heavy (if the batteries are taken into account)
- Short endurance





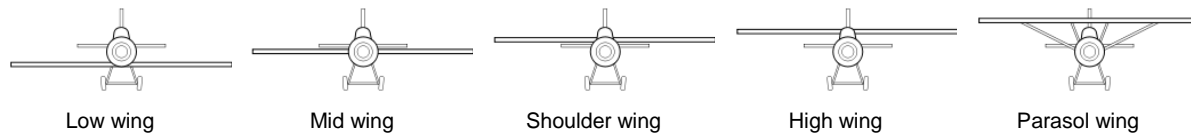
## **Annex 12. Lifting Surface Design Parameters**

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Some very important design criteria will be explained in such a way to understand their impact on the whole aircraft. The reader will understand that, most of the time, the designer will need to make compromises.

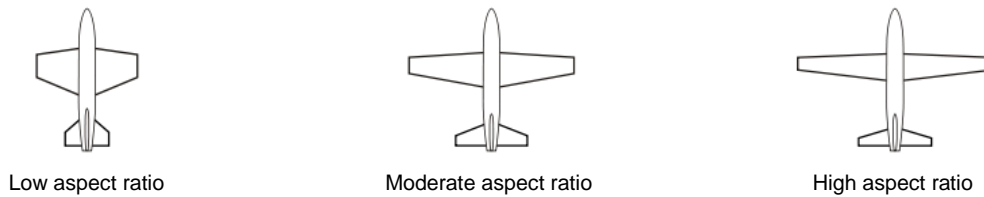
1. Wing vertical position on the fuselage
2. Lifting surface aspect ratio
3. Lifting surface sweep angle
4. Lifting surface taper ratio
5. Lifting surface dihedral effect
6. Lifting surface airfoil selection

### 12.1 Wing vertical position on the fuselage



|  | Low | High |
|--|-----|------|
| <b>Structure &amp; Aerodynamics</b>  |     |      |
| Favorable ground effect in takeoff & landing   | +   | -    |
| Moving surfaces closer to the ground are more easily damaged   | -   | +    |
| High wings tend to be strutted because they are often thinner so as to leave enough headroom. (more draggy than low-winged arrangements)   | +   | -    |
| Low wing structure is useful anchorage and stowage for landing gear  | +   | -    |
| Landing gear can be made shorter and lighter   | +   | -    |
| Deeper spar can be used (can be incorporated into seat structure)  | +   | -    |
| Increase the depth of the fuselage if deeper spar is needed  | +   | -    |
| Fairing between wing root and fuselage more critical aerodynamically (upper surface of the wing generates 66% of the total lift and some is lost by imperfect fillets, while imperfections beneath the root of a high wing increase static pressure and increase lift) | -   | +    |
| <b>→ Stability</b>   |     |      |
| High wing provides more <u>lateral stability</u> through dihedral effect   | -   | +    |
| <u>No dihedral needed</u> , easy to build (a high wing augments dihedral, while a low wing works against dihedral. So that low-winged airplanes need more dihedral than those with high wing)  | -   | +    |
| <b>→ Safety &amp; Visibility</b>   |     |      |
| Better fields of view from above the horizon, downwards (better touring aircraft)  | -   | +    |
| Better fields of view from above the horizon, upwards (agile aircraft)   | +   | -    |
| Visibility in the direction of turn  | +   | -    |
| Manoeuvrability, Agility (good fields of view in the direction of turn and manoeuvre)  | +   | -    |
| <u>Crashworthiness</u> , tough and resilient structure is needed to take the weight of the aircraft when on its back   | -   | +    |
| <u>Crashworthiness</u> , easily exit from the aircraft   | -   | +    |
| Note: the extend of cockpit glazing should be determined by the pilot needs. An agile airplane which regularly exceeds angles of bank of 60° needs wider fields of view than a stately transport machine, which rarely exceeds 30°                                     |     |      |
| <b>→ Aircraft category</b>   |     |      |
| Touring aircraft   | -   | +    |
| Agile aircraft   | +   | -    |

## 12.2 Lifting surface aspect ratio

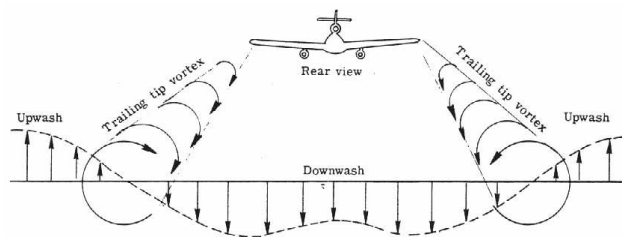


In selecting the lifting surface aspect ratio the designer must give considerations to several general requirements. These requirements are related to:

1. Aerodynamics
2. Structural weight
3. Safety

### Introduction

When a wing is generating lift, it has a reduced pressure on the upper surface and an increased pressure on the lower surface. This pressure difference tends to move the air from the bottom of the wing, moving to the top. This is not possible for a 2D-flow (airfoil profile) but for a real 3D-flow (3D-wing) the air can escape around the wing tip. Air escaping around the wing tip lowers the pressure difference between the upper and lower surfaces. This reduces lift near the wing tip and generates vortices. A wing with a high aspect ratio has smaller tips, less sensitive, than a wing of equal area with a low aspect ratio.



#### → Aerodynamics

AR as high as possible (↗) to reduce the induced drag.

Flight conditions concerned: climb, maxi range and maxi endurance

$$C_D = C_{D_0} + \frac{C_L^2}{\pi \cdot AR_w \cdot e}$$

#### → Structural weight

AR as low as possible (↘) to reduce the structural weight of the lifting surface

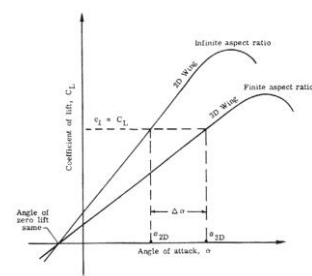
$$W_w = \text{fct}(AR_w^{0.6})$$

| $\Delta(AR)$ | $\Delta W_w$ |
|--------------|--------------|
| -20%         | -12.5%       |
| -10%         | -6.1%        |
| 10%          | 5.9%         |
| 20%          | 11.6%        |

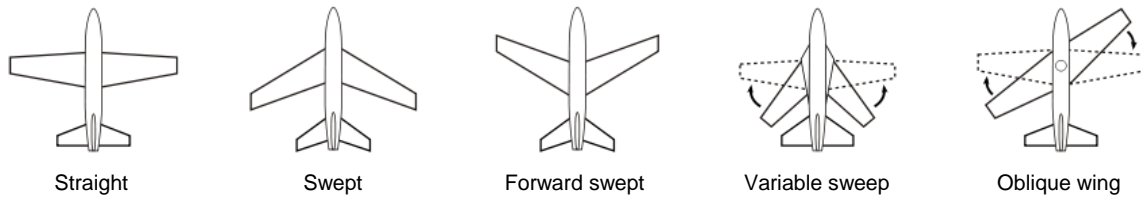
#### → Safety

AR changes modify the stalling angle. Surface with low aspect ratio will stall at a higher angle of attack than surface with high aspect ratio

A canard surface (↗) can be made to stall before the main wing by making it a very high aspect ratio surface. Horizontal tails (↘) tend to be of lower aspect ratio.



