

# Électronique

## TD Filtrage

May 6, 2020

### Synthèse d'un filtre passe-bande

Le but est ici de concevoir un filtre passe-bande, en utilisant deux structures différentes, et en respectant le cahier des charges suivant:

Type de filtre	Passe-bande
Fréquence centrale	10 kHz
Bande passante (BP)	$B = 1 \text{ kHz}$
Bande d'atténuation (BA)	$B' = 3 \text{ kHz}$
Atténuation minimale dans la BA	10 dB
Contrainte	Amplitude la plus plate possible dans la BP

### 1 Fonction de transfert du filtre

- En utilisant le cahier de charges, dessiner le gabarit correspondant.

*Afin de tracer le gabarit, il convient tout d'abord de calculer les fréquences  $f_1$ ,  $f_2$ ,  $f'_1$  et  $f'_2$ . Nous disposons pour cela de deux relations par couple de fréquences. D'un part:*

$$f_2 - f_1 = 1 \text{ kHz} \text{ et } f'_2 - f'_1 = 3 \text{ kHz}$$

*D'autre part, on définit la fréquence centrale avec:*

$$f_0 = \sqrt{f_1 f_2} = \sqrt{f'_1 f'_2}$$

*Avec les fréquences  $f_1$  et  $f_2$ , on obtient l'équation du second degré suivante:*

$$f_0^2 = f_1 f_2 = f_1(f_1 + B) = f_1^2 + B f_1$$

*On trouve alors (en ne gardant que la solution positive):*

$$f_1 = \frac{-B + \sqrt{B^2 + 4f_0^2}}{2}$$

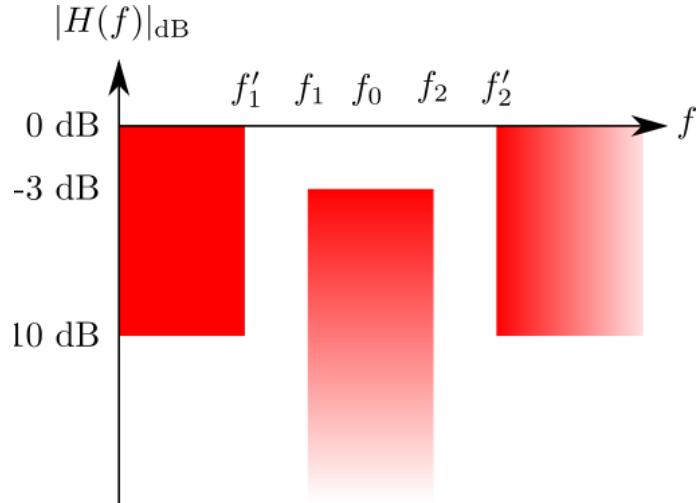


Figure 1: Gabarit du filtre passe-bande.

et donc:

$$f_2 = B + f_1 = \frac{B + \sqrt{B^2 + 4f_0^2}}{2}$$

On trouve de la même manière:

$$f'_1 = \frac{-B' + \sqrt{B'^2 + 4f_0^2}}{2} \text{ et } f'_2 = \frac{B' + \sqrt{B'^2 + 4f_0^2}}{2}$$

L'application numérique nous donne  $f_1 \approx 9512,5 \text{ Hz}$ ,  $f_2 \approx 10512,5 \text{ Hz}$ ,  $f'_1 \approx 8611,9 \text{ Hz}$ , et  $f'_2 \approx 11612,9 \text{ Hz}$ . Le gabarit du filtre passe-bande est représenté sur la figure 1.

2. Normaliser le filtre en calculant les fréquences à X dB.

La normalisation des fréquences donne  $f_c = 1$  (comme toujours pour la passe bas normalisé) et  $X = B'/B = 3$ . La gabarit du filtre passe-bas normalisé est représenté sur la figure 2

3. En utilisant les abaques pour les filtres passe-bas normalisés fournies à la fin du document, déterminer le type et l'ordre du filtre qui répond au cahier des charges.

La contrainte d'amplitude la plus plate possible indique l'utilisation d'un filtre de Butterworth. L'abaque correspondant indique d'un filtre passe-bas normalisé d'ordre 1 convient (la première courbe passe sous le point [3, -10 dB]). Attention: lors de la dénormalisation, on filtre passe-bas normalisé d'ordre 1 donnera un filtre passe-bande d'ordre 2.

4. Donner la fonction de transfert du filtre passe-bas normalisé correspondant. On donne la forme générale des racines des polynômes de Butterworth en fonction

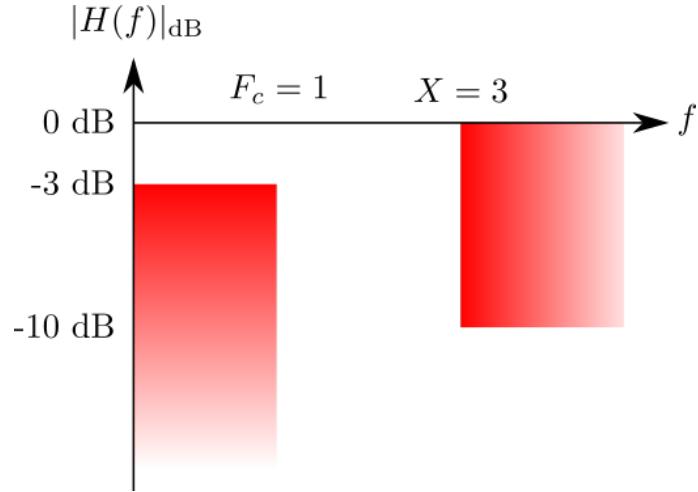


Figure 2: Gabarit du filtre passe-bas normalisé.

de l'ordre  $n$  ( $k \leq n$ ):

$$s_k = -\sin\left(\frac{2k-1}{2n}\pi\right) \pm i \cos\left(\frac{2k-1}{2n}\pi\right)$$

Avec la formule donnée, la racine unique pour un ordre 1 est  $s_1 = -1$ .  
 Le polynôme s'écrit donc:

$$H(s) = \frac{|s_1|^2}{s - s_1} = \frac{1}{s + 1} \rightarrow H(j\omega) = \frac{1}{1 + j\omega}$$

5. En utilisant le changement de variable suivant, calculer la fonction de transfert du filtre après dé-normalisation:

$$f \rightarrow \frac{f_0}{B} \left( \frac{f}{f_0} - \frac{f_0}{f} \right)$$

Exprimé en pulsation, le changement de variable s'écrit:

$$\omega \rightarrow \frac{\omega_0}{B''} \left( \frac{\omega}{\omega_0} - \frac{\omega_0}{\omega} \right) \text{ avec } B'' = 2\pi B$$

La dénormalisation donne ainsi:

$$H(j\omega) = \frac{1}{1 + j \frac{\omega_0}{B''} \left( \frac{\omega}{\omega_0} - \frac{\omega_0}{\omega} \right)} \quad (1)$$

$$= \frac{\frac{\omega}{\omega_0}}{\frac{\omega_0}{\omega_0} + j \frac{\omega^2}{B'' \omega_0} - j \frac{\omega_0}{B''}} = \frac{j \frac{\omega B''}{\omega_0^2}}{1 + j \frac{B'' \omega}{\omega_0^2} - \frac{\omega^2}{\omega_0^2}} \quad (2)$$

On pose alors le facteur de qualité  $Q = \omega_0/(2\pi B)$ , ce qui donne:

$$H(j\omega) = \frac{j \frac{\omega}{Q\omega_0}}{1 + j \frac{\omega}{Q\omega_0} - \frac{\omega^2}{\omega_0^2}}$$

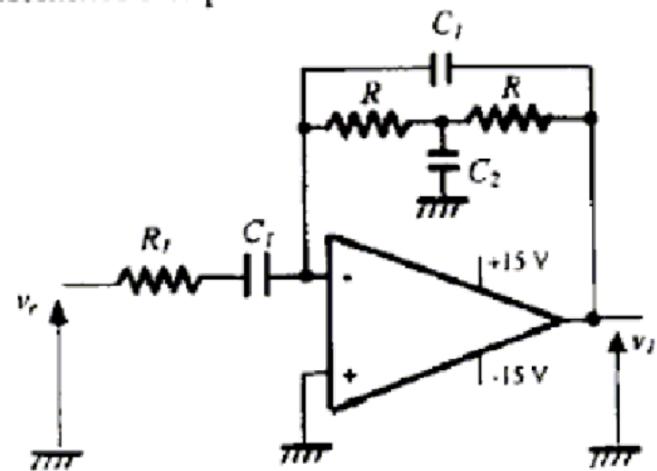


Figure 3: Première implémentation du filtre.

## 2 Première implémentation

On implémente tout d'abord le filtre en utilisant la structure présentée sur la figure 3, avec  $R_1 = (RC_2)/(2C_1)$ . On donne la fonction de transfert du filtre:

$$H(j\omega) = \frac{v_{\text{out}}}{v_{\text{in}}} = \frac{-\frac{j\omega}{Q\omega_0}}{1 + \frac{j\omega}{Q\omega_0} + \left(\frac{\omega}{\omega_0}\right)^2}$$

où  $Q = \frac{1}{2}\sqrt{\frac{C_2}{C_1}}$  and  $\omega_0 = \frac{1}{R\sqrt{C_1C_2}}$ .

6. En identifiant cette fonction de transfert à la fonction de transfert obtenue dans la partie 1, déterminer la valeur des capacités. On prendra  $R = 10 \text{ k}\Omega$ .

*Par identification, on a :*

$$Q = \frac{\omega_0}{2\pi B} = \frac{1}{2}\sqrt{\frac{C_2}{C_1}} \text{ et } \omega_0 = 2\pi f_0 = \frac{1}{R\sqrt{C_1C_2}} \rightarrow \sqrt{C_1C_2} = \frac{1}{R\omega_0}$$

*d'où:*

$$\frac{1}{2\pi BR\sqrt{C_1C_2}} = \frac{1}{2}\sqrt{\frac{C_2}{C_1}}$$

*et:*

$$C_2 = \frac{1}{\pi BR} \text{ et } C_1 = \frac{1}{R^2\omega_0^2 C_2} = \frac{\pi B}{R\omega_0^2}$$

L'application numérique donne:

$$C_2 \approx 31,8 \text{ nF} \text{ et } C_1 \approx 79,2 \text{ pF}$$

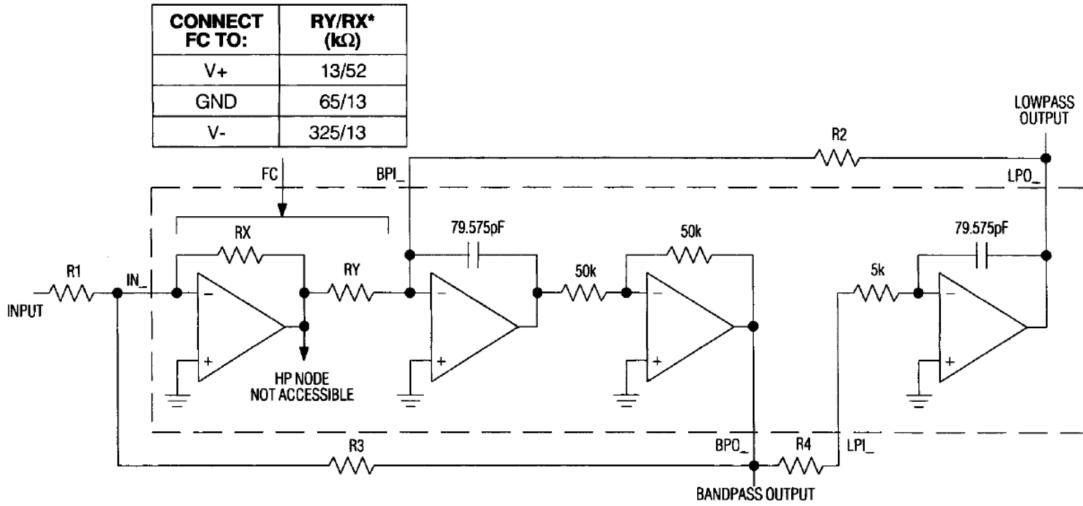


Figure 4: Seconde implémentation du filtre.

