
Oscillateur conservatif lineaire à un degré de liberté

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Question1

```
%1.1
w0 = 2*pi;
q = dsolve('D2q+(2*pi)^2*q=0', 'q(0)=1', 'Dq(0)=0');

%1.2
E = 0.5*((diff(q))^2+(2*pi*q)^2);
E = simplify(E)

##: Support of character vectors and strings will be removed in a
future
release. Use sym objects to define differential equations instead.

E =
2*pi^2
```

Question2 EULER implicite

```
% 2.1 on peut trouver que D2q=-w0^2*q. Donc, si l'on simplifier
l'équation
%5, on obtient les équations 6

%2.2
%methode 1
q2 = [1];
dq2 = [0];
deltat=0.01;
for i=1:300
    q2=[q2,q2(i)+deltat*dq2(i)];
    dq2=[dq2,dq2(i)+deltat*(-w0^2*q2(i))];
end

%2.3
```

```
figure(1);
fplot(q,[0,3]);
hold on;
plot([0:0.01:3],q2);
hold off;

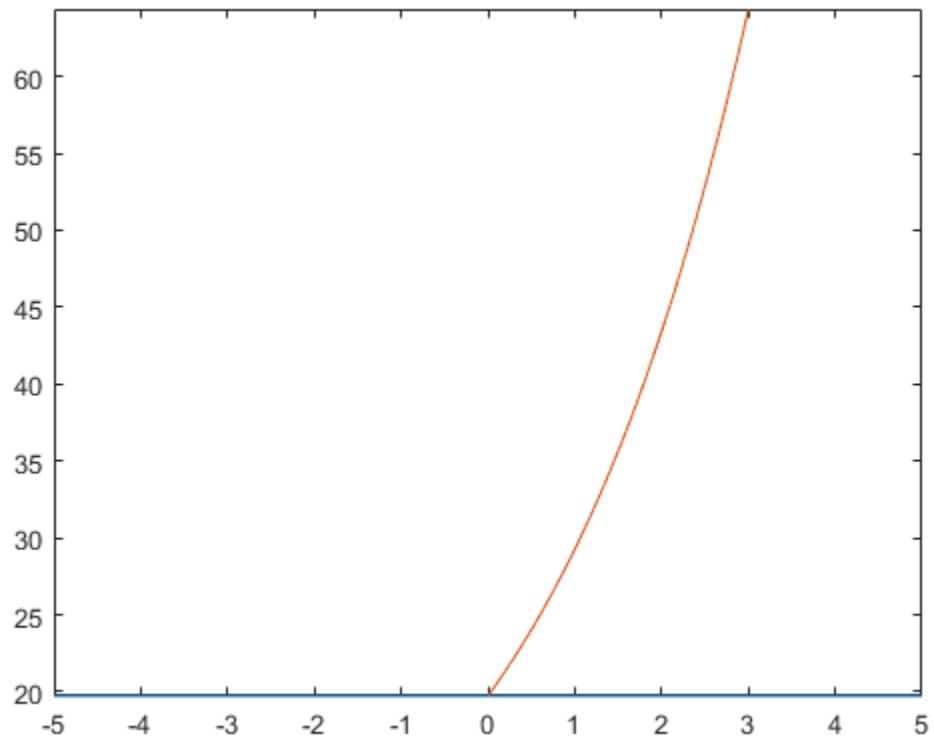
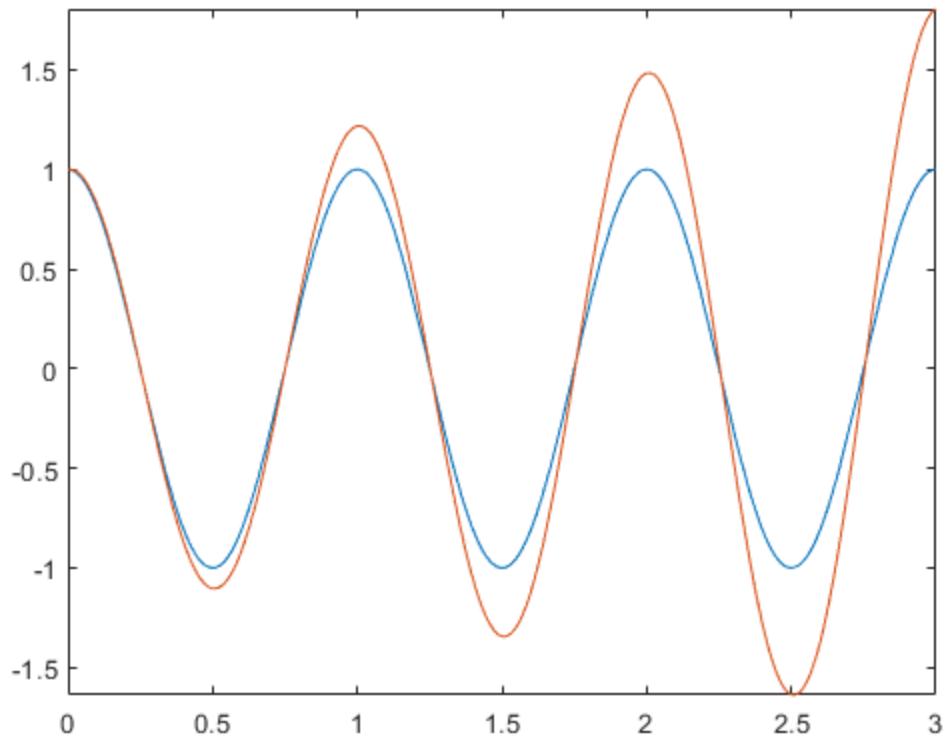
%2.4
E2 = 0.5.*((dq2).^2+(2*pi.*q2).^2);
figure(2);
fplot(E);
hold on;
plot([0:0.01:3],E2);
hold off;
%plus le deltat est petit, plus le résultat est proche avec la
%solution
%exacte

%2.5
syms deltat1;
Ma_Amplifica=[1,deltat1;-w0^2*deltat1,1];
[x,y]=eig(Ma_Amplifica)

x =
[ (70368744177664*((2778046668940015^(1/2)*deltat1*1i)/8388608
- 1))/(2778046668940015*deltat1) + 70368744177664/
(2778046668940015*deltat1), 70368744177664/(2778046668940015*deltat1)
- (70368744177664*((2778046668940015^(1/2)*deltat1*1i)/8388608 + 1))/(
2778046668940015*deltat1)]
[
1,
1]

y =
[ 1 - (2778046668940015^(1/2)*deltat1*1i)/8388608,
0]
[
0,
(2778046668940015^(1/2)*deltat1*1i)/8388608 + 1]
```