### 12.3 Lifting surface sweep angle

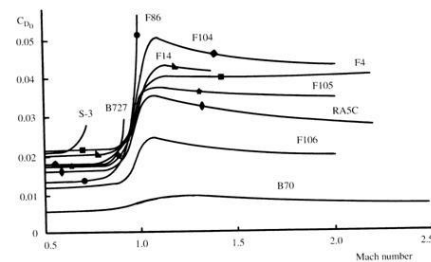


In selecting the lifting surface sweep angle the designer must give considerations to several general requirements. These requirements are related to:

1. Aerodynamics
2. Structural weight
3. Balance & Stability

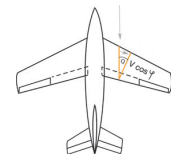
#### Introduction

Wing sweep is used preliminary to reduce the adverse effects of transonic and supersonic flow. The speed of the air passing on the upper surface of wing is increased. The critical Mach number is the speed at which the local flow on the upper surface reaches the speed of sound. If the speed continues to increase, a shock wave will appear and the drag will drastically increase.



#### → High speed aerodynamics

Sweep angle (↗) is favorable for high speed flight to delay the apparition of wave drag. Shock formation on a swept wing is determined by the air velocity in a direction perpendicular to the leading edge of the wing.



#### → Structural weight

Sweep angle as low as possible (↘) to reduce the structural weight of the lifting surface

$$W_w = fct(\cos(\Lambda)^{-0.9})$$

| $\Lambda$ | $\Delta W_w$ |
|-----------|--------------|
| 0°        | 0,0%         |
| 10°       | 1,4%         |
| 20°       | 5,8%         |
| 30°       | 13,8%        |

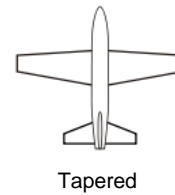
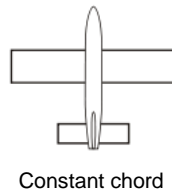
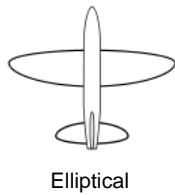
#### → Balance & Stability

Sweep Angle (↗, ↘) is necessary to balance the aircraft in order to move the Aerodynamic Center (AC) far enough from the CG position for balance.

Sweep angle (↗) improves stability. A swept wing has a natural dihedral effect (rolling moment caused by sideslip). Roughly speaking, 10° of sweep provides about 1° of effective dihedral.

If an aircraft has its vertical tails at the wing tips, sweeping the wing (↗) will push the tails aft, increasing their effectiveness.

## 12.4 Lifting surface taper ratio

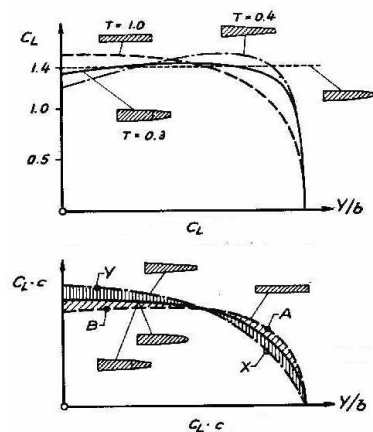


In selecting the lifting surface taper ratio the designer must give considerations to several general requirements. These requirements are related to:

1. Aerodynamics
2. Structural weight
3. Manufacturing

### Introduction

Taper ratio is the ratio between the tip chord and the root chord. Taper affects the distribution of the lift along the span of the lifting surface. Minimum drag due to lift or “induced” drag occurs when the lift is distributed in an elliptical fashion. For an untwist and unswept wing, this occurs when the wing planform is shaped as an ellipse. An elliptical planform is difficult and expensive to build. However, a wing with a taper ratio 0.4, which is simpler to build, produces lift distribution very close to the elliptical shape.



#### ➔ Aerodynamics

Taper ratio (↘) up to 0.4 will reduce the induced drag.

#### ➔ Structural weight

Taper ratio as low as possible (↘) to reduce the structural weight of the lifting surface

$$W_w = \text{fct}(TR^{0.04})$$

| $\Delta(TR)$ | $\Delta W_w$ |
|--------------|--------------|
| -10%         | -0.4%        |
| -20%         | -0.9%        |
| -30%         | -1.4%        |
| -40%         | -2.0%        |
| -50%         | -2.7%        |
| -60%         | -3.6%        |

#### ➔ Manufacturing

A wing with a taper ratio lower than 1 is more difficult and more expensive to build than a rectangular wing ( $TR = 1$ )

A wing with a given taper ratio is easier and less expensive to build than an elliptical wing.

## 12.5 Lifting surface dihedral angle



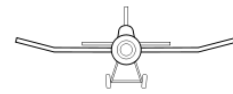
Dihedral



Anhedral



Inverted gull wing



Upward cranked tips

### Introduction

Dihedral effect tends to roll the aircraft level when side slipping.

Dihedral is the angle of the wing with the horizontal when seen from the front. Positive when the tip is higher than the root.

Three characteristics of the wing have an influence on the dihedral effect:

1. The wing dihedral angle itself
2. The vertical position of the wing on the fuselage
3. The wing sweep angle

#### → The wing dihedral angle

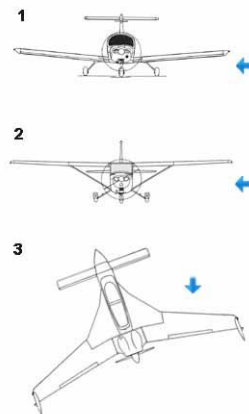
During a sideslip, the lateral wind coming from the sideslip direction increases the angle of attack and therefore the lift. The resulting moment is approximately proportional to the dihedral angle.

#### → The vertical position of the wing on the fuselage

The position of the wing on the fuselage has an influence on the dihedral effect, with the greatest effect provided by a high position. The fuselage in sideslip pushes the air over and under itself. If the wing is high-mounted, the air pushed over the top increases the angle of attack between the air and the wing and therefore increases the lift. The reverse is true for a low-mounted wing.

#### → The wing sweep angle

Wing sweep produces a rolling moment due to sideslip caused by the change in relative sweep of the left and right wings. Roughly speaking, 10° of sweep provides about 1° of effective dihedral.



### Notes

Due to additive effect of sweep and wing position, many high-winged transports such as the Lockheed C-5 require a negative geometric dihedral angle to avoid an excess of effective dihedral, which produces “Dutch Roll”, a repeated side-to-side motion involving roll and yaw. To counter a Dutch roll tendency, the vertical tail must be increased, which increases weight and drag.