### 3 Implémentation avec la structure Biquad.

On désire maintenant réaliser le filtre en utilisant la structure Biquad présentée sur la figure 4. La fonction de transfert de ce filtre est donnée:

$$H_{BP}(s) = K' \frac{s \frac{\omega_0}{Q}}{s^2 + s \frac{\omega_0}{Q} + \omega_0^2}$$

avec  $\omega_0 = \frac{1}{C\sqrt{R_2(R_4+5\text{ k}\Omega)}}$ ,  $Q = \frac{R_3}{\sqrt{R_2(R_4+5\text{ k}\Omega)}} \left( \frac{R_Y}{R_X} \right)$  et  $K' = \frac{R_3}{R_1}$ .

7. Déterminer les résistances  $R_1$ ,  $R_2$ ,  $R_3$ , et  $R_4$  nécessaires pour obtenir un filtre passe-bande respectant le cahier des charges de départ.

*Avec les expressions données dans le cours ou dans la fiche technique du composant MAX274, on détermine les valeurs des résistances. Avec la fréquence centrale:*

$$R_2 = \frac{1}{2\pi f_0 C} \approx 200 \text{ k}\Omega$$

*D'où:*

$$R_4 = R_2 - 5 \text{ k}\Omega \approx 195 \text{ k}\Omega$$

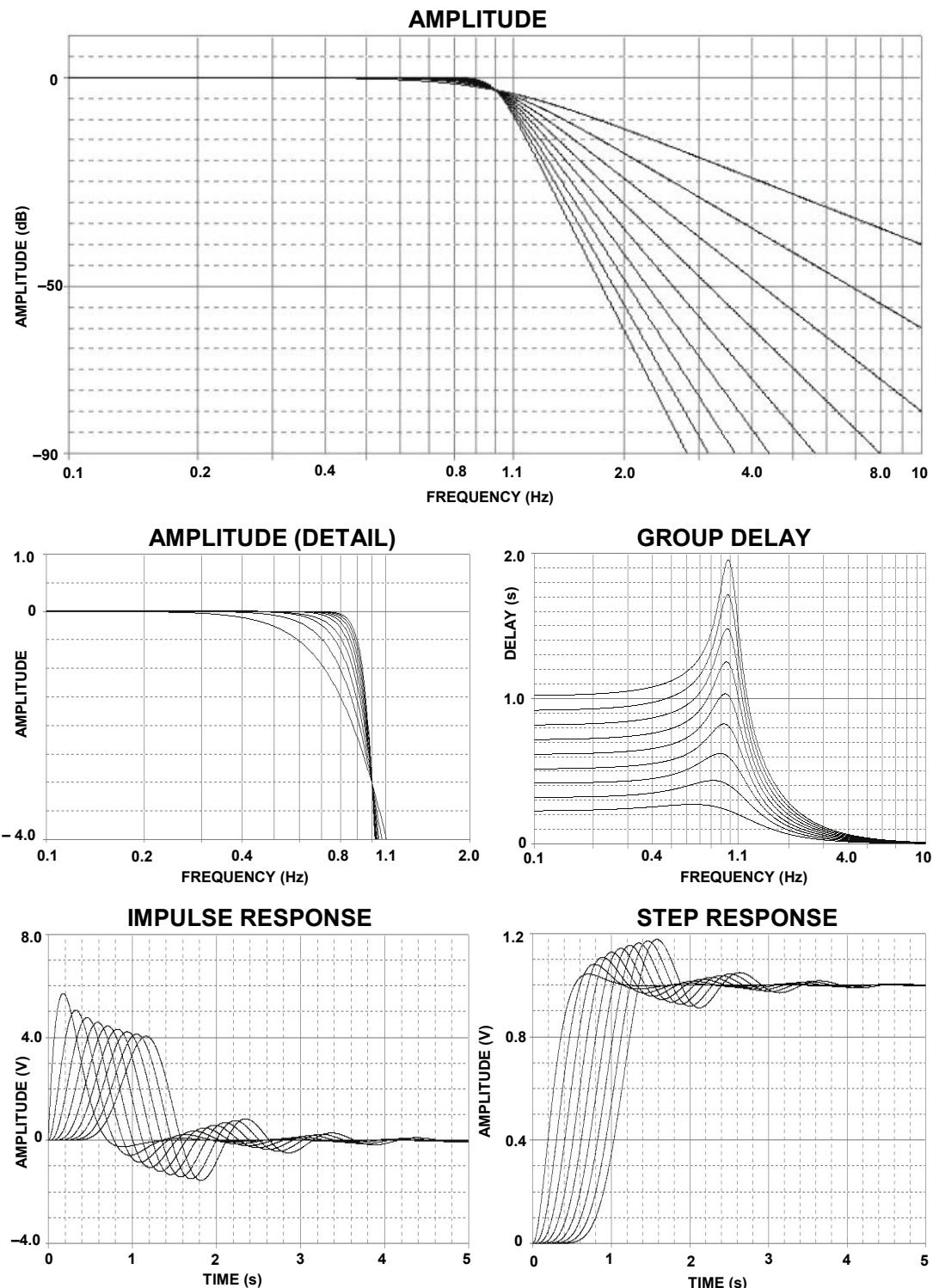
*Si on fixe  $R_Y/R_X = 5$  ( $FC=GND$ ), le facteur de qualité  $Q$  fixe la valeur de  $R_3$ :*

$$R_3 = Q \sqrt{R_2(R_4 + 5 \text{ k}\Omega)} \frac{R_X}{R_Y} \approx 400 \text{ k}\Omega$$

*Pour finir, si on souhaite un gain statique  $K = 1$ , on détermine  $R_1$ :*

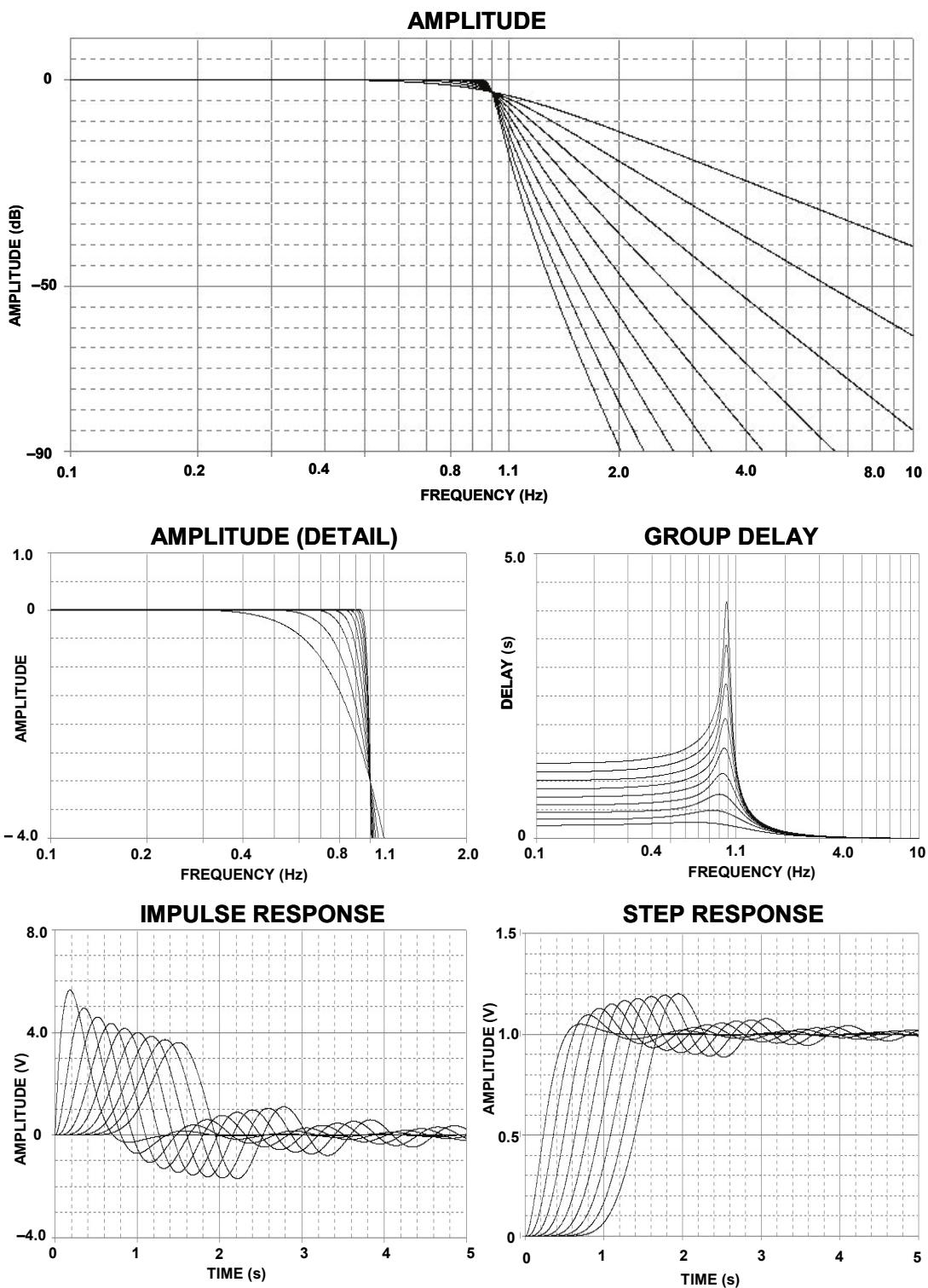
$$R_1 = \frac{R_3}{K} \approx 400 \text{ } k\Omega$$