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question3 EULER explicite

```
%3.1
q3 = [1];
dq3 = [0];
deltat=0.01;
for i=1:300
    q3=[q3,(q3(i)+deltat*dq3(i))/(1+deltat^2*w0^2)];
    dq3=[dq3,dq3(i)+deltat*(-w0^2*q3(i+1))];
end

%3.2
figure(3);
fplot(q,[0,3])
hold on;
plot([0:0.01:3],q3)
hold off;

%3.3 on change deltat

%3.4
E3 = 0.5.*((dq3).^2+(2*pi.*q3).^2);
figure(4);
fplot(E);
hold on;
plot([0:0.01:3],E3);
hold off;
%plus le deltat est petit, plus le résultat est loin avec la solution
%exacte

% 3.5
syms deltat2;
Ma_Amplifica2=inv([1,-deltat2;w0^2*deltat2,1]);
[x,y]=eig(Ma_Amplifica2)

x =
[ 70368744177664/(2778046668940015*deltat2)
+ (8388608*(2778046668940015*deltat2^2 +
70368744177664)*(2778046668940015^(1/2)*deltat2 - 8388608i))/(
2778046668940015*deltat2*(deltat2^2*2778046668940015i +
70368744177664i)), 70368744177664/(2778046668940015*deltat2)
- (8388608*(2778046668940015*deltat2^2 +
70368744177664)*(2778046668940015^(1/2)*deltat2 + 8388608i))/(
2778046668940015*deltat2*(deltat2^2*2778046668940015i +
70368744177664i))]
[
1,
```