### Historical values

|                       | Wing position |           |            |
|-----------------------|---------------|-----------|------------|
|                       | Low           | Mid       | High       |
| Unswept               | 5° to 7°      | 2° to 4°  | 0° to 2°   |
| Subsonic swept wing   | 3° to 7°      | -2° to 2° | -5° to -2° |
| Supersonic swept wing | 0° to 5°      | -5° to 0° | -5° to 0°  |

## Annex 13. Lifting surface airfoil profile

### 13.1 Introduction

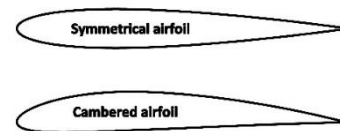
If a horizontal wing is cut by a vertical plane, parallel to the center line, the shape of the section is the airfoil section.

The airfoil is probably one of the most important characteristics of an airplane. It affects the cruise speed, the stall speed, the takeoff and landing distances, handling qualities and overall aerodynamic efficiency during all phases of flight.

There are two types of airfoils:

- Cambered airfoil
- Symmetrical airfoils

The cambered airfoil will be used on the wings to generate the upward lift. The symmetrical airfoils will be used on the stabilizers to generate lift in both directions (up and down for the horizontal stabilizer or left and right for the vertical stabilizer)

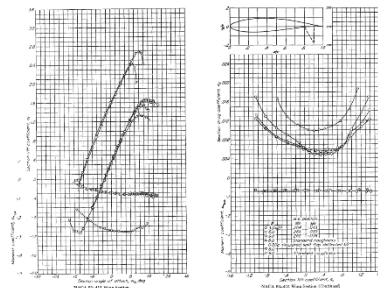


The shape of the airfoil will be function of the flight speed of the airplane. An airfoil designed to operate in supersonic flow will have a sharp leading edge to reduce supersonic drag, compared to a slow-speed airplane which will have a round nose.

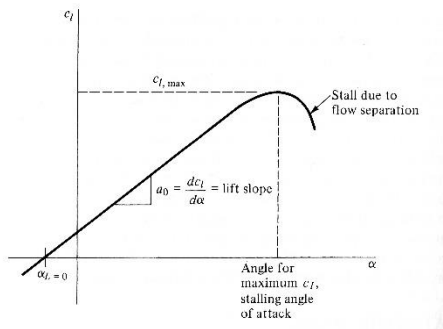
### 13.2 Aerodynamic performance

The aerodynamic performance of an airfoil are given in general in three graphs.

- One graph which shows the correlation between the lift coefficient and the angle of attack
- One graph which shows the correlation between the drag coefficient and the lift coefficient. This graph is also named the drag polar
- One graph which shows the correlation between the pitching moment coefficient and the lift coefficient



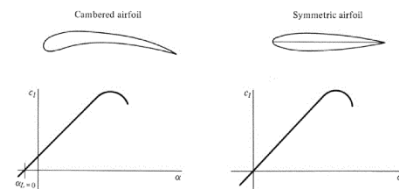
### 13.2.1 Lift Curve



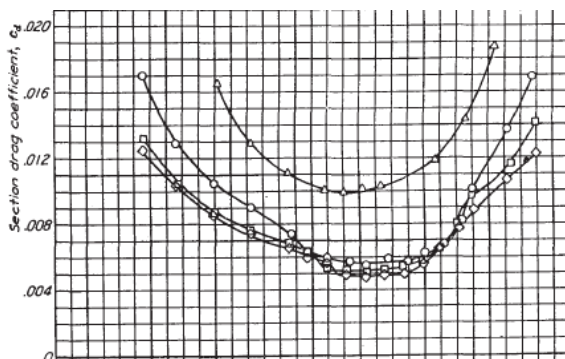
The lift curve is characterized by:

|                        |  |
|------------------------|--|
| $\alpha$               | is the angle of attack. This value is always small with a maximum value of about $15^\circ$              |
| $C_l$                  | is the lift coefficient  |
| $\alpha_0$             | is the zero-lift angle of attack   |
| $\alpha_{C_{l_{max}}}$ | is the angle of attack for maximum lift coefficient, also named stalling angle of attack                 |
| $C_{l_0}$              | is the lift coefficient which is reached at zero angle of attack   |
| $C_{l_{max}}$          | is the maximum lift coefficient. Typical values of this maximum lift coefficient lie between 0,8 and 1,6 |
| $a_0$                  | is the lift gradient. This value is close to $2\pi$  |

Looking at the curve of the lift coefficient, a symmetrical airfoil will generate no lift at zero angle of attack, while a cambered airfoil will generate no lift at a negative angle of attack.



### 13.2.2 Drag Curve

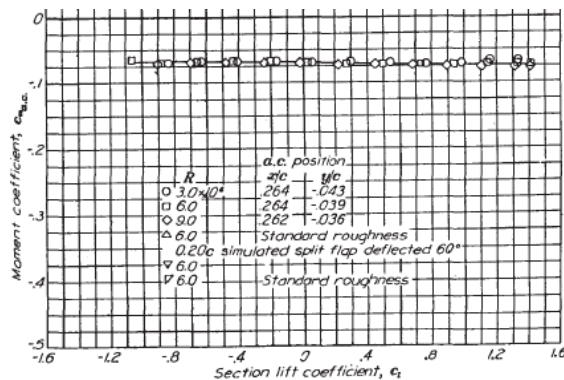


The drag curve is characterized by:

|                  |   |
|------------------|---|
| $C_{D_{Min}}$    | is the minimum drag coefficient                 |
| Laminar bulkhead | is the range of $C_l$ where the drag is minimum |



### 13.2.3 Moment Curve



The moment curve is characterized by:

$C_{m0}$  is the moment coefficient at zero lift coefficient

### 13.3 Geometric parameters that affect the performance of an airfoil

$C_{L_{Mx}}$  increases with increasing the relative thickness up to 15%, beyond  $C_{L_{Mx}}$  start decreasing.

The minimum drag coefficient increases with the relative thickness.

The nose radius strongly affects the angle of attack capability. A large radius of curvature will lead to a high lift coefficient and gentle stall break. A small leading edge radius has sharp stall break.

The maximum camber affects the value of  $\alpha_0$ ,  $C_{l0}$  and  $C_{m0}$

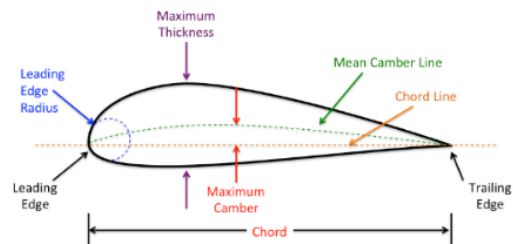
The maximum camber also affects the maximum lift coefficient and the minimum drag coefficient.