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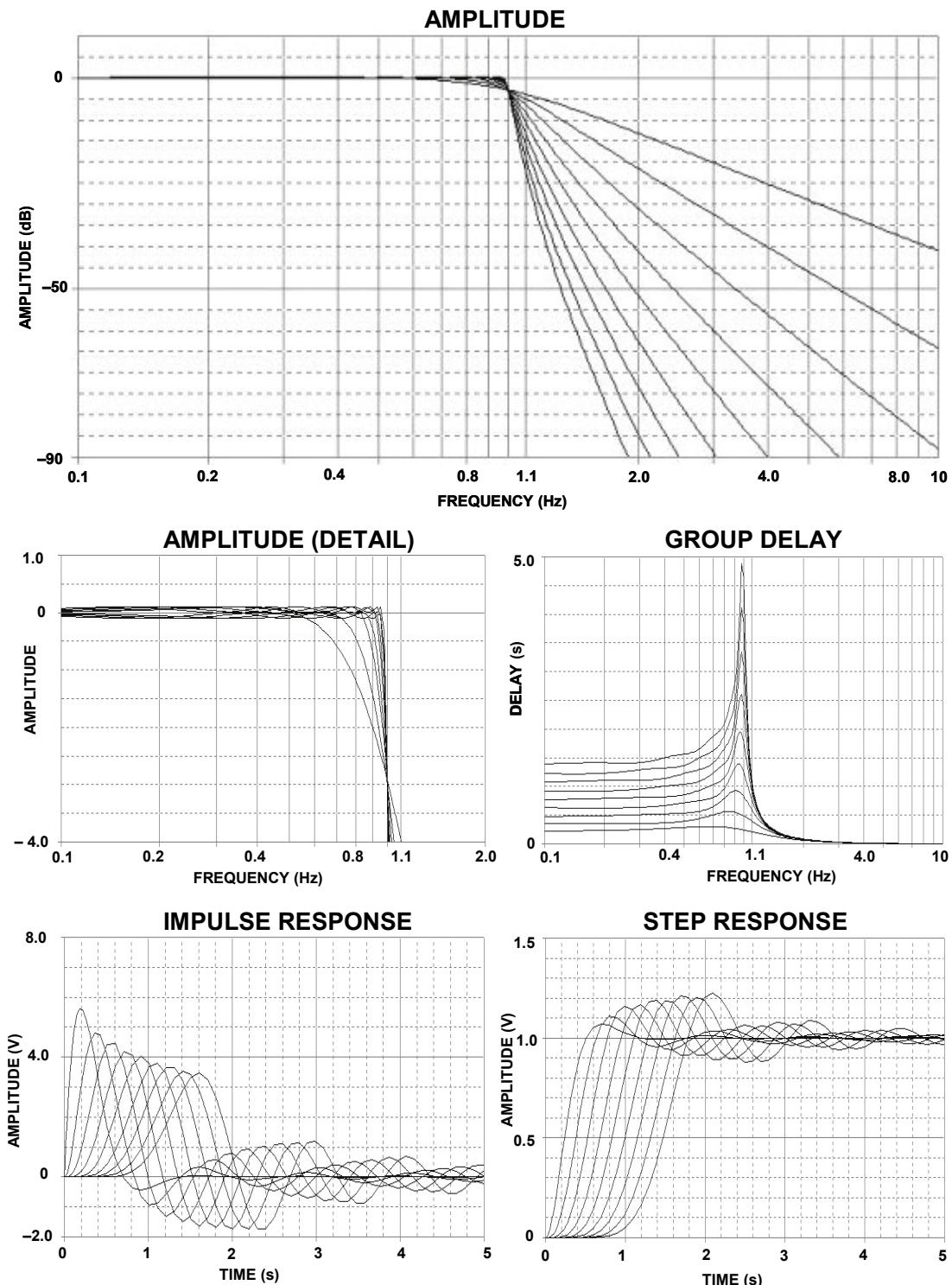
*Figure 8.15: Butterworth Response*

## ► BASIC LINEAR DESIGN



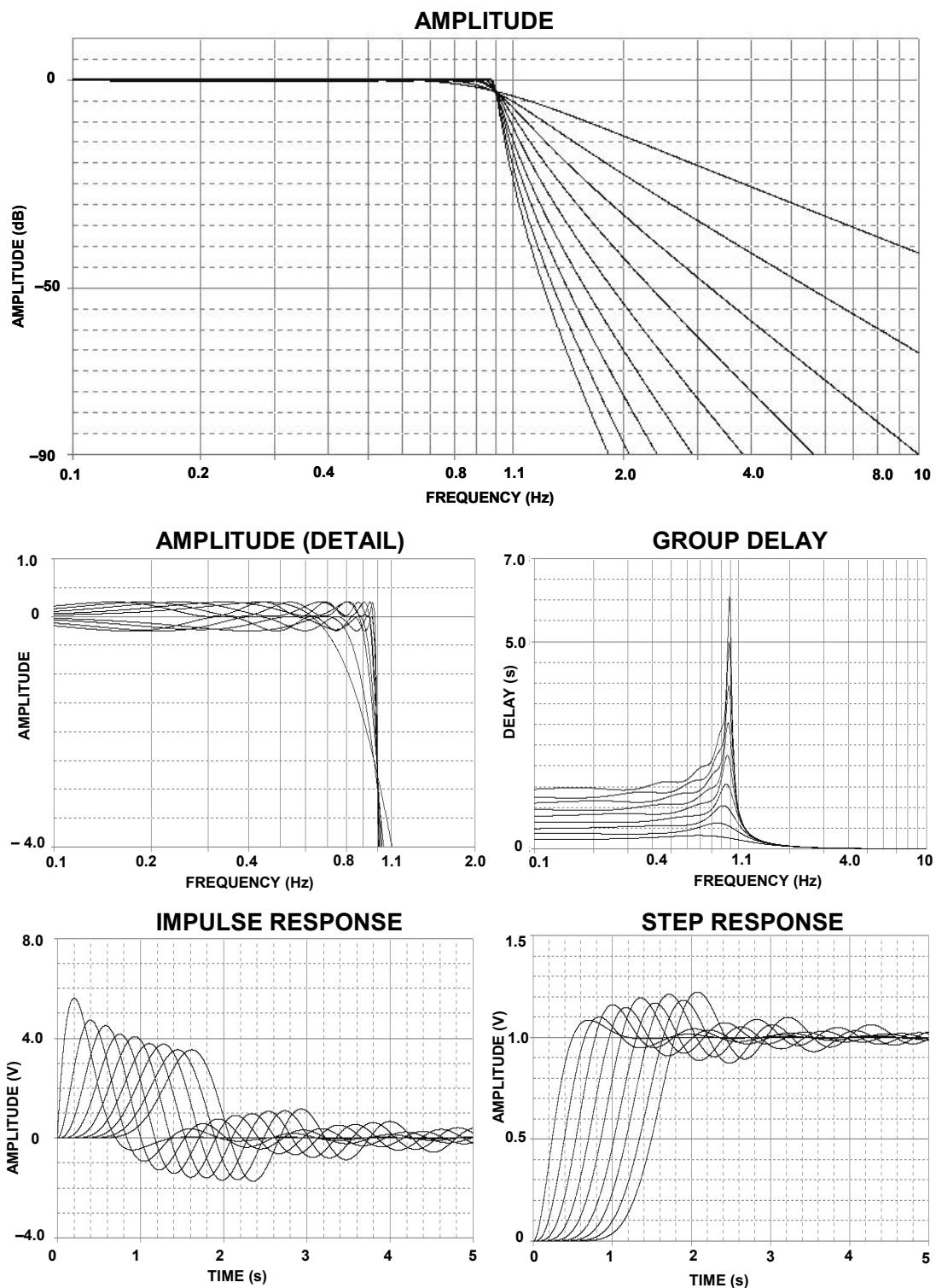
**Figure 8.16:** 0.01 dB Chebyshev Response

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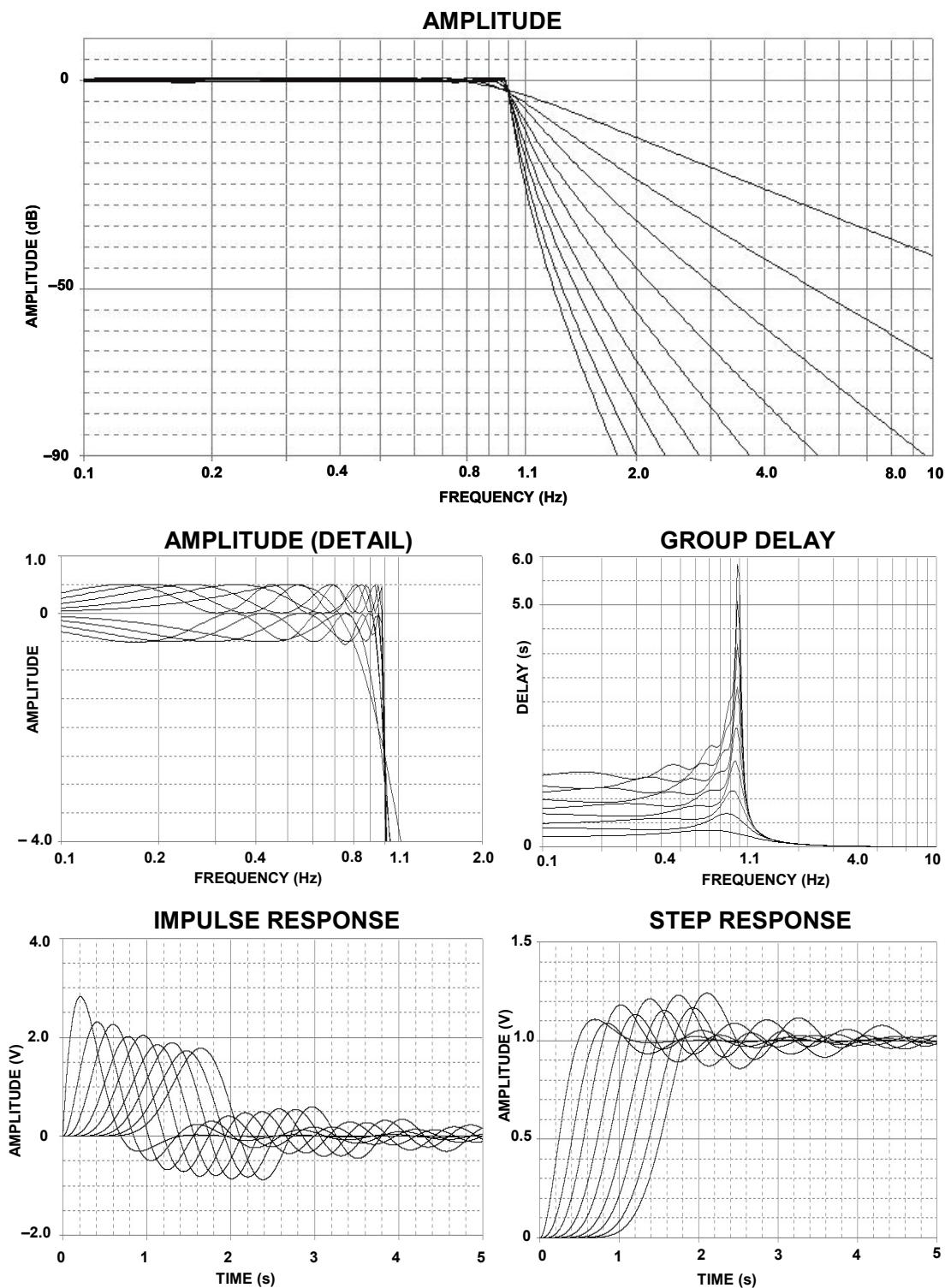
**Figure 8.17:** 0.1 dB Chebyshev Response

