

$$\{x \in \mathbb{R}, x \geq 1\} = \{y \in \mathbb{R}, y \geq 1\}$$

↔
muette

$$\lim_{t \rightarrow +\infty} \exp(-t) = \lim_{u \rightarrow +\infty} \exp(-u)$$

$$\sum_{k=1}^5 k = 1+2+3+4+5, \quad \sum_{k=0}^n k = \frac{n(n+1)}{2}$$

$$\sum_{i=1}^5 i$$

$$\prod_{i=1}^4 i = 1 \times 2 \times 3 \times 4 = 4!$$

↙ factorielle

$$n! = 1 \times 2 \times 3 \times \dots \times (n-1) \times n$$

Représentation graphique

f est bornée :

- f est majorée : $\exists M \in \mathbb{R} \forall x \in \mathbb{R} \quad f(x) \leq M$

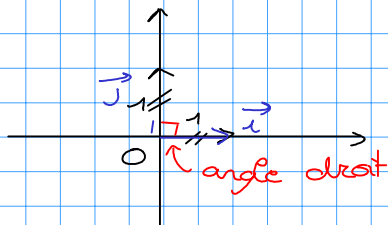
- f est minorée : $\exists m \in \mathbb{R} \forall x \in \mathbb{R} \quad f(x) \geq m$

Donc $\exists M \in \mathbb{R} \exists m \in \mathbb{R} \forall x \in \mathbb{R} \quad m \leq f(x) \leq M$.

Si f est impaire,

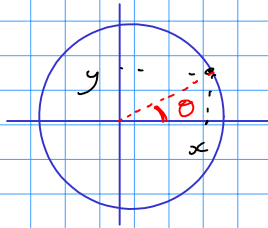
$$f(0) = 0 : \quad f(0) = f(-0) \stackrel{f \text{ est impaire}}{=} -f(0)$$

$$\text{donc } f(0) = 0.$$



repère

ortho norme

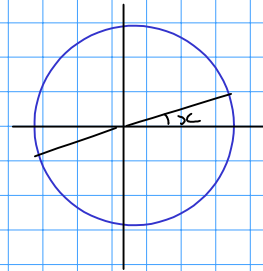
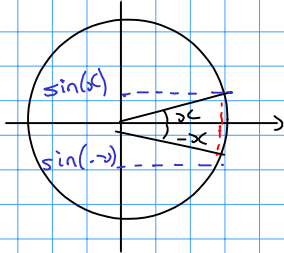


$$x^2 + y^2 = 1$$

$$x = \cos(\theta)$$

$$y = \sin(\theta)$$

Théorème de Thalès.



Si n est pair

$$\cos(x + n\pi) = \cos(x)$$

Si n est impair,

$$\cos(x + n\pi) = -\cos(x)$$

$$n = 2p + 1, \quad \cos(x + n\pi) = \cos(x + \pi + 2p\pi)$$

$$\cos(x + \pi) = -\cos(x)$$

$$\cos(x + 2\pi) = \cos(x)$$

$$\cos(x + 3\pi) = -\cos(x)$$