The slope of the camber line at the leading edge position affects the values of  $\alpha_0$  and  $C_{l0}$

The slope of the camber line at the trailing edge position affects the values  $C_{m0}$

The slope of the camber line affects the drag raise characteristics

The trailing edge angle affects the profile drag



**A high glide ratio is reached with a low maximum relative thickness and a low camber**

## Annex 14. Lifting surface airfoil selection

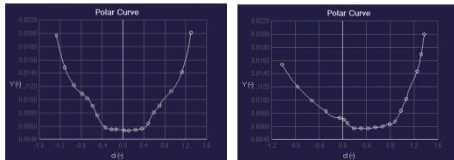
In selecting the airfoil sections the designer must give considerations to several general requirements. These requirements are related to:

1. Aerodynamics
2. Structural weight
3. Manufacturing
4. Safety

### → Aerodynamics

Maximum lift coefficient, as high as possible to minimize wing wetted area

Drag coefficient during the main flight condition (flight at a given lift coefficient and Reynolds Number) as low as possible to minimize required power



Drag coefficient during low speed flight (takeoff and climb) as low as possible to minimize required power

Pitching moment coefficient as low as possible to avoid high torsion loads and high trim drag

Critical Mach Number must be sufficiently high to ensure that critical compressibility effects are avoided in the case of aircraft flying at high speed (> Mach 0.7)

Sensitivity to contamination and dirt must be as low as possible

### → Structural weight

Relative thickness must be as high as possible in the interest of low structural weight

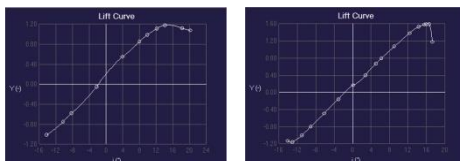
| $\Delta(t/c)$ | $\Delta W_w$ | $W_w = fct\left(\left(\frac{t}{c}\right)_w^{-0.3}\right)$ |
|---------------|--------------|---|
| -20%          | 6.9%         |   |
| -10%          | 3.2%         |   |
| 10%           | -2.8%        |   |
| 20%           | -5.3%        |   |

### → Manufacturing

Sensitivity to manufacturing variations must be as low as possible

### → Safety

Stall characteristics must be as gentle as possible to warn the pilot that a loss of lift will occur and to minimize the loss of altitude during the stall



**Unfortunately** all of these requirements cannot be satisfied at the same time and compromise must be done.

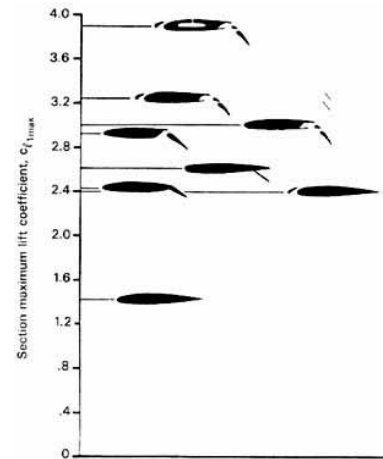
## Annex 15. The high lift devices

The main objective of the high lift device is to increase the maximum lift coefficient of a lifting surface. This is achieved most of the time by increasing the wing camber and sometimes the wing area at the same time.

There are two types of mechanical high lift devices:

- Trailing edge high lift device
- Leading edge high lift device

The choice will affect the maximum lift coefficient, and therefore the stall speeds and the takeoff and landing distances of the aircraft.



### 15.1 Trailing edge aerodynamic devices

- Plain flap
- Split flap
- Single slotted flap
- Double slotted flap
- Fowler flap

The approximate maximum lift contribution is:

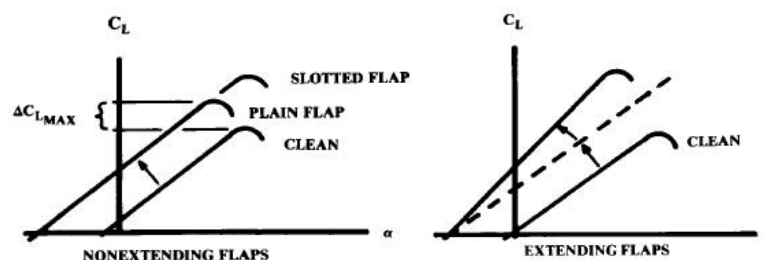
|                     |          |
|---------------------|----------|
| Plain flap          | 0.9      |
| Split flap          | 0.9      |
| Single slotted flap | 1.3      |
| Fowler flap         | 1.3 c'/c |
| Double slotted flap | 1.6 c'/c |

The plain flap is the hinged part of the trailing edge that moves downward in order to increase the camber of the airfoil.

The split flap is like the plain flap except that only the lower surface of the airfoil moves downward. The lift increment is the same as the plain flap but the drag increment is HIGHER and the change in pitching moment is LOWER.

The slotted flap is a plain flap with a gap between the wing and the flap. The hole allows high-pressure air from the lower surface of the wing to reach the upper surface of the wing in order to delay separation and stall.

The Fowler flap is a slotted flap which moves rearward when deflected. This provides 1) an increase of the camber of the airfoil, 2) an increase in wing area.



## 15.2 Leading edge aerodynamic devices

- Leading edge flap
- Kruger flap
- Leading edge slot
- Leading edge slat

The approximate maximum lift contribution is:

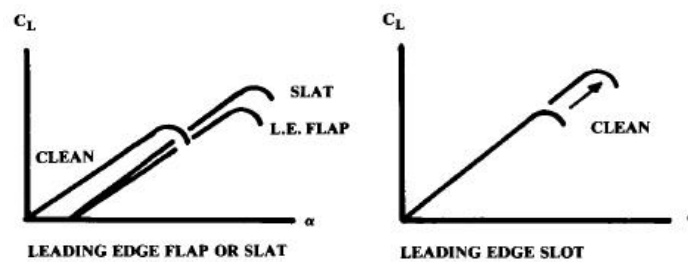
|                   |          |
|-------------------|----------|
| Leading edge slot | 0.2      |
| Leading edge flap | 0.3      |
| Kruger flap       | 0.3      |
| Leading edge slat | 0,4 c'/c |

The leading edge slot is a hole which allows high-pressure air from the lower surface of the wing to reach the upper surface of the wing in order to delay separation and stall.

The leading edge flap is the hinged part of the leading edge that moves down in order to increase the camber of the airfoil.

The leading edge slat provides 1) an increase of the camber of the airfoil, 2) a slot and 3) an increase in wing area

The Kruger flap works as a deflector, forcing the air to go over the top of the wing. Mostly used by large airliners



## 15.3 Effects of high lift devices

The non-extending flaps such as the plain, split or slotted flaps act as an increase in camber, which moves the angle of zero lift to the left and increases the maximum lift. The slope of the curve remains unchanged, and the angle of stall is somewhat reduced.

An extending flap such as the Fowler flap acts much like the other flaps as far as zero-lift angle and stall angle are concerned. However, the wing area is increased as the flap deflects, so the wing generates more lift at any given angle of attack compared to the non-extending flap.

Because the lift coefficient is referenced to the original wing area, not the extended wing area, the effective slope of the lift curve for an extending flap is increased by approximately the ratio of the total extended wing area to the original wing area.