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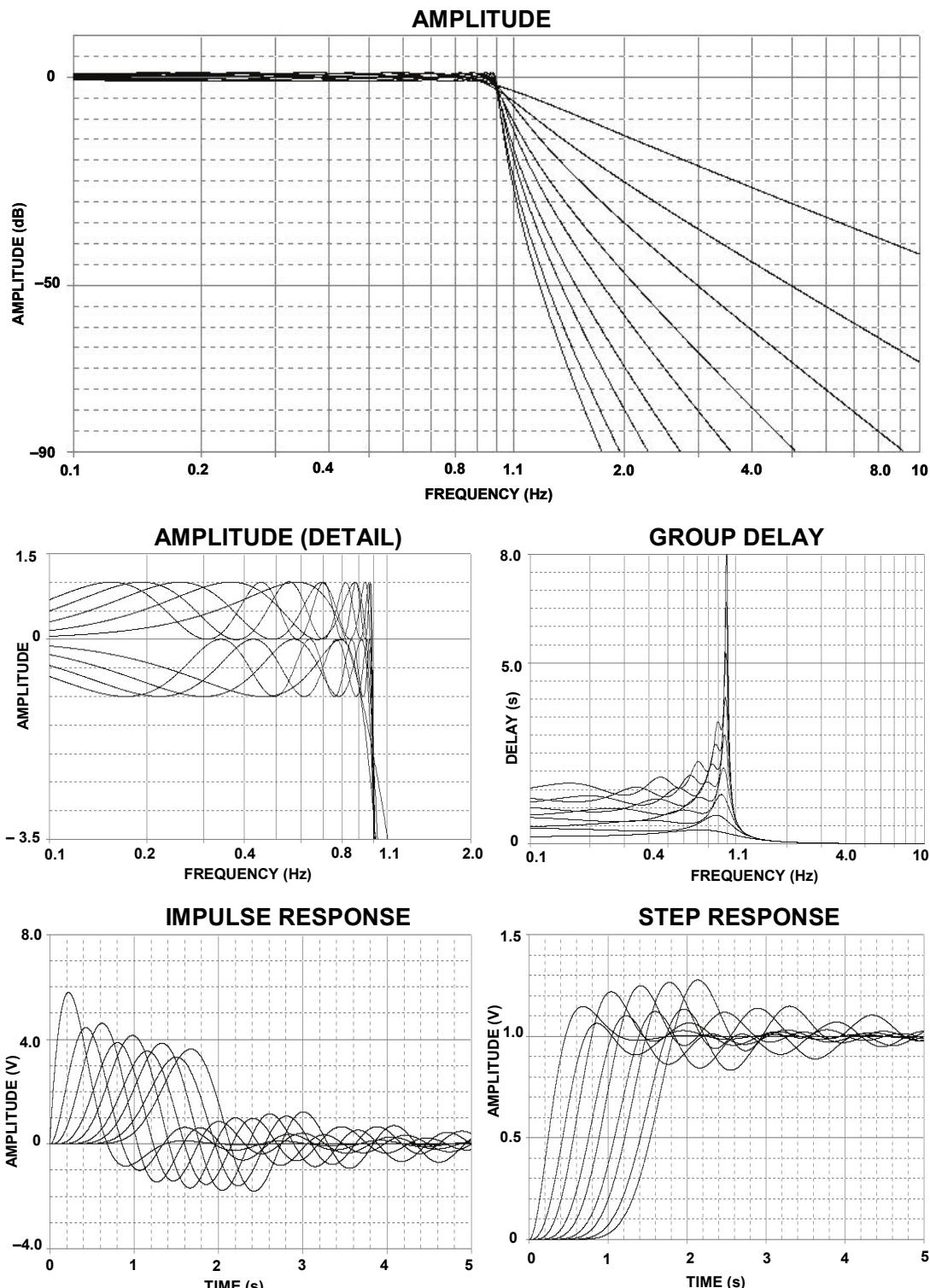
**Figure 8.18:** 0.25 dB Chebyshev Response

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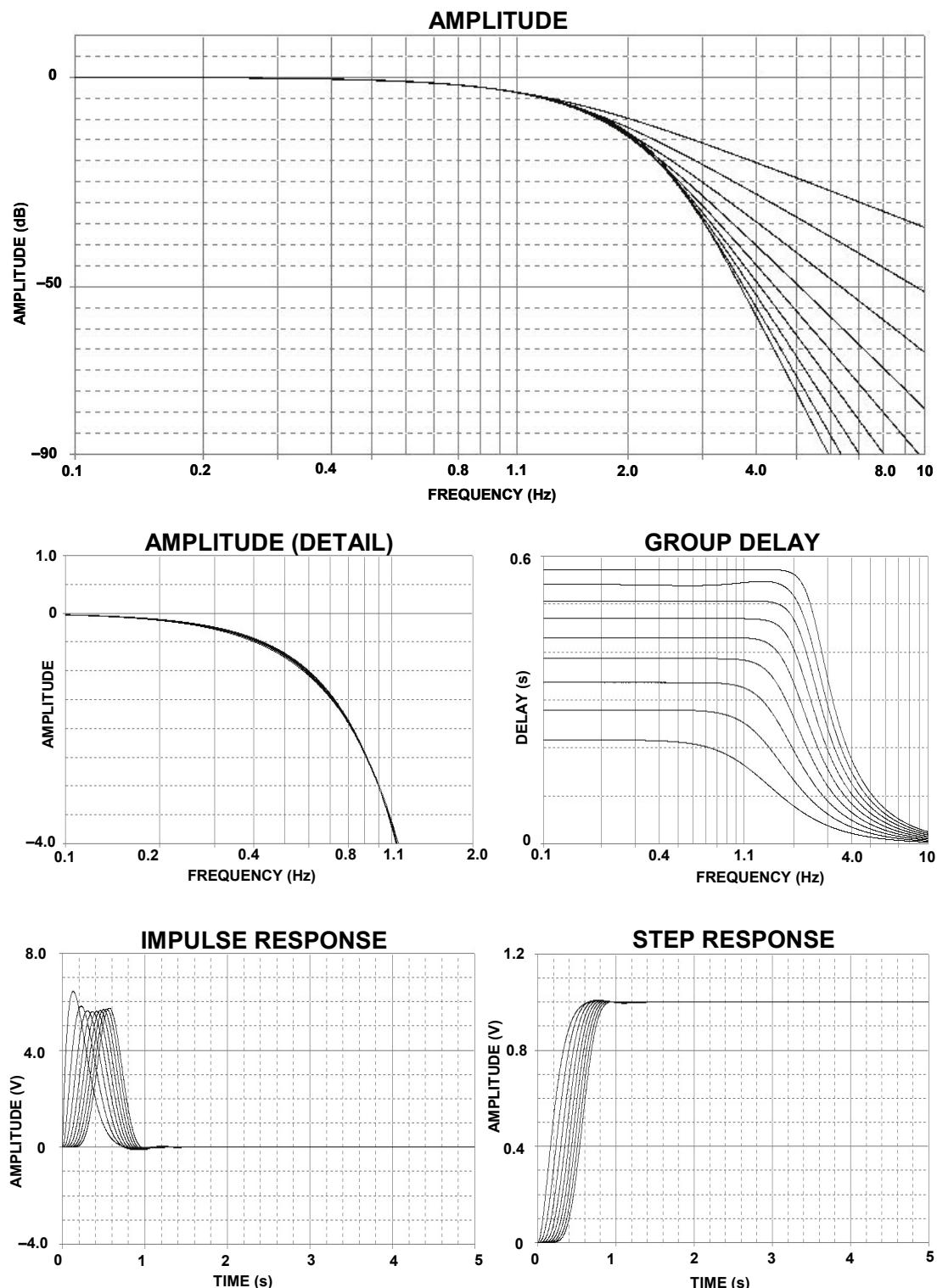
**Figure 8.19:** 0.5 dB Chebyshev Response

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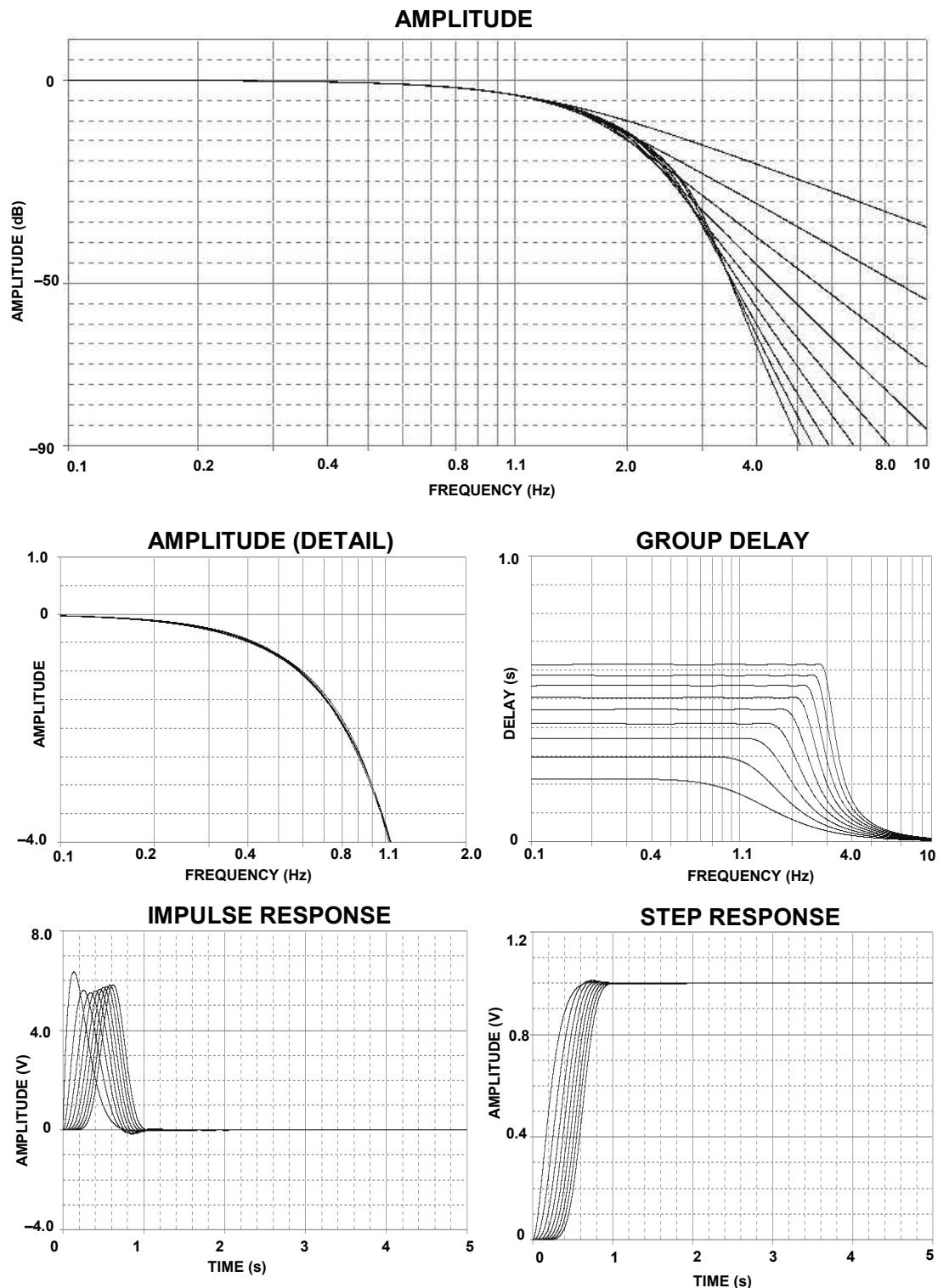
**Figure 8.20:** 1 dB Chebyshev Response