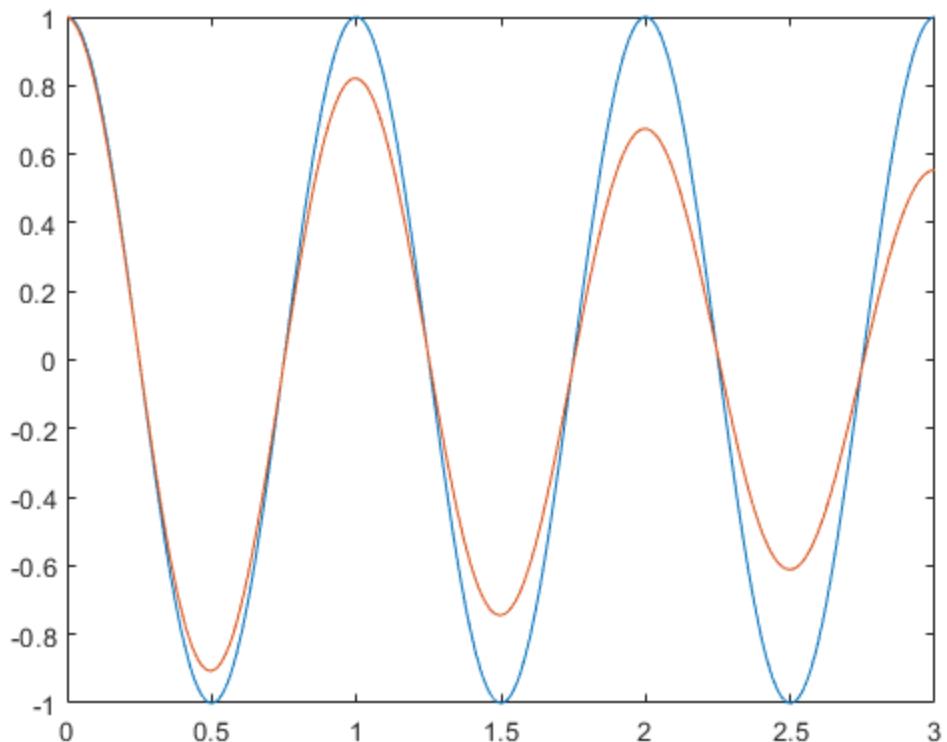
1]

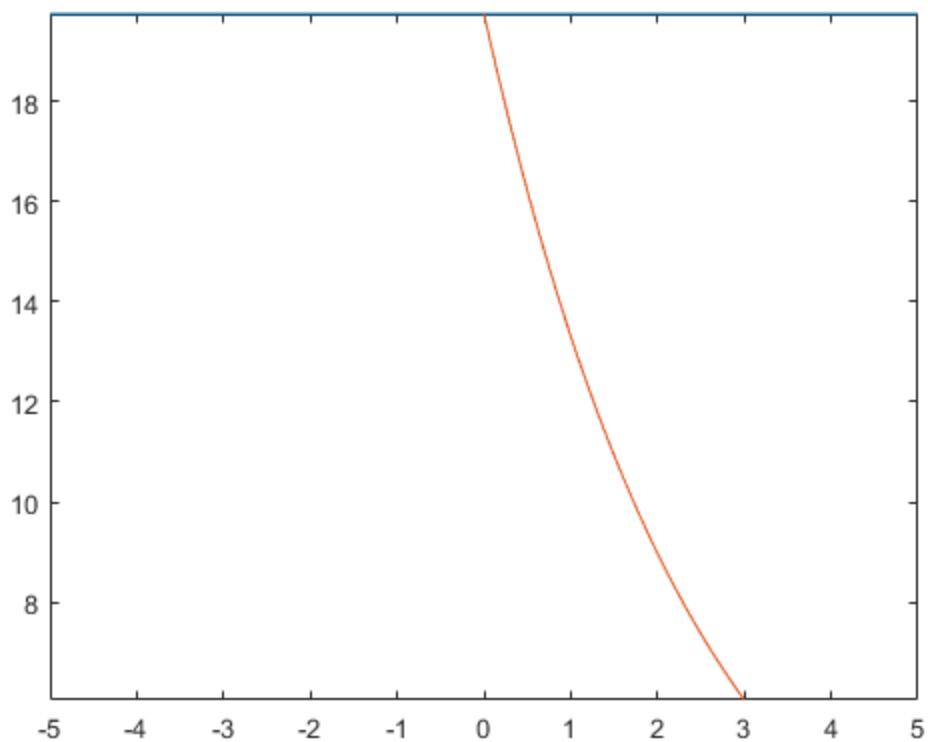
$y =$

$$[-(8388608 * (2778046668940015^{(1/2)} * \text{deltat2} - 8388608i)) / (\text{deltat2}^2 * 2778046668940015i + 70368744177664i),$$

0]

$$[0, \\ (8388608 * (2778046668940015^{(1/2)} * \text{deltat2} + 8388608i)) / (\text{deltat2}^2 * 2778046668940015i + 70368744177664i)]$$





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