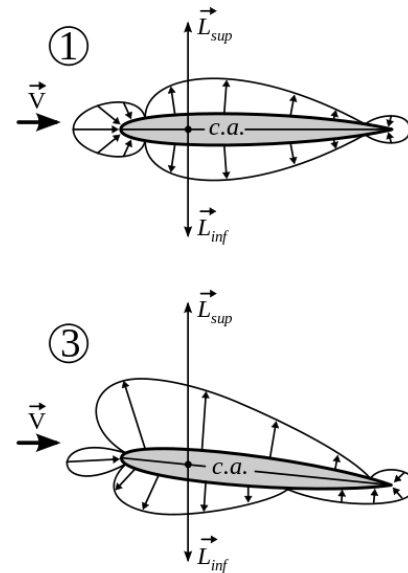
## Annex 16. The aerodynamic centre

### 16.1 Aerodynamic centre / Symmetric airfoil

For symmetric airfoils, the center of pressure does not vary with lift coefficient. The center of pressure coincide with the aerodynamic center.

In subsonic flight, for symmetric airfoils, the aerodynamic center is located at 25% of the chord, measured from the leading edge of the airfoil.

In supersonic flight, due to compressibility effects, the aerodynamic center moves to the 50% chord position.

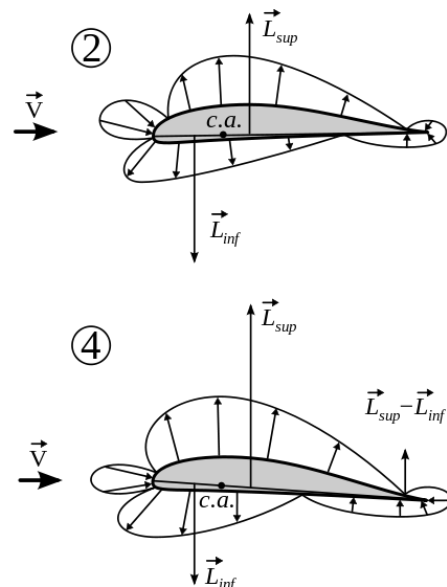


### 16.2 Aerodynamic centre / Cambered airfoil

For non-symmetric airfoils, or cambered airfoils, the center of pressure varies with lift coefficient. The center of pressure does not coincide with the aerodynamic center.

In subsonic flight and for incidences up to  $10^\circ$ , the aerodynamic center is located close to, not in general on, the chord line, between 23% and 25% of the chord, behind the leading edge. Compressibility tends to move it backwards. For thin airfoil in supersonic flow, the aerodynamic center is theoretically at 50% chord position.

For a conventional cambered airfoil, at high lift coefficient, close to the maximum lift coefficient, the center of pressure lies a little behind the quarter-chord point. When the lift coefficient reduces, the center of pressure moves to the rear. When the lift coefficient is equal to zero, a cambered airfoil generates a nose-down pitching moment. That means that the center of pressure is located at an infinite distance behind the airfoil

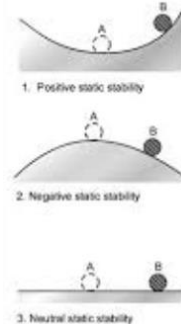


## Annex 17. Introduction to stability

### 17.1 Static stability

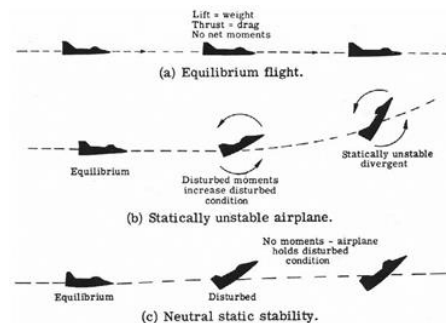
Static stability of a ball in a U-Shape describes the tendency of the ball to go back to its original position.

- Statistically stable, the ball will roll back to its original position
- Statistically unstable, the ball goes further and further its original position
- Statistically neutral, the ball remains in the disturbed position



Static stability of an aircraft describes the tendency to go back to its original position when subjected to disturbance acting on it.

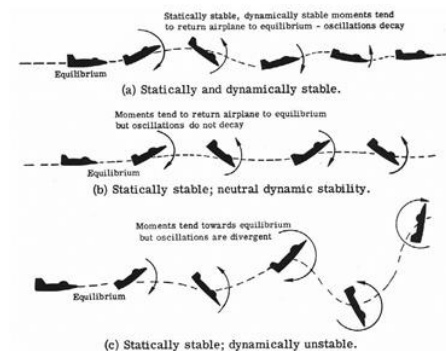
- Statically stable means that the aircraft is able to go back to its original position after disturbance.
- Statically unstable means that the aircraft continues to diverge from its original position
- Statically neutral means that the aircraft remains in its disturbed position



### 17.2 Dynamic stability

Dynamic stability describes the form of the motion of an aircraft when it tries to return to its original position.

- Dynamically stable means that the original position will be retrieved after a series of decaying oscillations
- Dynamically neutral means that the aircraft continues the oscillatory motion without decay in magnitude.
- Dynamically unstable means that the oscillatory motion increases in magnitude



### 17.3 Stability about the Axis

The stability of an airplane determines its ability to be trimmed to fly hands-off at any speed.

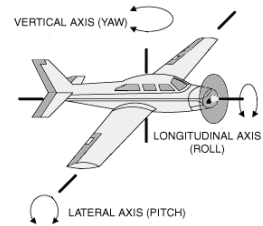
#### 17.3.1 Longitudinal stability

The longitudinal or pitch stability is stability about the lateral axis.

Longitudinal stability is provided primarily by the horizontal tail surface

Because the aerodynamic center is behind the center of gravity, an increment of lift will produce a nose down pitching moment. This nose down pitching moment will reduce the angle of attack, and at the same time the lift. The airplane goes back automatically in its original position.

The position of the center of gravity, in front of the aerodynamic center, is the condition for longitudinal stability. The greater this distance the more stable the aircraft. The lesser this distance the less stable the aircraft, but the more agile the aircraft



#### 17.3.2 Lateral stability

The lateral or roll stability is stability about the longitudinal axis.

Lateral stability is provided primarily by the dihedral of the wing

Dihedral is the angle between the wing and the lateral axis. Positive when the tip of the wing is at a higher position than the root of the wing. When an airplane enters in a downward sideslip toward the low wing, the direction of the relative wind changes. The low wing experience an increase of lift while the high wing experience a reduction of lift. This is due to a modification of the angle of attack. The combined forces tend to roll back the aircraft in its wings-level attitude

#### 17.3.3 Directional stability

The directional or yaw stability is stability about the vertical axis.

Directional stability is provided primarily by the vertical tail surface.

Most airplane are designed with more projected area behind the center of gravity than forward it.