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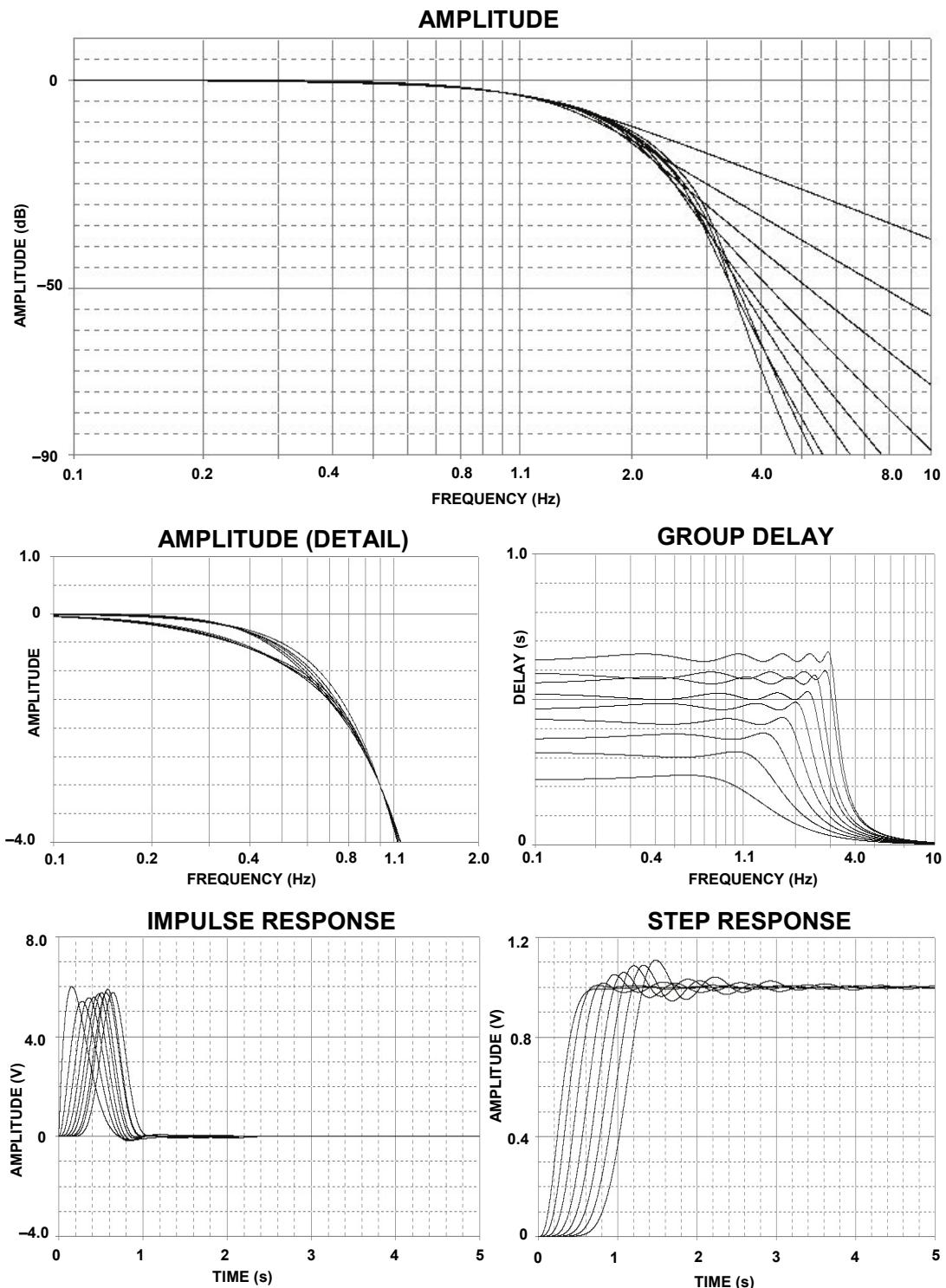
*Figure 8.21: Bessel Response*

## ► BASIC LINEAR DESIGN



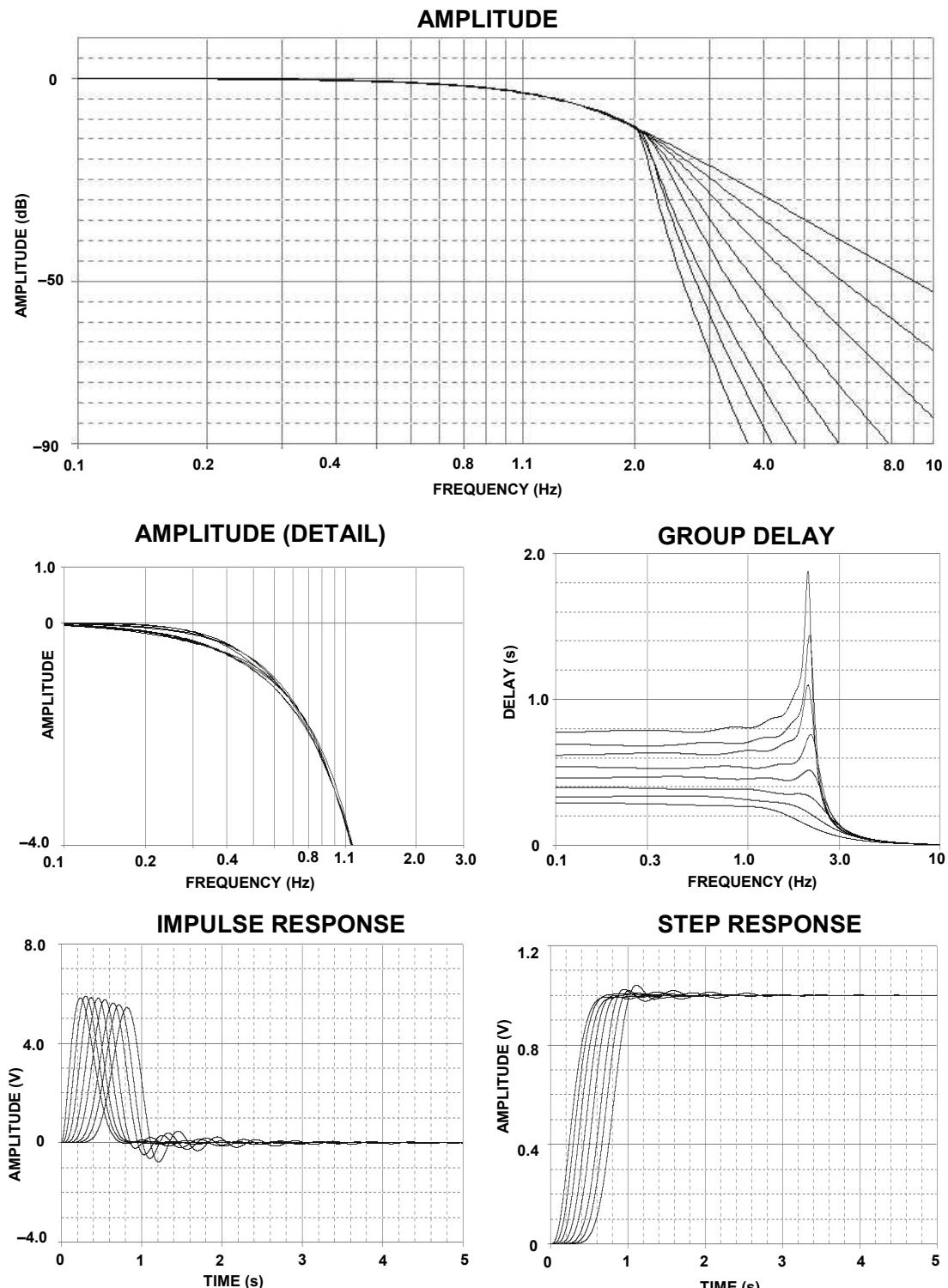
**Figure 8.22:** Linear Phase Response with Equiripple Error of  $0.05^\circ$

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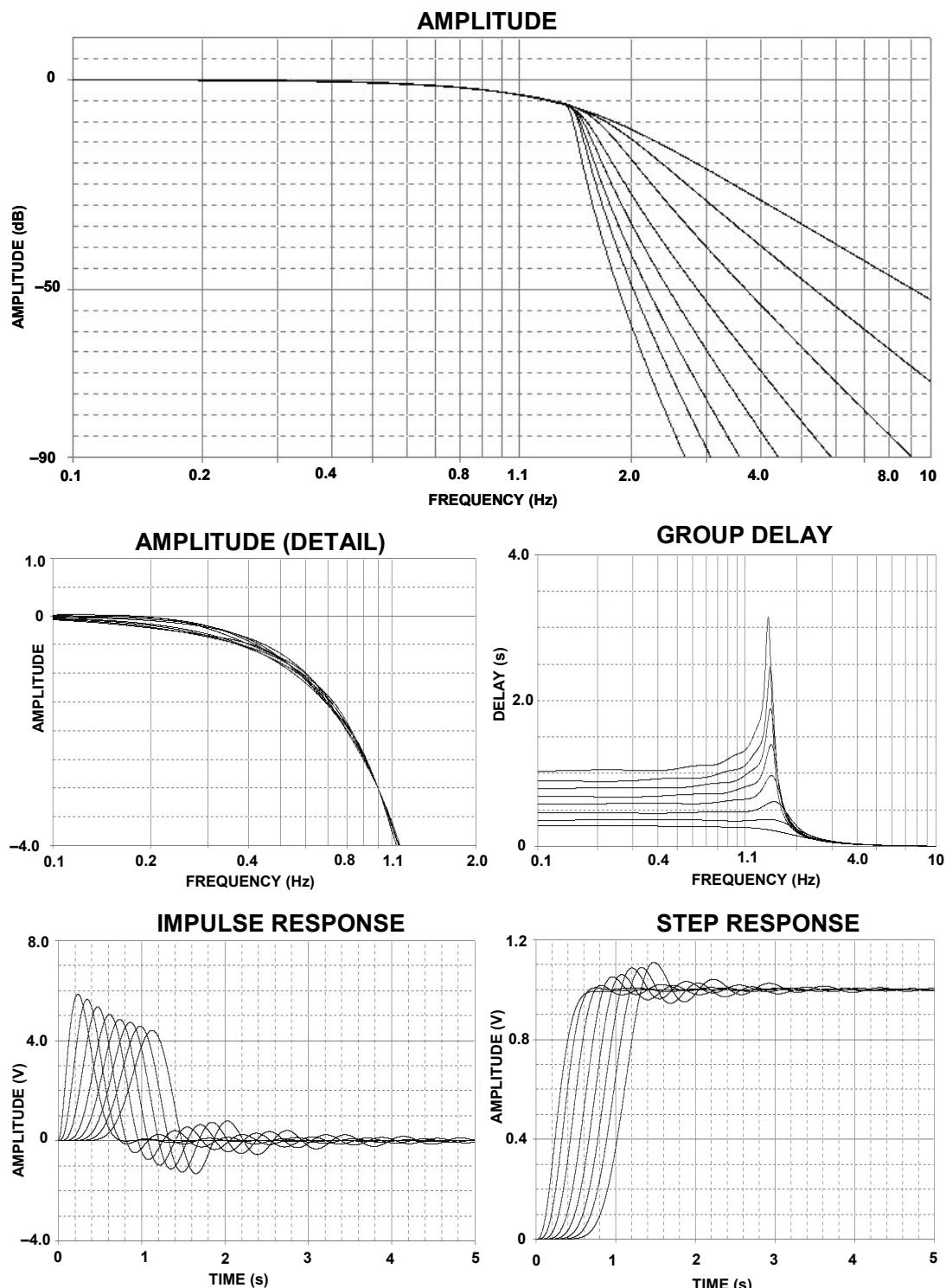
*Figure 8.23: Linear Phase Response with Equiripple Error of 0.5°*

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**Figure 8.24:** Gaussian to 12 dB Response

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*Figure 8.25: Gaussian to 6 dB Response*

## ► BASIC LINEAR DESIGN

ORDER	SECTION	REAL PART	IMAGINARY PART	$F_o$	$\alpha$	Q	-3 dB FREQUENCY	PEAKING FREQUENCY	PEAKING LEVEL
2	1	0.7071	0.7071	1.0000	1.4142	0.7071	1.0000		
3	1	0.5000	0.8660	1.0000	1.0000	1.0000	1.0000	0.7071	1.2493
	2	1.0000		1.0000					
4	1	0.9239	0.3827	1.0000	1.8478	0.5412	0.7195		
	2	0.3827	0.9239	1.0000	0.7654	1.3065		0.8409	3.0102
5	1	0.8090	0.5878	1.0000	1.6180	0.6180	0.8588		
	2	0.3090	0.9511	1.0000	0.6180	1.6182		0.8895	4.6163
	3	1.0000		1.0000					
6	1	0.9659	0.2568	1.0000	1.9319	0.5176	0.6758		
	2	0.7071	0.7071	1.0000	1.4142	0.7071	1.0000		
	3	0.2568	0.9659	1.0000	0.5176	1.9319		0.9306	6.0210
7	1	0.9010	0.4339	1.0000	1.8019	0.5560	0.7449		
	2	0.6235	0.7818	1.0000	1.2470	0.8019		0.4717	0.2204
	3	0.2225	0.9749	1.0000	0.4450	2.2471		0.9452	7.2530
	4	1.0000		1.0000					
8	1	0.9808	0.1951	1.0000	1.9616	0.5098	0.6615		
	2	0.8315	0.5586	1.0000	1.6629	0.6013	0.8295		
	3	0.5556	0.8315	1.0000	1.1112	0.9000		0.6186	0.6876
	4	0.1951	0.9808	1.0000	0.3902	2.5628		0.9612	8.3429
	5	1.0000		1.0000					
9	1	0.9397	0.3420	1.0000	1.8794	0.5321	0.7026		
	2	0.7660	0.6428	1.0000	1.5320	0.6527	0.9172		
	3	0.5000	0.8660	1.0000	1.0000	1.0000		0.7071	1.2493
	4	0.1737	0.9848	1.0000	0.3474	2.8785		0.9694	9.3165
	5	1.0000		1.0000					
10	1	0.9877	0.1564	1.0000	1.9754	0.5062	0.6549		
	2	0.8910	0.4540	1.0000	1.7820	0.5612	0.7564		
	3	0.7071	0.7071	1.0000	1.4142	0.7071	1.0000		
	4	0.4540	0.8910	1.0000	0.9080	1.1013		0.7667	1.8407
	5	0.1564	0.9877	1.0000	0.3128	3.1970		0.9752	10.2023

**Figure 8.26:** Butterworth Design Table

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ORDER	SECTION	REAL	IMAGINARY	$F_o$	$\alpha$	Q	-3 dB	PEAKING	PEAKING
		PART	PART				FREQUENCY	FREQUENCY	LEVEL
2	1	0.6743	0.7075	0.9774	1.3798	0.7247		0.2142	0.0100
3	1	0.4233	0.8663	0.9642	0.8780	1.1389		0.7558	2.0595
4	1	0.6762	0.3828	0.7770	1.7405	0.5746	0.6069		
4	2	0.2801	0.9241	0.9656	0.5801	1.7237	0.8467		
5	1	0.5120	0.5879	0.7796	1.3135	0.7613		0.2889	0.0827
5	2	0.1966	0.9512	0.9711	0.4028	2.4824		0.9309	8.0772
	3	0.6328		0.6328			0.6328		
6	1	0.5335	0.25688	0.5930	1.7995	0.5557	0.4425		
6	2	0.3906	0.7072	0.8079	0.9670	1.0342		0.5895	1.4482
	3	0.1430	0.9660	0.9765	0.2929	3.4144		0.9554	10.7605
7	1	0.4393	0.4339	0.6175	1.4229	0.7028	0.6136		
7	2	0.3040	0.7819	0.8389	0.7247	1.3798		0.7204	3.4077
	3	0.1085	0.9750	0.9810	0.2212	4.5208		0.9689	13.1578
	4	0.4876		0.4876			0.4876		
8	1	0.4268	0.1951	0.4693	1.8190	0.5498	0.3451		
8	2	0.3168	0.5556	0.6396	0.9907	1.0094		0.4564	1.3041
	3	0.2418	0.8315	0.8659	0.5585	1.7906		0.7956	5.4126
	4	0.0849	0.9808	0.9845	0.1725	5.7978		0.9771	15.2977
9	1	0.3686	0.3420	0.5028	1.4661	0.6821	0.4844		
9	2	0.3005	0.6428	0.7096	0.8470	1.1807		0.5682	2.3008
	3	0.1961	0.8661	0.8880	0.4417	2.2642		0.8436	7.3155
	4	0.0681	0.9848	0.9872	0.1380	7.2478		0.9824	17.2249
	5	0.3923		0.3923			0.3923		
10	1	0.3622	0.1564	0.3854	1.8279	0.5471	0.2814		
10	2	0.3178	0.454	0.5542	1.1469	0.8719		0.3242	0.5412
	3	0.2522	0.7071	0.7507	0.6719	1.4884		0.6606	3.9742
	4	0.1619	0.891	0.9056	0.3576	2.7968		0.8762	9.0742
	5	0.0568	0.9877	0.9893	0.1128	8.8645		0.9861	18.9669

**Figure 8.27:** 0.01 dB Chebyshev Design Table

## ► BASIC LINEAR DESIGN

ORDER	SECTION	REAL PART	IMAGINARY PART	$F_o$	$\alpha$	$Q$	-3 dB FREQUENCY	PEAKING FREQUENCY	PEAKING LEVEL
2	1	0.6104	0.7106	0.9368	1.3032	0.7673		0.3638	0.0999
3	1	0.3490	0.8684	0.9359	0.7458	1.3408		0.7952	3.1978
	2	0.6970		0.6970			0.6970		
4	1	0.2177	0.9254	0.9507	0.4580	2.1834		0.8994	7.0167
	2	0.5257	0.3833	0.6506	1.6160	0.6188	0.5596		
5	1	0.3842	0.5884	0.7027	1.0935	0.9145		0.4457	0.7662
	2	0.1468	0.9521	0.9634	0.3048	3.2812		0.9407	10.4226
	3	0.4749		0.4749			0.4749		
6	1	0.3916	0.2580	0.4695	1.6682	0.5995	0.3879		
	2	0.2867	0.7077	0.7636	0.7509	1.3316		0.6470	3.1478
	3	0.1049	0.9667	0.9724	0.2158	4.6348		0.9610	13.3714
7	1	0.3178	0.4341	0.5380	1.1814	0.8464		0.2957	0.4157
	2	0.2200	0.7823	0.8126	0.5414	1.8469		0.7507	5.6595
	3	0.0785	0.9755	0.9787	0.1604	6.2335		0.9723	15.9226
	4	0.3528		0.3528			0.3528		
8	1	0.3058	0.1952	0.3628	1.6858	0.5932	0.2956		
	2	0.2529	0.5588	0.6106	0.8283	1.2073		0.4949	2.4532
	3	0.1732	0.8319	0.8497	0.4077	2.4531		0.8137	7.9784
	4	0.0608	0.9812	0.9831	0.1237	8.0819		0.9793	18.1669
	5	0.2790		0.2790			0.2790		
9	1	0.2622	0.3421	0.4310	1.2166	0.8219		0.2197	0.3037
	2	0.2137	0.6430	0.6776	0.6308	1.5854		0.6064	4.4576
	3	0.1395	0.8663	0.8775	0.3180	3.1450		0.8550	10.0636
	4	0.0485	0.9852	0.9864	0.0982	10.1795		0.9840	20.1650
	5	0.2790		0.2790			0.2790		
10	1	0.2493	0.1564	0.2943	1.6942	0.5902	0.2382		
	2	0.2249	0.4541	0.5067	0.8876	1.1266		0.3945	1.9880
	3	0.1785	0.7073	0.7295	0.4894	2.0434		0.6844	6.4750
	4	0.1146	0.8913	0.8986	0.2551	3.9208		0.8839	11.9386
	5	0.0395	0.9880	0.9888	0.0799	12.5163		0.9872	21.9565