When an airplane enters a sideslip, the relative wind strikes the side of the fuselage and the vertical tail. Since the force exerted on the airplane is behind the center of gravity, the airplane tends to yaw in the direction of the relative wind

## Annex 18. Weight estimation

### 18.1 Wing, $W_w$ (3)

$$W_w = MCF_w \cdot 0,14278 \cdot TR_w^{0,04} \cdot \left( \frac{AR_w}{(\cos \Lambda_{25w})^2} \right)^{0,6} \cdot \left( \frac{100 \cdot (t/c)_w}{\cos \Lambda_{25w}} \right)^{-0,3} \cdot q_{cr}^{0,006} \cdot S_w^{0,758} \cdot (1,5 \cdot n_1 \cdot W_{TO})^{0,49} \cdot W_{fw}^{0,0035}$$

### 18.2 Horizontal Tail, $W_{HT}$ (3)

$$W_{HT} = MCF_{HT} \cdot 0,044194 \cdot TR_{HT}^{-0,02} \cdot \left( \frac{AR_{HT}}{(\cos \Lambda_{25HT})^2} \right)^{0,043} \cdot \left( \frac{100 \cdot (t/c)_{HT}}{\cos \Lambda_{25HT}} \right)^{-0,12} \cdot q_{cr}^{0,168} \cdot S_{HT}^{0,896} \cdot (1,5 \cdot n_1 \cdot W_{TO})^{0,414}$$

### 18.3 Vertical Tail, $W_{VT}$

$$W_{VT} = MCF_{VT} \cdot N_{VT} \cdot 0,22136 \cdot TR_{VT}^{0,039} \cdot (1 + 0,2 \cdot a) \cdot \left( \frac{AR_{VT}}{(\cos \Lambda_{25VT})^2} \right)^{0,357} \cdot \left( \frac{100 \cdot (t/c)_{VT}}{\cos \Lambda_{25VT}} \right)^{-0,49} \cdot q_{cr}^{0,122} \cdot S_{VT}^{0,873} \cdot (1,5 \cdot n_1 \cdot W_{TO})^{0,376}$$

With:

|              | a |
|--------------|---|
| Conventional | 0 |
| T-tail       | 1 |

### 18.4 Canard Surface, $W_{crd}$ (3)

$$W_{crd} = MCF_{crd} \cdot 0,044194 \cdot TR_{crd}^{-0,02} \cdot \left( \frac{AR_{crd}}{(\cos \Lambda_{25crd})^2} \right)^{0,043} \cdot \left( \frac{100 \cdot (t/c)_{crd}}{\cos \Lambda_{25crd}} \right)^{-0,12} \cdot q_{cr}^{0,168} \cdot S_{crd}^{0,896} \cdot (1,5 \cdot n_1 \cdot W_{TO})^{0,414}$$

### 18.5 Winglets, $W_{wgl}$

$$W_{wgl} = MCF_{wgl} \cdot N_{wgl} \cdot 0,22136 \cdot TR_{wgl}^{0,039} \cdot \left( \frac{AR_{wgl}}{(\cos \Lambda_{25wgl})^2} \right)^{0,357} \cdot \left( \frac{100 \cdot (t/c)_{wgl}}{\cos \Lambda_{25wgl}} \right)^{-0,49} \cdot q_{cr}^{0,122} \cdot S_{wgl}^{0,873} \cdot (1,5 \cdot n_1 \cdot W_{TO})^{0,376}$$

### 18.6 Fuselage, $W_{fus}$ (3)

$$W_{fus} = MCF_{fus} \cdot 0,13274 \cdot q_{cr}^{0,241} \cdot \left( \frac{L_{fus}}{MD_{fus}} \right)^{-0,072} \cdot L_{APfus}^{-0,051} \cdot WA_{fus}^{1,086} \cdot (1,5 \cdot n_1 \cdot W_{TO})^{0,177} + W_{press}$$

### 18.7 Nacelle, $W_{nac}$

$$W_{nac} = MCF_{nac} \cdot 0,13274 \cdot q_{cr}^{0,241} \cdot \left( \frac{L_{nac}}{MD_{nac}} \right)^{-0,072} \cdot WA_{nac}^{1,086} \cdot (1,5 \cdot n_1 \cdot W_{TO})^{0,177}$$



### 18.8 Tailboom, $W_{tb}$

$$W_{tb} = MCF_{tb} \cdot N_{TB} \cdot 0,13274 \cdot q_{cr}^{0,241} \cdot \left( \frac{L_{tb}}{MD_{tb}} \right)^{-0,072} \cdot WA_{tb}^{1,086} \cdot (1,5 \cdot n_1 \cdot W_{TO})^{0,177}$$

### 18.9 Landing gear (main), $W_{LGM}$ (6)

$$W_{LGM} = MCF_{LGM} \cdot a \cdot b \cdot c \cdot W_{TO}$$

With:

|                           | a   | b   | c     |
|---------------------------|-----|-----|-------|
| Conventional, fixed       | 1.0 | 0.8 | 0.045 |
| Conventional, retractable | 1.5 | 0.8 | 0.045 |
| Tricycle, fixed           | 1.0 | 0.7 | 0.055 |
| Tricycle, retractable     | 1.5 | 0.7 | 0.055 |
| Single wheel, fixed       | 1.0 | 0.4 | 0.045 |
| Single wheel, retractable | 1.5 | 0.4 | 0.045 |

### 18.10 Landing gear (auxiliary), $W_{LGA}$ (6)

$$W_{LGA} = MCF_{LGA} \cdot a \cdot b \cdot c \cdot W_{TO}$$

With:

|                           | a   | b   | c     |
|---------------------------|-----|-----|-------|
| Conventional, fixed       | 1.0 | 0.2 | 0.045 |
| Conventional, retractable | 1.5 | 0.2 | 0.045 |
| Tricycle, fixed           | 1.0 | 0.3 | 0.055 |
| Tricycle, retractable     | 1.5 | 0.3 | 0.055 |

### 18.11 Propulsion, $W_p$ (6)

$$W_p = MCF_p \cdot N_{eng} \cdot (a \cdot W_{engdry} - W_{prop})$$

With:

|                  | a    |
|------------------|------|
| 4 stroke         | 1.30 |
| 2 stroke         | 1.30 |
| 4 stroke, Diesel | 1.30 |
| 2 stroke, Diesel | 1.30 |
| Rotary           | 1.90 |
| Turbopropeller   | 1.70 |
| Turbojet         | 1.25 |
| Electric         | 1.00 |

### 18.12 Propeller, $W_{prop}$

$$W_{prop} = MCF_{prop} \cdot N_{prop} \cdot a \cdot \left( \frac{P_{eng}}{1000} \right)$$

With:

|   | a      |
|---|--------|
| Hydraulic (variable pitch – constant speed) | 0.0888 |
| Electric (variable pitch – constant speed)  | 0.1167 |
| Fixed – Ground adjustable                   | 0.0572 |

### 18.13 Propeller Shaft, $W_{PS}$

$$W_{PS} = MCF_{PS} \cdot 1.1 \cdot \left[ \pi \cdot (0.5 \cdot 0.01 \cdot D_{PS})^2 \cdot 79 \right] \cdot l_{PS}$$