**Figure 8.28:** 0.1 dB Chebyshev Design Table

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ORDER	SECTION	REAL PART	IMAGINARY PART	F <sub>0</sub>	$\alpha$	Q	-3 dB FREQUENCY	PEAKING FREQUENCY	PEAKING LEVEL
2	1	0.5621	0.7154	0.9098	1.2356	0.8093	0.4425	0.2502	
3	1	0.3062	0.8712	0.9234	0.6632	1.5079	0.8156	4.0734	
4	1	0.4501	0.3840	0.5916	1.5215	0.6572	0.5470		
4	2	0.1865	0.9272	0.9458	0.3944	2.5356			
5	1	0.3247	0.5892	0.6727	0.9653	1.0359	0.4917	1.4585	
5	2	0.1240	0.9533	0.9613	0.2580	3.8763	0.9452	11.8413	
5	3	0.4013		0.4013		0.4013			
6	1	0.3284	0.2593	0.4184	1.5697	0.6371	0.3730	0.6663	4.3121
6	2	0.2404	0.7083	0.7480	0.6428	1.5557			
6	3	0.0880	0.9675	0.9715	0.1811	5.5205	0.9635	14.8753	
7	1	0.2652	0.4344	0.5090	1.0421	0.9596	0.3441	1.0173	
7	2	0.1835	0.7828	0.8040	0.4565	2.1908	0.7610	7.0443	
7	3	0.0655	0.9761	0.9783	0.1339	7.4679	0.9739	17.4855	
7	4	0.2944		0.2944		0.2944			
8	1	0.2543	0.1953	0.3206	1.5862	0.6304	0.2822	0.5126	3.4258
8	2	0.2156	0.5561	0.5964	0.1730	1.3832			
8	3	0.1441	0.8323	0.8447	0.3412	2.9309	0.8197	9.4683	
8	4	0.0506	0.9817	0.9830	0.1029	9.7173	0.9804	19.7624	
9	1	0.2176	0.3423	0.4056	1.0730	0.9320	0.2642	0.8624	
9	2	0.1774	0.6433	0.6673	0.5317	1.8808	0.6184	5.8052	
9	3	0.1158	0.8667	0.8744	0.2649	3.7755	0.8589	11.6163	
9	4	0.0402	0.9856	0.9864	0.0815	12.2659	0.9848	21.7812	
9	5	0.2315		0.2315		0.2315			
10	1	0.2065	0.1565	0.2591	1.5940	0.6274	0.2267	0.4143	3.0721
10	2	0.1863	0.4543	0.4910	0.7588	1.3178			
10	3	0.1478	0.7075	0.7228	0.4090	2.4451	0.6919	7.9515	
10	4	0.0949	0.8915	0.8965	0.2117	4.7236	0.8864	13.5344	
10	5	0.0327	0.9883	0.9888	0.0661	15.1199	0.9878	23.5957	

**Figure 8.29:** 0.25 dB Chebyshev Design Table

## ► BASIC LINEAR DESIGN

ORDER	SECTION	REAL PART		IMAGINARY PART		$F_0$	$\alpha$	$Q$	-3 dB FREQUENCY	PEAKING FREQUENCY	PEAKING LEVEL
		REAL	IMAGINARY	REAL	IMAGINARY						
2	1	0.5129	0.7225	1.2314	1.1577	0.8638			0.7072	0.5002	
3	1	0.2683	0.8753	1.0688	0.5861	1.7061			0.9727	5.0301	
	2	0.5366		0.6265					0.6265		
4	1	0.3872	0.3850	0.5969	1.4182	0.7051			0.5951		
	2	0.1605	0.9297	1.0313	0.3402	2.9391			1.0010	9.4918	
5	1	0.2767	0.5902	0.6905	0.8490	1.1779			0.5522	2.2849	
	2	0.1057	0.9550	1.0178	0.2200	4.5451			1.0054	13.2037	
	3	0.3420		0.3623					0.3623		
6	1	0.2784	0.2596	0.3963	1.4627	0.6836			0.3827		
	2	0.2037	0.7091	0.7680	0.5522	1.8109			0.7071	5.5025	
	3	0.0746	0.9687	1.0114	0.1536	6.5119			1.0055	16.2998	
7	1	0.2241	0.4349	0.5040	0.9161	1.0916			0.3839	1.7838	
	2	0.1550	0.7836	0.8228	0.3881	2.5767			0.7912	8.3880	
	3	0.0553	0.9771	1.0081	0.1130	8.8487			1.0049	18.9515	
	4	0.2487		0.2562					0.2562		
8	1	0.2144	0.1955	0.2968	1.4779	0.6767			0.2835		
	2	0.1817	0.5565	0.5989	0.6208	1.6109			0.5381	4.5815	
	3	0.1214	0.8328	0.8610	0.2885	3.4662			0.8429	10.8885	
	4	0.0426	0.9824	1.0060	0.0867	11.5305			1.0041	21.2452	
9	1	0.1831	0.3425	0.3954	0.9429	1.0605			0.2947	1.6023	
	2	0.1493	0.6436	0.6727	0.4520	2.2126			0.6374	7.1258	
	3	0.0974	0.8671	0.8884	0.2233	4.4779			0.8773	13.0759	
	4	0.0338	0.9861	1.0046	0.0686	14.5829			1.0034	23.2820	
	5	0.1949		0.1984					0.1984		
10	1	0.1736	0.1566	0.2338	1.4851	0.6734			0.2221		
	2	0.1566	0.4545	0.4807	0.6515	1.5349			0.4267	4.2087	
	3	0.1243	0.7078	0.7186	0.3459	2.8907			0.6968	9.3520	
	4	0.0798	0.8919	0.8955	0.1782	5.6107			0.8883	15.0149	
	5	0.0275	0.9887	0.9891	0.0556	17.9833			0.9883	25.1008	

**Figure 8.30:** 0.5 dB Chebyshev Design Table

ANALOG FILTERS  
STANDARD RESPONSES

ORDER	SECTION	REAL PART	IMAGINARY PART	F <sub>0</sub>	$\alpha$	Q	-3 dB FREQUENCY	PEAKING FREQUENCY	PEAKING LEVEL
2	1	0.4508	0.7351	0.8623	1.0456	0.9564	0.5896	0.9995	
	2	0.2257	0.8822	0.9106	0.4957	2.0173	0.8528	6.3708	
3	1	0.4513	0.4513	0.4513		0.4513			
	2	0.1325	0.9339	0.5019	1.2746	0.7845	0.2174	0.1557	
4	1	0.3199	0.3868	0.9433	0.2809	3.5594	0.9245	11.1142	
	2	0.0865	0.9575	0.9614	0.1800	5.5559	0.5467	3.5089	
5	1	0.2265	0.5918	0.6337	0.7149	1.3988	0.9536	14.9305	
	2	0.0608	0.2800	0.2800		0.2800			
6	1	0.2268	0.2601	0.3451	1.3144	0.7608	0.1273	0.0813	
	2	0.1550	0.7106	0.7273	0.4262	2.3462	0.6935	7.6090	
7	1	0.1819	0.4354	0.4719	0.7710	1.2971	0.3956	2.9579	
	2	0.1259	0.7846	0.7946	0.3169	3.1558	0.7744	10.0927	
8	1	0.0449	0.9785	0.9795	0.0918	10.8982	0.9775	20.7563	
	2	0.2019	0.2019	0.2019		0.2019			
9	1	0.1737	0.1956	0.2616	1.3280	0.7530	0.0899	0.0611	
	2	0.1473	0.5571	0.5762	0.5112	1.9560	0.5373	6.1210	
10	1	0.0984	0.8337	0.8395	0.2344	4.2657	0.8279	12.6599	
	2	0.0346	0.9836	0.9842	0.0702	14.2391	0.9830	23.0750	
11	1	0.1482	0.3427	0.3734	0.7938	1.2597	0.3090	2.7498	
	2	0.1208	0.6442	0.6554	0.3686	2.7129	0.6328	8.8187	
12	1	0.0788	0.8679	0.8715	0.1809	5.5268	0.8643	14.8852	
	2	0.0274	0.9869	0.9873	0.0555	18.0226	0.9865	25.1197	
13	1	0.1403	0.1567	0.2103	1.3341	0.7496	0.0698	0.0530	
	2	0.1266	0.4548	0.4721	0.5363	1.8645	0.4368	5.7354	
14	1	0.1005	0.7084	0.7155	0.2809	3.5597	0.7012	11.1147	
	2	0.0645	0.8926	0.8949	0.1441	6.9374	0.8903	16.8466	
15	1	0.0222	0.9895	0.9897	0.0449	22.2916	0.9893	26.9650	

**Figure 8.31:** 1 dB Chebyshev Design Table

## ► BASIC LINEAR DESIGN

ORDER	SECTION	REAL PART	IMAGINARY PART	$F_o$	$\alpha$	$Q$	-3 dB FREQUENCY	PEAKING FREQUENCY	PEAKING LEVEL
2	1	1.1050	0.6368	1.2754	1.7328	0.5771	1.0020		
3	1	1.0509	1.0025	1.4524	1.4471	0.6910	1.4185		
	2	1.3270		1.3270			1.3270		
4	1	1.3596	0.4071	1.4192	1.9160	0.5219	0.9705		
	2	0.9877	1.2476	1.5912	1.2414	0.8055		0.7622	0.2349
5	1	1.3851	0.7201	1.5611	1.7745	0.5635	1.1876		
	2	0.9606	1.4756	1.7607	1.0911	0.9165		1.1201	0.7768
	3	1.5069		1.5069			1.5069		
6	1	1.5735	0.3213	1.6060	1.9596	0.5103	1.0638		
	2	1.3836	0.9727	1.6913	1.6361	0.6112	1.4323		
	3	0.9318	1.6640	1.9071	0.9772	1.0234		1.3786	1.3851
7	1	1.6130	0.5896	1.7174	1.8784	0.5324	1.2074		
	2	1.3797	1.1923	1.8235	1.5132	0.6608	1.6964		
	3	0.9104	1.8375	2.0507	0.8879	1.1262		1.5961	1.9860
	4	1.6853		1.6853			1.6853		
8	1	1.7627	0.2737	1.7838	1.9763	0.5060	1.1675		
	2	0.8955	2.0044	2.1953	0.8158	1.2258		1.7932	2.5585
	3	1.3780	1.3926	1.9591	1.4067	0.7109		0.2011	0.0005
	4	1.6419	0.8256	1.8378	1.7868	0.5597	1.3849		
	5	1.8575		1.8575			1.8575		
9	1	1.8081	0.5126	1.8794	1.9242	0.5197	1.2774		
	2	1.6532	1.0319	1.9488	1.6966	0.5894	1.5747		
	3	1.3683	1.5685	2.0815	1.3148	0.7606		0.7668	0.0807
	4	0.8788	2.1509	2.3235	0.7564	1.3220		1.9632	3.0949
	5	1.8575		1.8575			1.8575		
10	1	1.9335	0.2451	1.9490	1.9841	0.5040	1.2685		
	2	1.8467	0.7335	1.9870	1.8587	0.5380	1.4177		
	3	1.6661	1.2246	2.0678	1.6115	0.6205	1.7848		
	4	1.3648	1.7395	2.2110	1.2346	0.8100		1.0785	0.2531
	5	0.8686	2.2984	2.4580	0.7067	1.4150		2.1291	3.5944