### 18.14 Fuel System, $W_{FSyst}$ (3)

$$W_{FSyst} = MCF_{FSyst} \cdot 0,4299 \cdot N_{eng}^{0,157} \cdot N_{Ftank}^{0,242} \cdot V_{Ftot}^{0,726}$$

### 18.15 Control System, $W_{CSyst}$ (3)

$$W_{CSyst} = MCF_{CSyst} \cdot 2,7519 \cdot 10^{-4} \cdot L_{fus}^{1,536} \cdot b_w^{0,371} \cdot (1,5 \cdot n_1 \cdot W_{TO})^{0,8}$$

### 18.16 Electrical System, $W_{ESyst}$ (6)

$$W_{ESyst} = MCF_{ESyst} \cdot 0,03 \cdot W_{TO}$$

### 18.17 Hydraulic System, $W_{HSyst}$ (6)

$$W_{HSyst} = MCF_{HSyst} \cdot 0,03 \cdot W_{TO}$$

### 18.18 Avionics, $W_{inst}$ (6)

$$W_{inst} = MCF_{inst} \cdot 0,015 \cdot W_{TO}$$

### 18.19 Furnishings, $W_{furn}$

$$W_{furn} = MCF_{furn} \cdot (0,000004 \cdot W_{TO}^2 + 0,0325 \cdot W_{TO})$$

### 18.20 Air Conditioning, $W_{AirCond}$ (3)

$$W_{AirCond} = MCF_{AirCond} \cdot 0,20743 \cdot W_{TO}^{0,52} \cdot N_{occ}^{0,68} \cdot W_{inst}^{0,17} \cdot M^{0,08}$$

### 18.21 Pressurization, $W_{\text{press}}$ (3)

$$W_{\text{press}} = MCF_{\text{press}} \cdot \left( 5,4026 + 2,4621 \cdot (V_{\text{press}} \cdot \Delta_{\text{press fus}})^{0,271} \right)$$

# Annex 19. Inboard isometric drawings

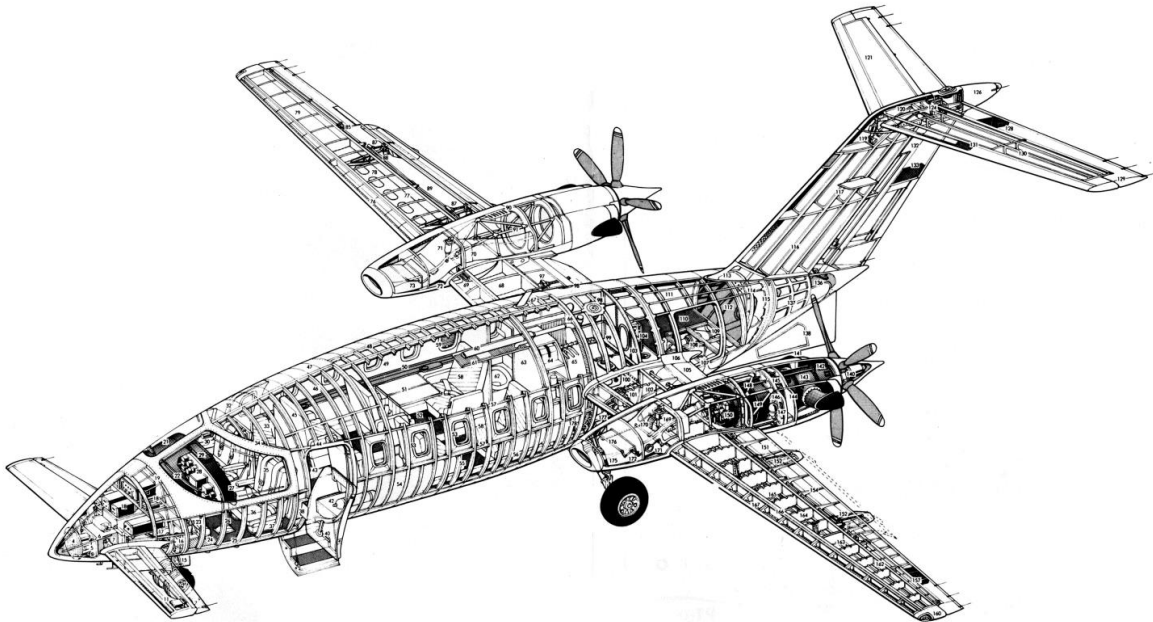


Figure 1: Avanti Piaggio

## FAIRCHILD A-10A

Noteworthy features in this presentation of the A-10A by "Flight" artist Mike Badrocke are the thick, large-area, three-segment wing with single slotted Fowler flaps and split aileron/dive-brake; the relative size of the GAU-8/A gun and its ammunition drum, which fits into a 22-ft-long bay in the underside of the fuselage; the main wheels retracting into underwing fairings; and the podded engines with slanted pylons to provide trim changes with thrust. The large weapon is HABS, a standard 2,000-lb bomb with television guidance. Three Hughes Mowerick anti-tank missiles are mounted on the detached pylon.