**Figure 8.32: Bessel Design Table**

ANALOG FILTERS  
STANDARD RESPONSES

ORDER	SECTION	REAL PART	IMAGINARY PART	$F_0$	$\alpha$	$Q$	-3 dB FREQUENCY	PEAKING FREQUENCY	PEAKING LEVEL
2	1	1.0087	0.6680	1.2098	1.6675	0.5997	0.9999		
3	1	0.8541	1.0725	1.3710	1.2459	0.8026		0.6487	0.2232
	2	1.0459		1.0459			1.0459		
4	1	0.9648	0.4748	1.0753	1.7945	0.5573	0.8056		
	2	0.7448	1.4008	1.5885	0.9389	1.0650		1.1864	1.6286
5	1	0.8915	0.8733	1.2480	1.4287	0.6999	1.2351		
	2	0.6731	1.7085	1.8363	0.7331	1.3641		1.5703	3.3234
	3	0.9430		0.9430			0.9430		
6	1	0.8904	0.4111	0.9807	1.8158	0.5507	0.7229		
	2	0.8233	1.2179	1.4701	1.1201	0.8928		0.8975	0.6495
	3	0.6152	1.9810	2.0743	0.5932	1.6859		1.8831	4.9365
7	1	0.8425	0.7791	1.1475	1.4684	0.6810	1.1036		
	2	0.7708	1.5351	1.7177	0.8975	1.1143		1.3276	1.9162
	3	0.5727	2.2456	2.3175	0.4942	2.0233		2.1713	6.3948
	4	0.8615		0.8615			0.8615		
8	1	0.8195	0.3711	0.8996	1.8219	0.5489	0.6600		
	2	0.7930	1.1054	1.3604	1.1658	0.8578		0.7701	0.4705
	3	0.7213	1.8134	1.9516	0.7392	1.3528		1.6638	3.2627
	4	0.5341	2.4761	2.5330	0.4217	2.3713		2.4178	7.6973
9	1	0.7853	0.7125	1.0604	1.4812	0.6751	1.0102		
	2	0.7555	1.4127	1.6020	0.9432	1.0602		1.1937	1.6005
	3	0.6849	2.0854	2.1950	0.6241	1.6024		1.9697	4.5404
	4	0.5060	2.7133	2.7601	0.3667	2.7274		2.6657	8.8633
	5	0.7983		0.7983			0.7983		
10	1	0.7592	0.3413	0.8324	1.8241	0.5482	0.6096		
	2	0.7467	1.0195	1.2637	1.1818	0.8462		0.6941	0.4145
	3	0.7159	1.6836	1.8295	0.7826	1.2778		1.5238	2.8507
	4	0.6475	2.3198	2.4085	0.5377	1.8598		2.2276	5.7152
	5	0.4777	2.9128	2.9517	0.3237	3.0895		2.8734	9.9130

**Figure 8.33: Linear Phase with Equiripple Error of 0.05° Design Table**

## ► BASIC LINEAR DESIGN

ORDER	SECTION	REAL PART	IMAGINARY PART	$F_0$	$\alpha$	$Q$	-3 dB FREQUENCY	PEAKING FREQUENCY	PEAKING LEVEL
2	1	0.8590	0.6981	1.1069	1.5521	0.6443	1.0000		
3	1	0.6969	1.1318	1.3292	1.0486	0.9536	0.8257	0.8918	0.9836
4	1	0.7448	0.5133	0.9045	1.6468	0.6072	0.7597	1.3713	3.1817
4	2	0.6037	1.4983	1.6154	0.7475	1.3379			
5	1	0.6775	0.9401	1.1588	1.1693	0.8552		0.6518	0.4579
5	2	0.5412	1.8256	1.9041	0.5684	1.7592		1.7435	5.2720
5	3	0.7056		0.7056			0.7056		
6	1	0.6519	0.4374	0.7850	1.6608	0.6021	0.6522		
6	2	0.6167	1.2963	1.4355	0.8592	1.1639		1.1402	2.2042
6	3	0.4893	2.0982	2.1545	0.4542	2.2016		2.0404	7.0848
7	1	0.6190	0.8338	1.0385	1.1922	0.8388		0.5586	0.3798
7	2	0.5816	1.6455	1.7453	0.6665	1.5004		1.5393	4.0353
7	3	0.4598	2.3994	2.4431	0.3764	2.6567		2.3549	8.6433
7	4	0.6283		0.6283			0.6283		
8	1	0.5791	0.3857	0.6958	1.6646	0.6007	0.5764		
8	2	0.5665	1.1505	1.2824	0.8835	1.1319		1.0014	2.0187
8	3	0.5303	1.8914	1.9643	0.5399	1.8521		1.8155	5.6819
8	4	0.4148	2.5780	2.6112	0.3177	3.1475		2.5444	10.0703
8	5								
9	1	0.5688	0.7595	0.9489	1.1989	0.8341		0.5033	0.3581
9	2	0.5545	1.5089	1.6076	0.6899	1.4496		1.4033	3.7748
9	3	0.5179	2.2329	2.2922	0.4519	2.2130		2.1720	7.1270
9	4	0.4080	2.9028	2.9313	0.2784	3.5923		2.8740	11.1925
9	5	0.5728		0.5728			0.5728		
10	1	0.5249	0.3487	0.6302	1.6659	0.6003	0.5215		
10	2	0.5193	1.0429	1.1650	0.8915	1.1217		0.9044	1.9598
10	3	0.5051	1.7264	1.7988	0.5616	1.7806		1.6509	5.3681
10	4	0.4711	2.3850	2.4311	0.3876	2.5802		2.3380	8.3994
10	5	0.3708	2.9940	3.0169	0.2458	4.0681		2.9709	12.2539

Figure 8.34: Linear Phase with Equiripple Error of 0.5° Design Table

ANALOG FILTERS  
STANDARD RESPONSES

ORDER	SECTION	REAL PART	IMAGINARY PART	$F_0$	$\alpha$	Q	-3 dB FREQUENCY	PEAKING FREQUENCY	PEAKING LEVEL
3	1	0.9360	1.2168	1.5352	1.2194	0.8201	0.9360	0.7775	0.2956
	2	0.9360		0.9360					
4	1	0.9278	1.6695	1.9363	0.9583	1.0435	0.8582	1.4239	1.5025
	2	0.9192	0.5560	1.0743	1.7113	0.5844			
5	1	0.8075	0.9973	1.2832	1.2585	0.7946	0.5853	0.1921	
	2	0.7153	0.2053	0.7442	1.9224	0.5202			
	3	0.8131		0.8131					
6	1	0.7019	0.4322	0.8243	1.7030	0.5872	0.6627	1.1080	1.7809
	2	0.6667	1.2931	1.4549	0.9165	1.0911			
	3	0.4479	2.1363	2.1827	0.4104	2.4366			
7	1	0.6155	0.7703	0.9860	1.2485	0.8010	0.4632	0.2168	
	2	0.5486	1.5154	1.6116	0.6808	1.4689			
	3	0.2905	2.1486	2.1681	0.2680	3.7318			
	4	0.6291		0.6291					
8	1	0.5441	0.3358	0.6394	1.7020	0.5876	0.5145	0.8512	1.7432
	2	0.5175	0.9662	1.1226	0.9220	1.0846			
	3	0.4328	1.6100	1.6672	0.5192	1.9260			
	4	0.1978	2.0103	2.0797	0.1902	5.2571			
9	1	0.4961	0.6192	0.7934	1.2505	0.7997	0.3705	0.2116	
	2	0.4568	1.2445	1.2976	0.7041	1.4203			
	3	0.3592	1.7429	1.7795	0.4037	2.4771			
	4	0.1489	2.1003	2.1056	0.1414	7.0704			
	5	0.5065		0.5065					
10	1	0.4535	0.2794	0.5327	1.7028	0.5873	0.4283	0.7055	1.6904
	2	0.4352	0.8289	0.9362	0.9297	1.0756			
	3	0.3886	1.3448	1.3998	0.5552	1.8011			
	4	0.2908	1.7337	1.8072	0.3218	3.1074			
	5	0.1136	2.0599	2.0630	0.1101	9.0802			

**Figure 8.35: Gaussian to 12 dB Design Table**

## ► BASIC LINEAR DESIGN

ORDER	SECTION	REAL PART	IMAGINARY PART	$F_0$	$\alpha$	$Q$	-3 dB FREQUENCY	PEAKING FREQUENCY	PEAKING LEVEL
3	1	0.9622	1.2214	1.55649	1.2377	0.8080	0.7523	0.2448	
	2	0.9776	0.5029	1.0984	1.7785	0.5623			
4	1	0.7940	0.5029	0.9399	1.6896	0.5919	0.7636	1.4058	3.0859
	2	0.6304	1.5407	1.6647	0.7574	1.3203			
5	1	0.6190	0.8254	1.0317	1.1999	0.8334	0.5460	0.3548	
	2	0.3559	1.5688	1.6087	0.4425	2.2600			
	3	0.6650	0.6650	0.6650					
6	1	0.5433	0.3431	0.6426	1.6910	0.5914	0.5215	0.8831	2.2992
	2	0.4672	0.9991	1.1029	0.8472	1.1804			
	3	0.2204	1.5067	1.5227	0.2895	3.4545			
7	1	0.4580	0.5932	0.7494	1.2223	0.8182	0.3770	0.2874	
	2	0.3649	1.1286	1.1861	0.6153	1.6253			
	3	0.1522	1.4938	1.5015	0.2027	4.9328			
	4	0.4828	0.4828	0.4828					
8	1	0.4222	0.2640	0.4979	1.6958	0.5897	0.4026	0.6697	1.9722
	2	0.3833	0.7716	0.8616	0.8898	1.1239			
	3	0.2678	1.2066	1.2360	0.4333	2.3076			
	4	0.1122	1.4798	1.4840	0.1512	6.6134			
9	1	0.3700	0.4704	0.5985	1.2365	0.8088	0.2905	0.2480	
	2	0.3230	0.9088	0.9626	0.6711	1.4901			
	3	0.2309	1.2624	1.2843	0.3596	2.7811			
	4	0.0860	1.4740	1.4765	0.1165	8.5804			
	5	0.3842	0.3842	0.3842					
10	1	0.3384	0.2101	0.3983	1.6991	0.5885	0.3212	0.5309	1.8164
	2	0.3164	0.6180	0.6943	0.9114	1.0972			
	3	0.2677	0.9852	1.0209	0.5244	1.9068			
	4	0.1849	1.2745	1.2878	0.2871	3.4825			
	5	0.0671	1.4339	1.4405	0.0931	10.7401			

**Figure 8.36:** Gaussian to 6 dB Design Table