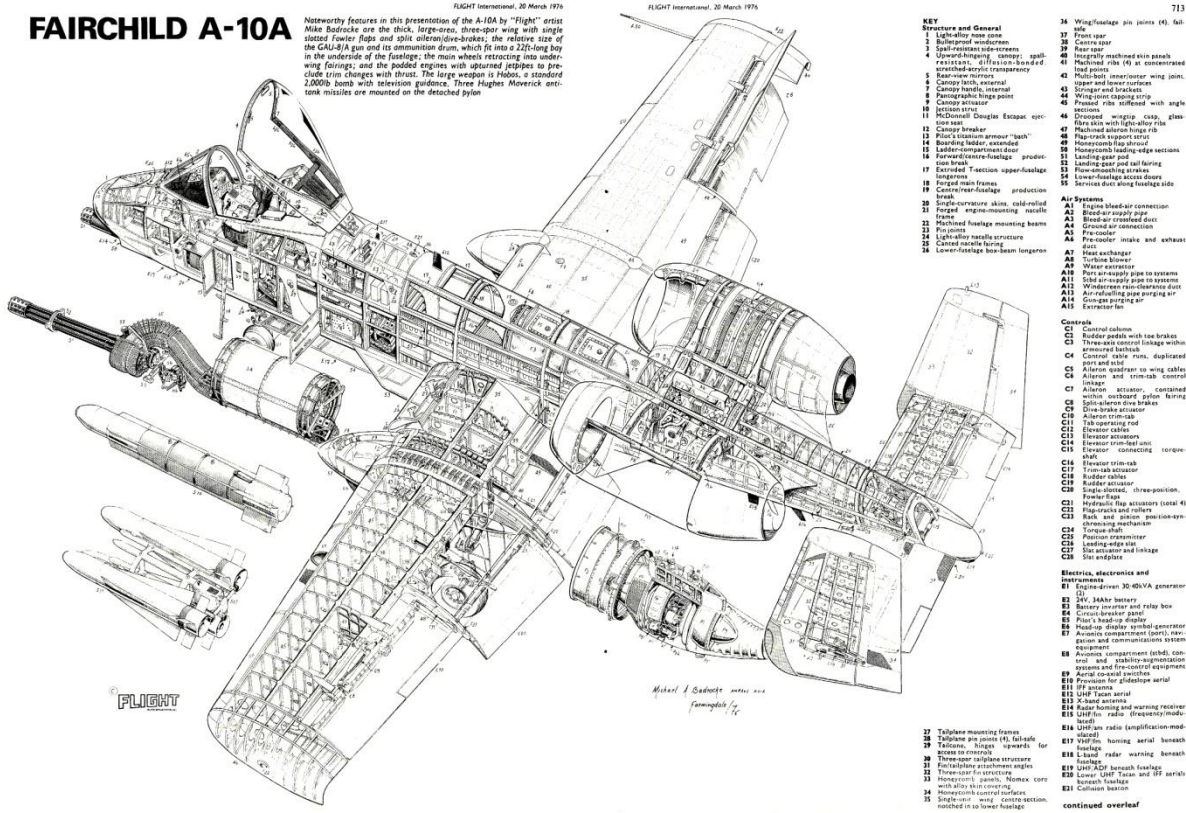
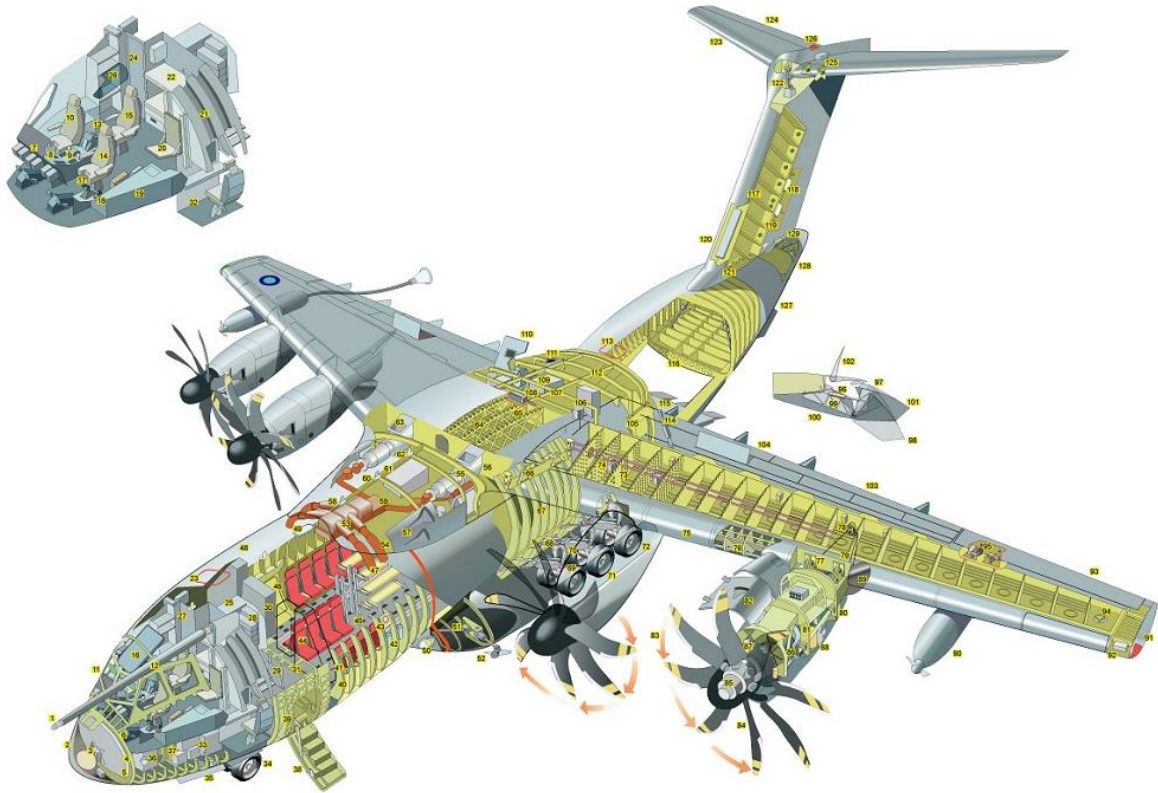
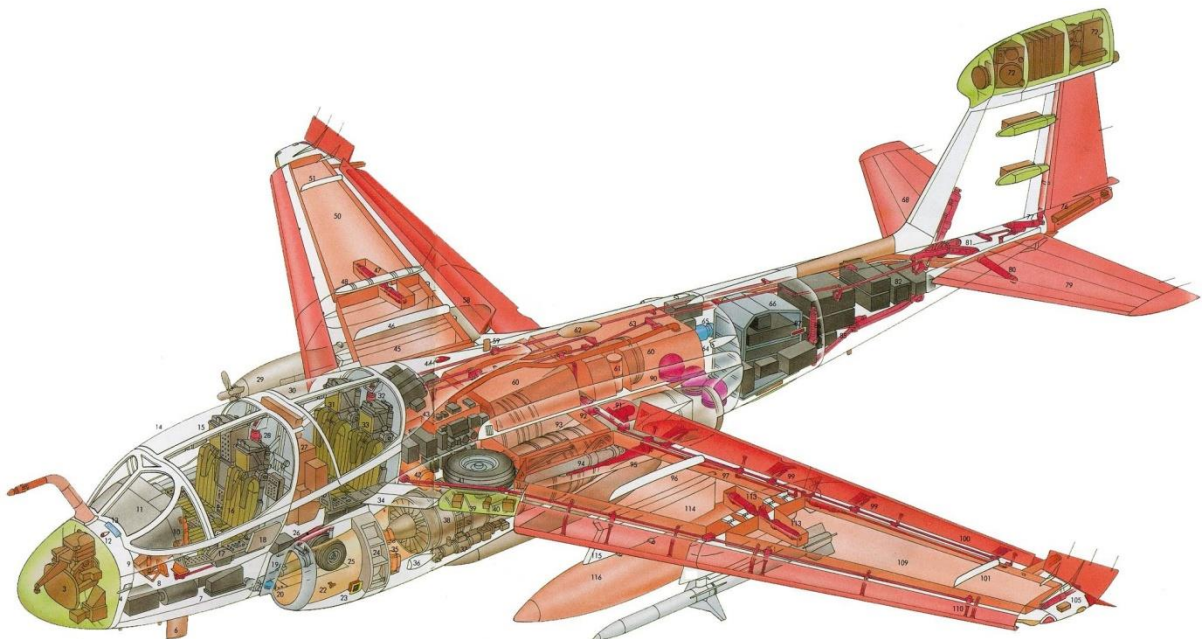


Figure 2: Fairchild A-10A



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Figure 3: Airbus A400M



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Figure 4: Grumman A-6 Intruder